

Fire resistance assessment of Composite structures

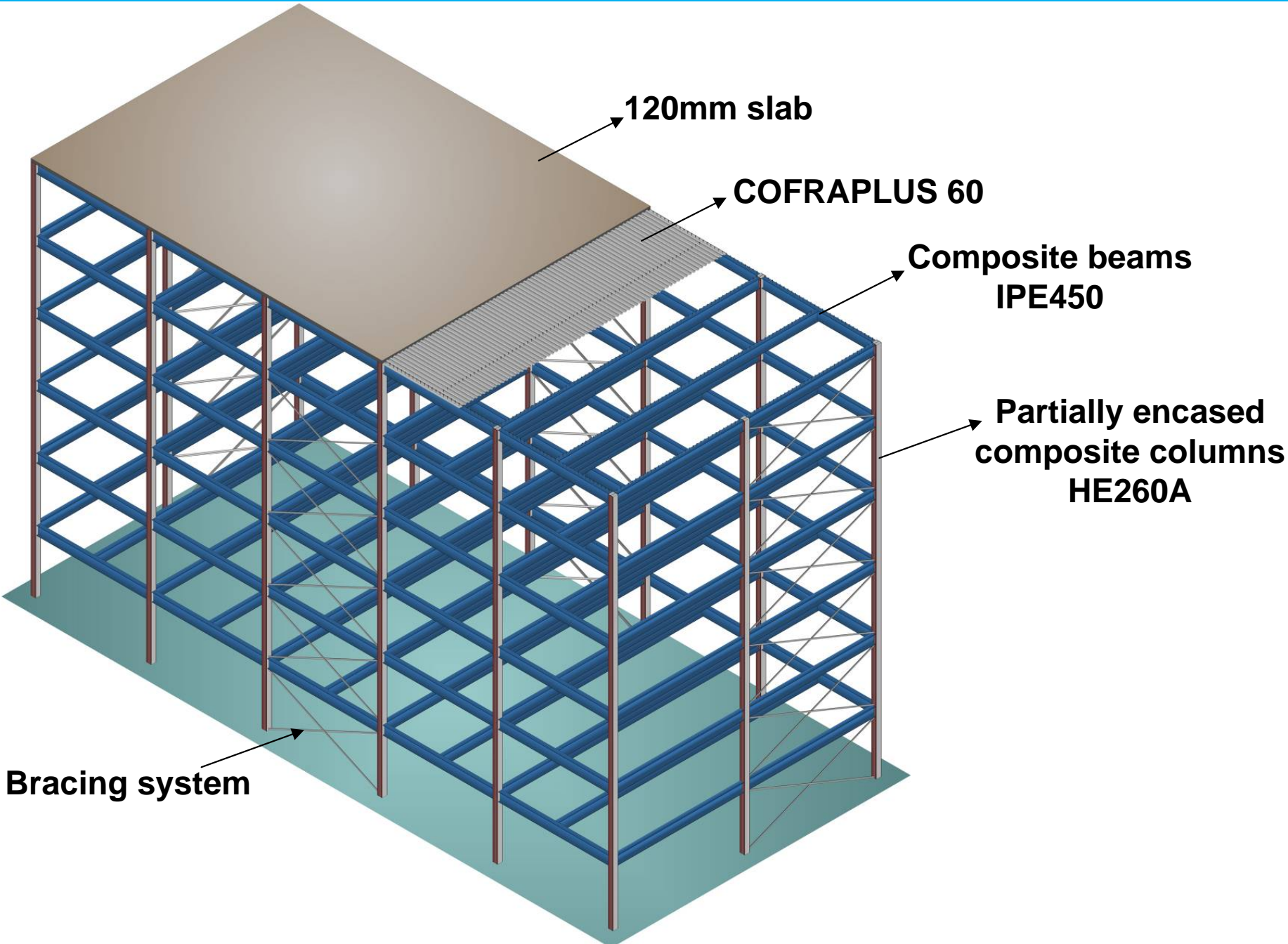
Basic design methods
Worked examples

CAJOT Louis-Guy

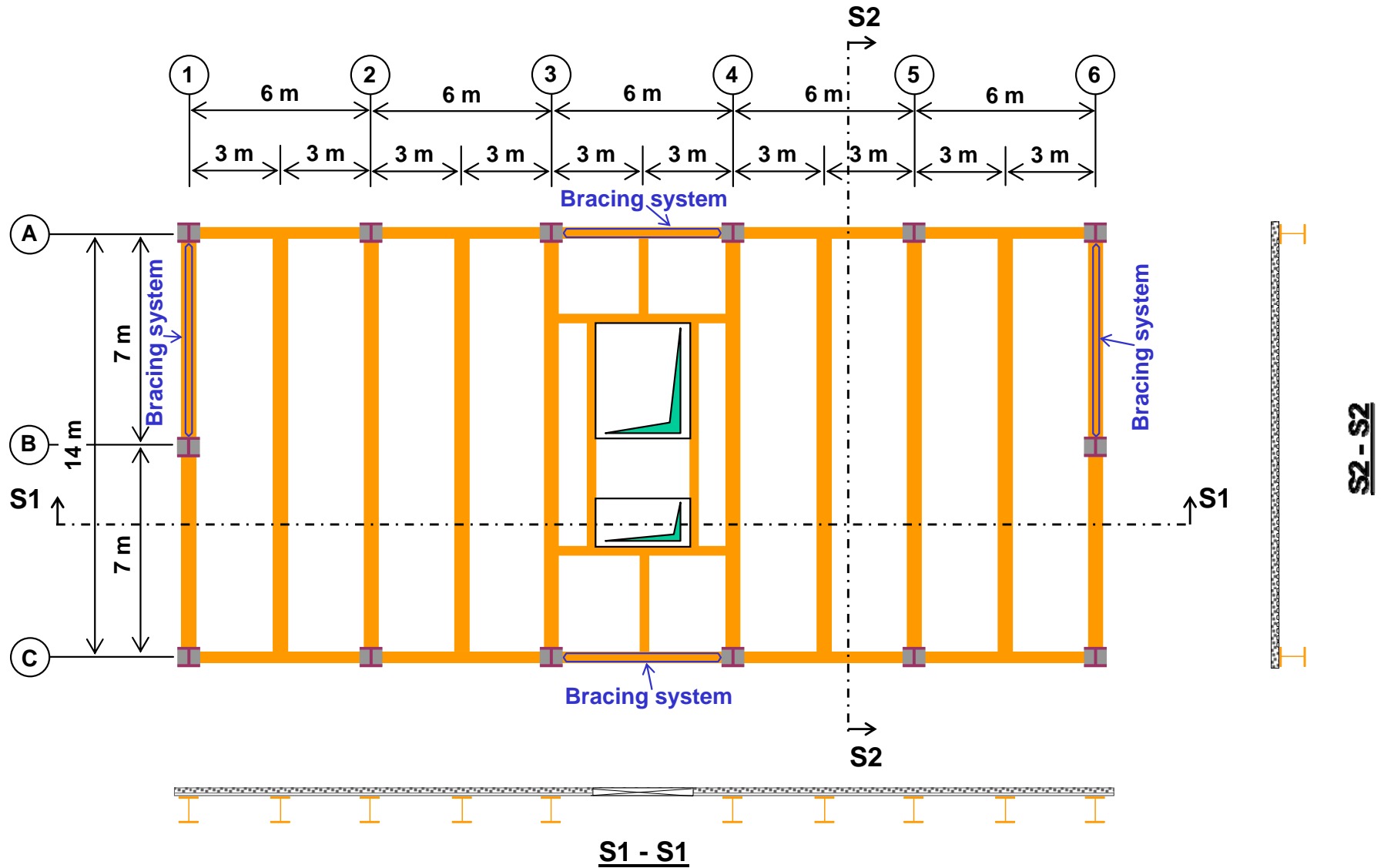
Chairman of CEN/TC250/SC4/EG - Fire Part

ArcelorMittal

The Building (R+5)



Composite slab, composite beams, composite columns



Actions (for all floor levels)

- ⇒ Self weight G1
 - ✓ Composite slab unit weight : 2.12 kN/m²
 - ✓ Steel structural members
- ⇒ Permanent load G2
 - ✓ Finishing, embedded services, partitions : 1.50 kN/m²
- ⇒ Façade G3 : 2 kN/m
- ⇒ Characteristic values of variable loads and ψ factors

Type	q_k	ψ_1	ψ_2
Live load on floors	4.0 kN/m ²	0.7	0.6
Snow on roof	1.7 kN/m ²	0.2	0.0

Structural members

⇒ Composite slab

- ✓ Total thickness: 12 cm
- ✓ Steel deck: COFRAPLUS60
- ✓ Thickness of steel deck: 0.75 mm
- ✓ Continuous slab over 2 spans

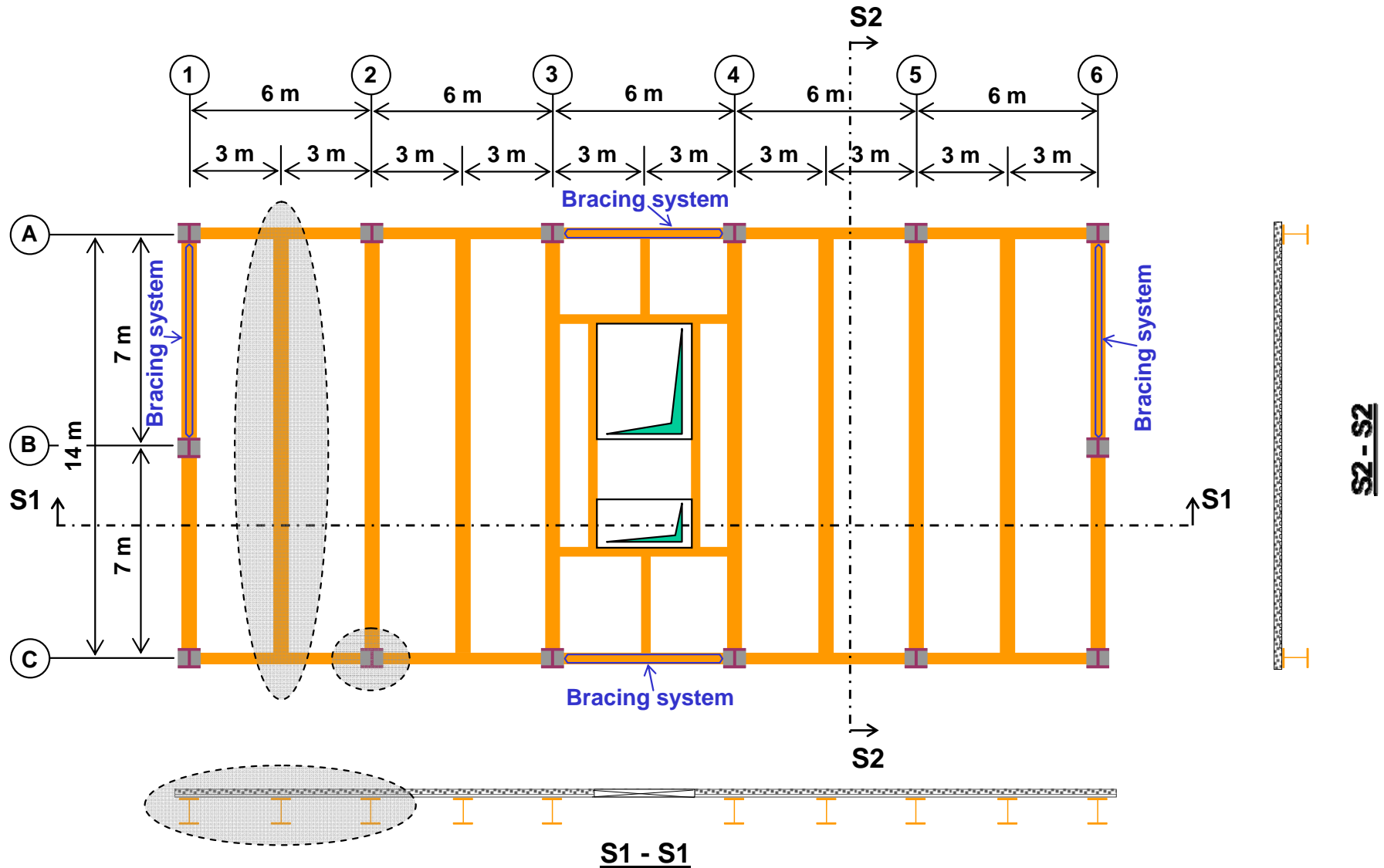
⇒ Secondary beams

- ✓ IPE450 linked with headed studs to the composite slab; fire protected steel sections
- ✓ Alternative : Partially encased composite beams IPE450; fire protection obtained through partial encasement

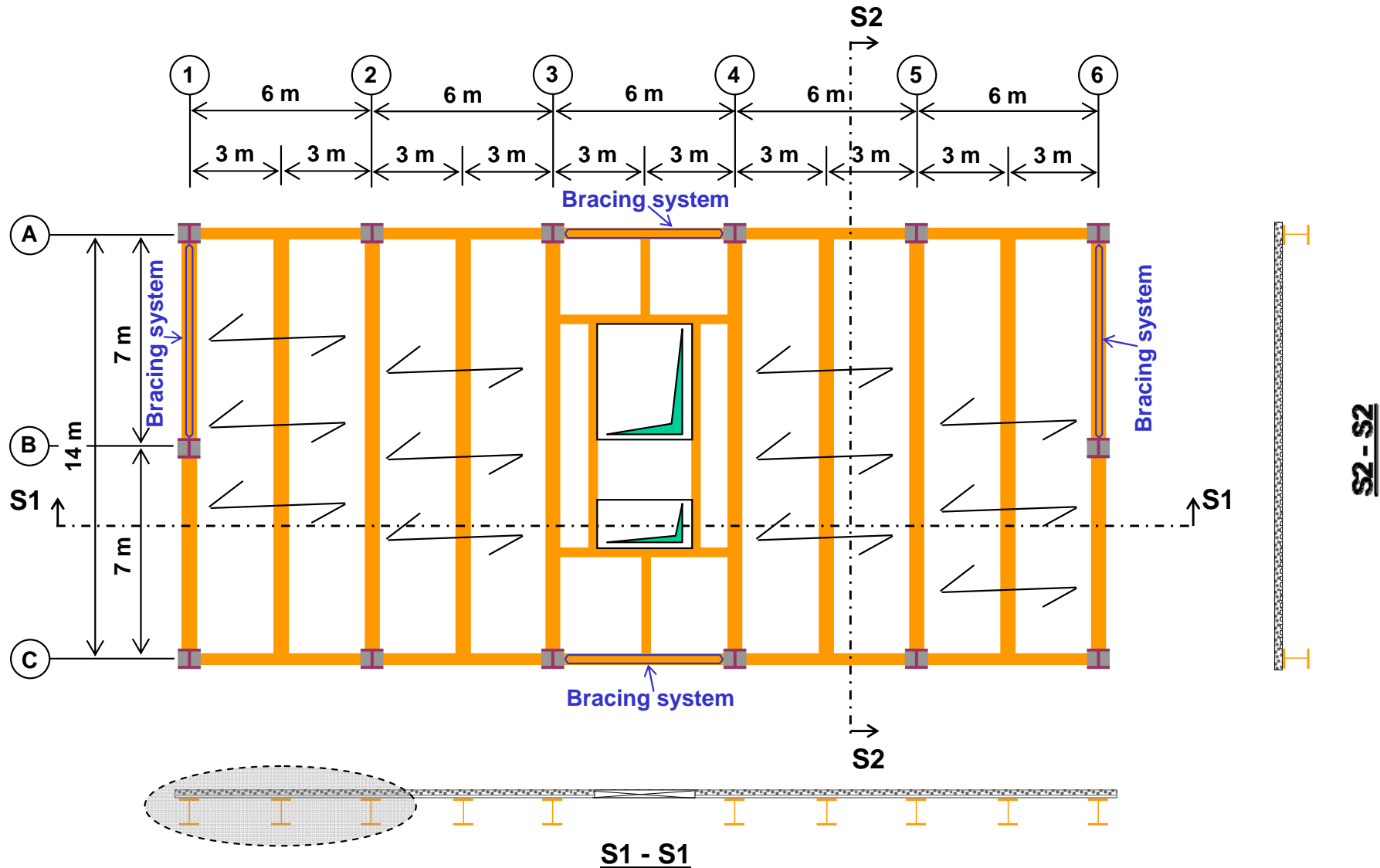
⇒ Columns for ground level

- ✓ Facade columns: Partially encased HEA260
- ✓ Alternative: Fully encased HEB160

Composite slab, composite beams, composite columns



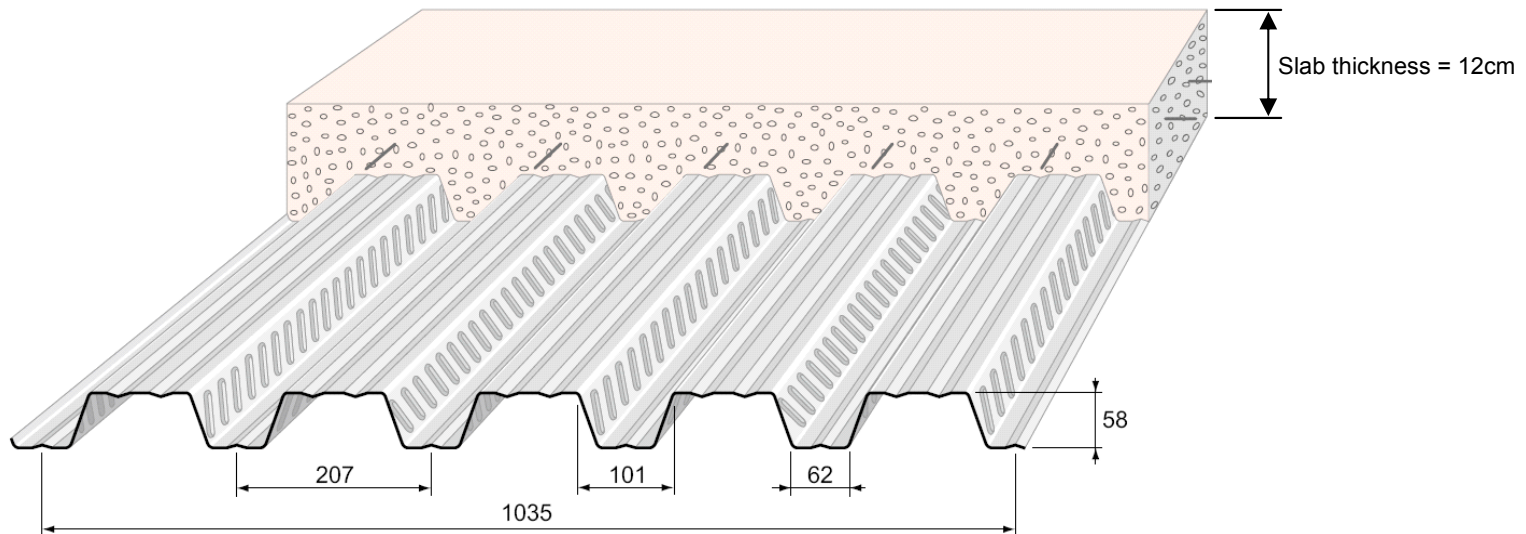
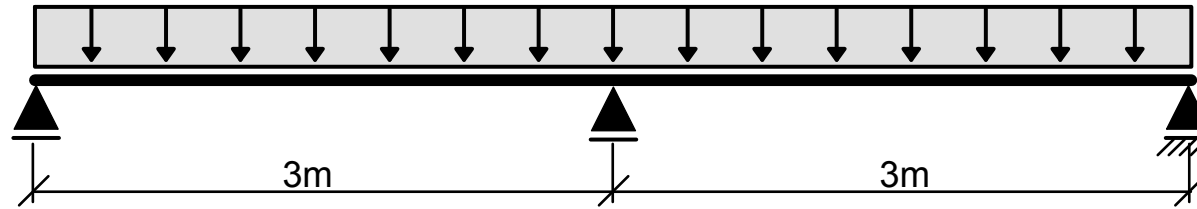
Composite slab continuous on 3 supports



Verification of the composite slab



Summary of data



Required fire resistance : R60

Material characteristics

Steel decking : $f_y = 350 \text{ N/mm}^2$

Concrete : C25/30 ; $f_c = 25 \text{ N/mm}^2$

Rebars : $f_y = 500 \text{ N/mm}^2$

Mesh ST25 ; $A = 2,57 \text{ cm}^2/\text{m}$

Ribs : 1 $\phi 8$ /rib

Loads

Permanent loads:

Steel decking : $g_{t,k} = 0,085 \text{ kN/m}^2$

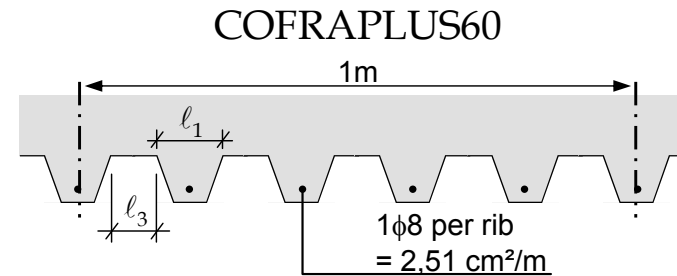
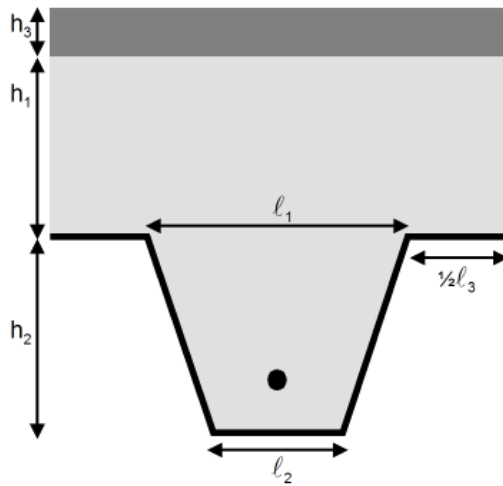
Concrete : $g_{b,k} = 2,03 \text{ kN/m}^2$

Permanent load : $g_{c,k} = 1,5 \text{ kN/m}^2$

Variable load:

Variable load : $q_k = 4,0 \text{ kN/m}^2$

Geometric parameters



$$\begin{array}{lll}
 h_1 = 62 \text{ mm} & h_2 = 58 \text{ mm} & h_3 = 0 \\
 l_1 = 101 \text{ mm} & l_2 = 62 \text{ mm} & l_3 = 106 \text{ mm}
 \end{array}$$

Application field

Trapezoidal steel decking profiles [mm]	Existing geometric parameters [mm]	Condition fulfilled ?
$80 \leq l_1 \leq 155$	$l_1 = 101$	OK
$32 \leq l_2 \leq 132$	$l_2 = 62$	OK
$40 \leq l_3 \leq 115$	$l_3 = 106$	OK
$50 \leq h_1 \leq 125$	$h_1 = 62$	OK
$50 \leq h_2 \leq 100$	$h_2 = 58$	OK

Fire resistance according to thermal insulation

$$t_i = a_0 + a_1 \cdot h_1' + a_2 \cdot \Phi + a_3 \cdot \frac{A}{L_r} + a_4 \cdot \frac{1}{l_3} + a_5 \cdot \frac{A}{L_r} \cdot \frac{1}{l_3}$$

$$t_i = (-28,8) + 1,55 \cdot h_1' + (-12,6) \cdot \Phi + 0,33 \cdot \frac{A}{L_r} + (-735) \cdot \frac{1}{l_3} + 48 \cdot \frac{A}{L_r} \cdot \frac{1}{l_3}$$

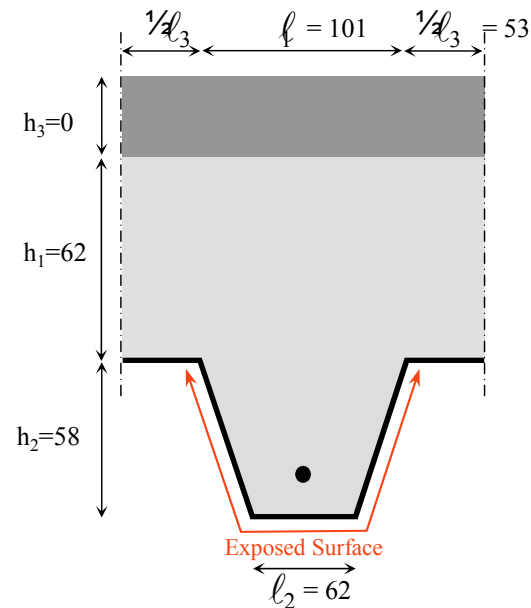
For Normal Weight Concrete

a_0 [min]	a_1 [min/mm]	a_2 [min]	a_3 [min/mm]	a_4 mm min	a_5 [min]
-28,8	1,55	-12,6	0,33	-735	48

Fire resistance according to thermal insulation

$$t_i = a_0 + a_1 \cdot h_1' + a_2 \cdot \Phi + a_3 \cdot \frac{A}{L_r} + a_4 \cdot \frac{1}{l_3} + a_5 \cdot \frac{A}{L_r} \cdot \frac{1}{l_3}$$

$$t_i = (-28,8) + 1,55 \cdot 62 + (-12,6) \cdot \Phi + 0,33 \cdot \frac{A}{L_r} + (-735) \cdot \frac{1}{106} + 48 \cdot \frac{A}{L_r} \cdot \frac{1}{106}$$

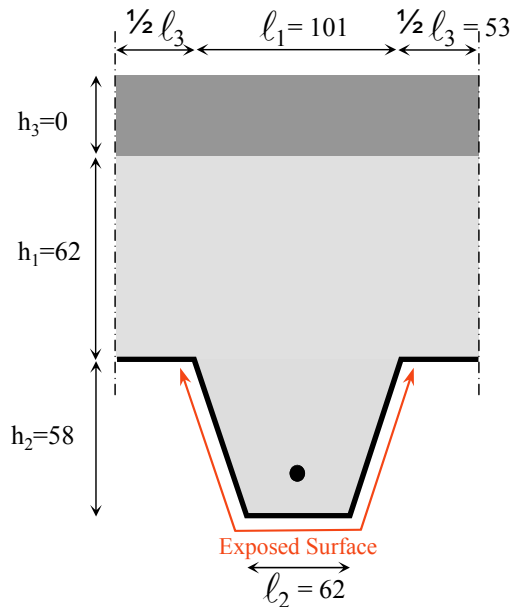


$$h_1' = h_1 + h_3 = 62 \text{ mm} \quad (h_3 = \text{thickness of the screed})$$

Fire resistance according to thermal insulation

$$t_i = a_0 + a_1 \cdot h_1' + a_2 \cdot \Phi + a_3 \cdot \frac{A}{L_r} + a_4 \cdot \frac{1}{l_3} + a_5 \cdot \frac{A}{L_r} \cdot \frac{1}{l_3}$$

$$t_i = (-28,8) + 1,55 \cdot 62 + (-12,6) \cdot \Phi + 0,33 \cdot 25,6 + (-735) \cdot \frac{1}{106} + 48 \cdot 25,6 \cdot \frac{1}{106}$$



Rib geometry factor

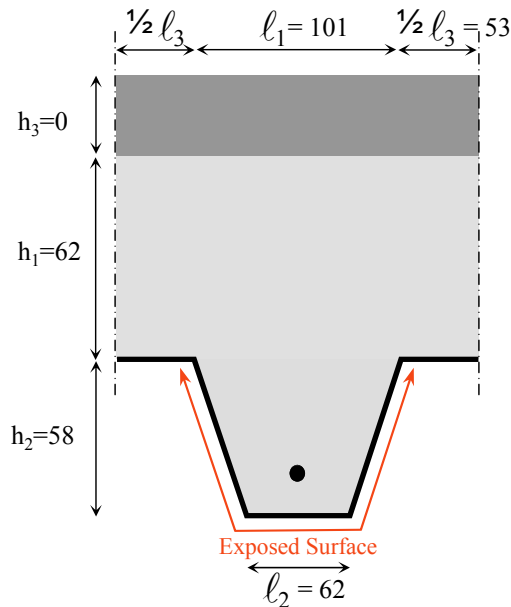
$$\frac{A}{L_r} = \frac{h_2 \cdot \left(\frac{l_1 + l_2}{2} \right)}{l_2 + 2 \cdot \sqrt{h_2^2 + \left(\frac{l_1 - l_2}{2} \right)^2}} = 25,6 \text{ mm}$$

Fire resistance according to thermal insulation

$$t_i = a_0 + a_1 \cdot h_1' + a_2 \cdot \Phi + a_3 \cdot \frac{A}{L_r} + a_4 \cdot \frac{1}{l_3} + a_5 \cdot \frac{A}{L_r} \cdot \frac{1}{l_3}$$

$$t_i = (-28,8) + 1,55 \cdot 62 + (-12,6) \cdot 0,727 + 0,33 \cdot 25,6 + (-735) \cdot \frac{1}{106} + 48 \cdot 25,6 \cdot \frac{1}{106}$$

$$t_i = 71\text{min}$$



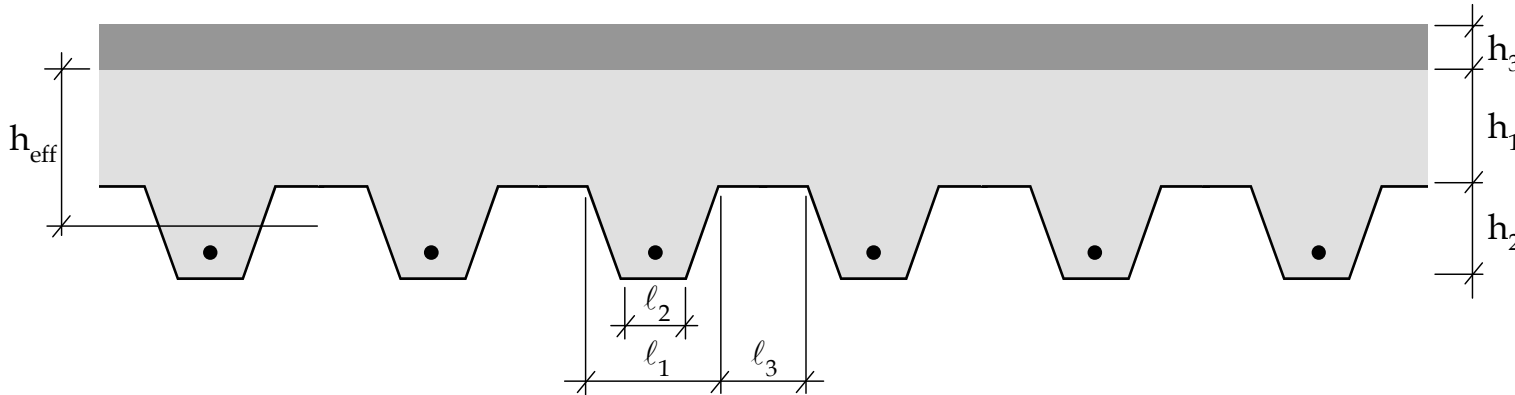
View factor

$$\Phi = \left[\sqrt{h_2^2 + \left(l_3 + \frac{l_1 - l_2}{2} \right)^2} - \sqrt{h_2^2 + \left(\frac{l_1 - l_2}{2} \right)^2} \right] / l_3 = 0,727$$

Simplified method (EN1994-1-2/Annex D/§D.4)

For $h_2/h_1 \leq 1,5$ and $h_1 > 40\text{mm}$

$$h_{\text{eff}} = h_1 + 0,5 \cdot h_2 \cdot \left(\frac{l_1 + l_2}{l_1 + l_3} \right) = 62 + 0,5 \cdot 58 \cdot \left(\frac{101 + 62}{101 + 106} \right) = 85 \text{ mm}$$



$$\begin{aligned} h_1 &= 62 \text{ mm} \\ h_2 &= 58 \text{ mm} \\ l_1 &= 101 \text{ mm} \\ l_2 &= 62 \text{ mm} \\ l_3 &= 106 \text{ mm} \end{aligned}$$

Minimal effective thickness of the slab h_{eff} to satisfy the thermal insulation criteria

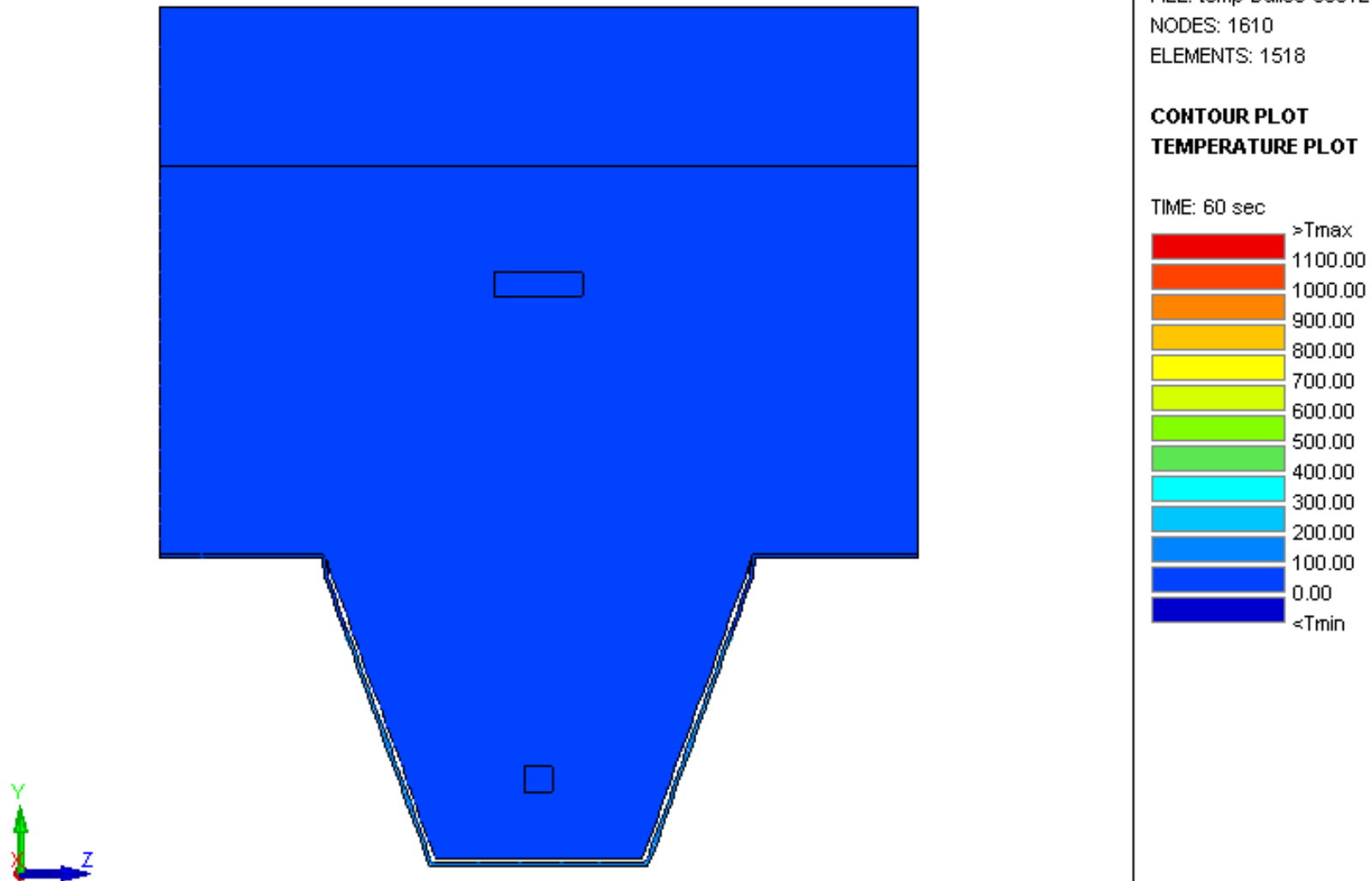
Standard fire resistance	h_{eff} [mm]
I 30	$60 - h_3$
I 60	$80 - h_3$
I 90	$100 - h_3$
I 120	$120 - h_3$
I 180	$150 - h_3$
I 240	$175 - h_3$

$$h_3 = 0 ; h_{\text{eff}} = 85 \text{ mm}$$

I 60

Verification of the composite slab

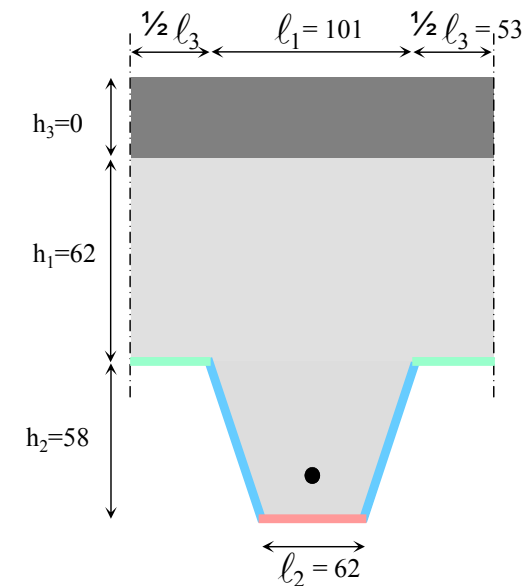
Temperature evolution in the section as a function of the time



Calculation of the sagging moment resistance $M_{fi,t,Rd}^+$

Temperature distribution in the steel decking : $\theta_a = b_0 + b_1 \cdot \frac{1}{l_3} + b_2 \cdot \frac{A}{L_r} + b_3 \cdot \Phi + b_4 \cdot \Phi^2$

Concrete	Fire resistance [min]	Part of the Steel decking	b_0 [°C]	b_1 [°C·mm]	b_2 [°C/mm]	b_3 [°C]	b_4 [°C]
Normal Concrete	60	Lower flange	951	-1197	-2.32	86.4	-150.7
		Web	661	-833	-2.96	537.7	-351.9
		Upper flange	340	-3269	-2.62	1148.4	-679.8
	90	Lower flange	1018	-839	-1.55	65.1	-108.1
		Web	816	-959	-2.21	464.9	-340.2
		Upper flange	618	-2786	-1.79	767.9	-472.0
	120	Lower flange	1063	-679	-1.13	46.7	-82.8
		Web	925	-949	-1.82	344.2	-267.4
		Upper flange	770	-2460	-1.67	592.6	-379.0



For the different parts of the steel decking, the temperatures at 60 minutes are :

Upper Flange $\theta_a = 951 - 1197 \cdot \frac{1}{106} - 2,32 \cdot 25,6 + 86,4 \cdot 0,727 - 150,7 \cdot 0,727^2 = 863 \text{ °C}$

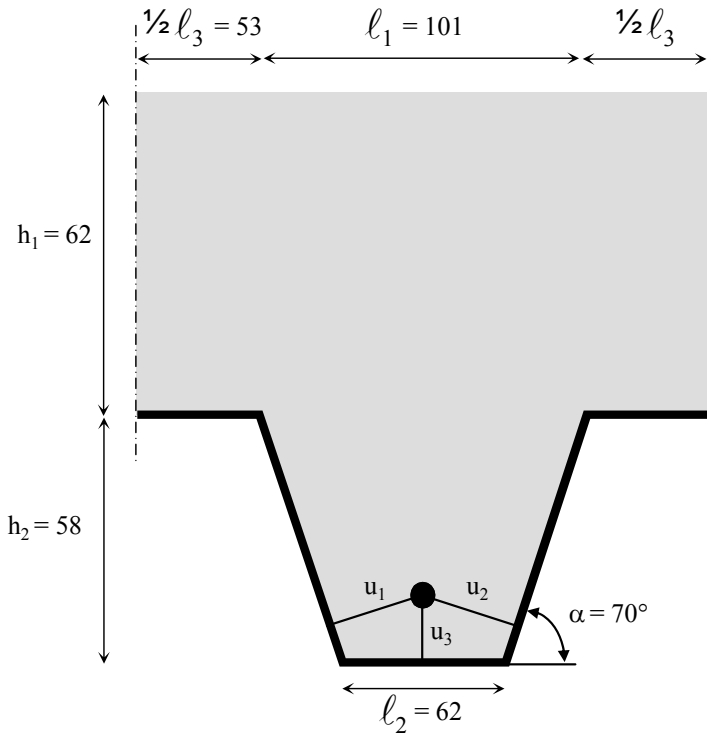
Web $\theta_a = 661 - 833 \cdot \frac{1}{106} - 2,96 \cdot 25,6 + 537,7 \cdot 0,727 - 351,9 \cdot 0,727^2 = 782 \text{ °C}$

Lower Flange $\theta_a = 340 - 3269 \cdot \frac{1}{106} - 2,62 \cdot 25,6 + 1148,4 \cdot 0,727 - 679,8 \cdot 0,727^2 = 718 \text{ °C}$

Verification of the composite slab



Temperature of the reinforcing bar in the rib :
$$\theta_s = c_0 + c_1 \cdot \frac{u_3}{h_2} + c_2 \cdot z + c_3 \cdot \frac{A}{L_r} + c_4 \cdot \alpha + c_5 \cdot \frac{1}{l_3}$$



with
$$\frac{1}{z} = \frac{1}{\sqrt{u_1}} + \frac{1}{\sqrt{u_2}} + \frac{1}{\sqrt{u_3}} = \frac{1}{\sqrt{35,8}} + \frac{1}{\sqrt{35,8}} + \frac{1}{\sqrt{20}}$$

$$\rightarrow z = 1,79 \text{ mm}^{0,5}$$

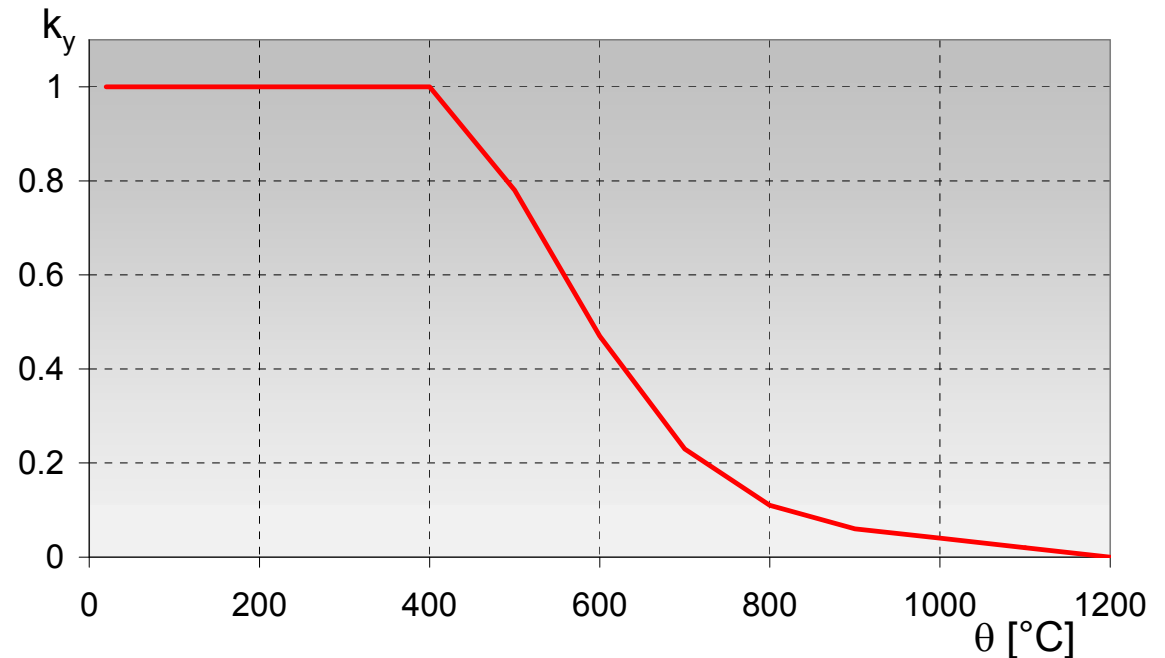
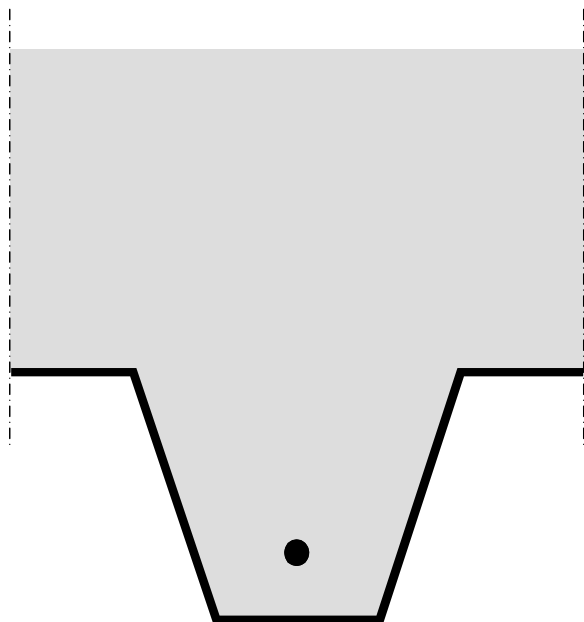
$u_1 = 35,8 \text{ mm}$
 $u_2 = 35,8 \text{ mm}$
 $u_3 = 20 \text{ mm}$
 (axis distances)

Concrete	Fire resistance [min]	c_0 [°C]	c_1 [°C]	c_2 [°C/mm ^{0.5}]	c_3 [°C/mm]	c_4 [°C/°]	c_5 [°C]
Normal Concrete	60	1191	-250	-240	-5.01	1.04	-925
	90	1342	-256	-235	-5.30	1.39	-1267
	120	1387	-238	-227	-4.79	1.68	-1326

$$\theta_s = 1191 - 250 \cdot \frac{20}{58} - 240 \cdot 1,79 - 5,01 \cdot 25,6 + 1,04 \cdot 71,4 - 925 \cdot \frac{1}{106} = 612 \text{ °C}$$

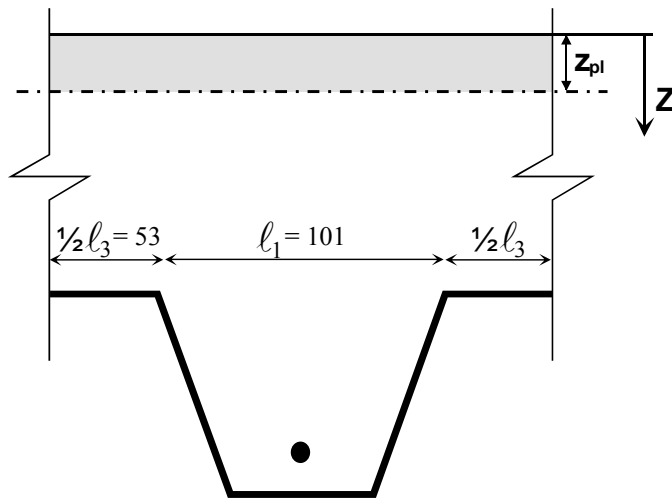
Bearing capacity of the different parts of the steel decking and the reinforcing bar :

	Temperature θ_i [°C]	Reduction factor $k_{y,i}$ [-]	Partial area A_i [cm ²]	$f_{y,i,\theta}$ [kN/cm ²]	F_i [kN]
Lower flange	863	0,078	0,465	2,74	1,274
Web	782	0,131	0,918	4,60	4,221
Upper flange	718	0,209	0,795	7,31	5,813
Rebar in the rib	612	0,367	0,503	18,34	9,22



Positive moment of the composite slab

Determination of the plastic neutral axis :



Equilibrium of the horizontal forces

$$\rightarrow \sum F_i = \alpha_{\text{slab}} \cdot (l_1 + l_3) \cdot z_{\text{pl}} \cdot f_c$$

$$z_{\text{pl}} = \frac{\sum F_i}{\alpha_{\text{slab}} \cdot (l_1 + l_3) \cdot f_c} = \frac{1,274 + 4,221 + 5,813 + 9,22}{0,85 \cdot (101 + 106) \cdot 25 \cdot 10^{-3}} = 4,7 \text{ mm}$$

Determination of the positive moment resistance of the composite slab :

	F_i [kN]	z_i [cm]	M_i [kNcm]
Lower flange	1,274	11,96	15,245
Web	4,221	9,10	38,410
Upper flange	5,813	6,16	35,820
Reinforcing bar in the rib	9,22	10,0	92,196
Concrete	-20,527	0,23	-4,79

for a rib width of 207mm,

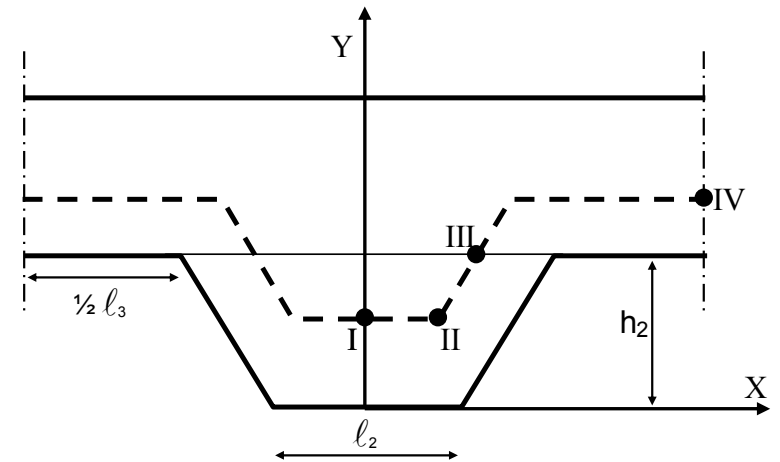
$$\sum M_i = 176,9 \text{ kNcm}$$

Than, for a slab width equal to 1m,

$$M_{\text{fi,Rd}}^+ = \frac{\sum M_i}{\text{rib width}} = \frac{1,769}{0,207} = 8,5 \text{ kNm/m}$$

Calculation of the hogging moment resistance $M_{fi,t,Rd}^-$

The hogging moment resistance of the slab is calculated by considering a reduced cross section established on the basis of the isotherm for the limit temperature θ_{lim} schematised by means of 4 characteristic points.

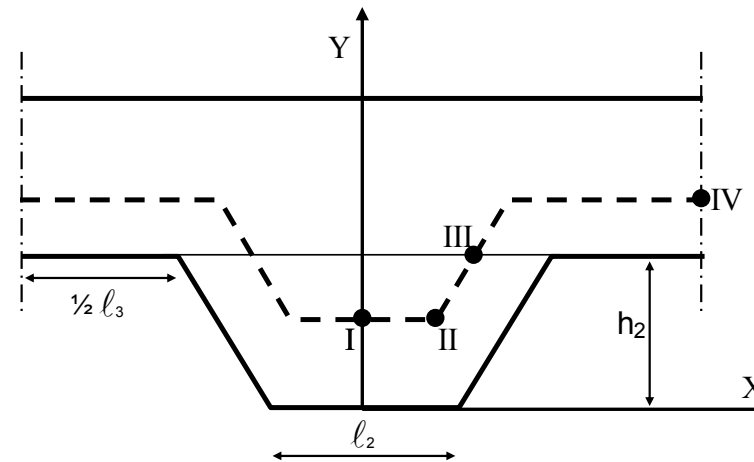


$$\theta_{lim} = d_0 + d_1 \cdot N_s + d_2 \cdot \frac{A}{L_r} + d_3 \cdot \Phi + d_4 \cdot \frac{1}{l_3} \quad (N_s = 26,6 \text{ kN is the normal force in the upper reinforcing bar})$$

	Fire resistance [min]	d_0 [° C]	d_1 [° C].N	d_2 [° C].mm	d_3 [° C]	d_4 [° C].mm
Normal weight concrete	60	867	$-1,9 \cdot 10^{-4}$	-8,75	-123	-1378
	90	1055	$-2,2 \cdot 10^{-4}$	-9,91	-154	-1990
	120	1144	$-2,2 \cdot 10^{-4}$	-9,71	-166	-2155

$$\theta_{lim} = 867 - 1,9 \cdot 10^{-4} \cdot 26600 - 8,75 \cdot 25,6 - 123 \cdot 0,727 - 1378 \cdot \frac{1}{106} = 535^\circ\text{C}$$

Determination of the points of the isotherm :



The parameter z of the formula D.9 is obtained from the equation for the determination of the temperature of the reinforcing bar, assuming that $u_3/h_2 = 0,75$ and $\theta_s = \theta_{lim}$

$$\theta_{lim} = c_0 + c_1 \cdot \frac{u_3}{h_2} + c_2 \cdot z + c_3 \cdot \frac{A}{L_r} + c_4 \cdot \alpha + c_5 \cdot \frac{1}{l_3}$$

$$\Rightarrow z = \frac{\theta_{lim} - c_0 - 0,75 \cdot c_1 - 25,6 \cdot c_3 - 71,4 \cdot c_4 - c_5 \cdot \frac{1}{106}}{c_2} = \frac{535 - 1191 + 0,75 \cdot 250 + 25,6 \cdot 5,01 - 71,4 \cdot 1,04 + 925 \cdot \frac{1}{106}}{(-240)} = 1,69 \text{ mm}^{0,5}$$

Coordinates of the points of the isotherm :

The coordinates of the 4 characteristic points are determined by the following formulae :

$$Y_I = Y_{II} = \frac{1}{\left(\frac{1}{z} - \frac{4}{\sqrt{l_1 + l_3}}\right)^2}$$

$$Y_{III} = h_2$$

$$Y_{IV} = h_2 + b$$

$$X_I = 0$$

$$X_{II} = \frac{1}{2} l_2 + \frac{Y_I}{\sin \alpha} \cdot (\cos \alpha - 1)$$

$$X_{III} = \frac{1}{2} l_1 - \frac{b}{\sin \alpha}$$

$$X_{IV} = \frac{1}{2} (l_1 + l_3)$$

Points	Coordinates [mm]	
	X	Y
I	0,0	10,1
II	23,7	10,1
III	42,1	58,0
IV	103,5	66,0

with

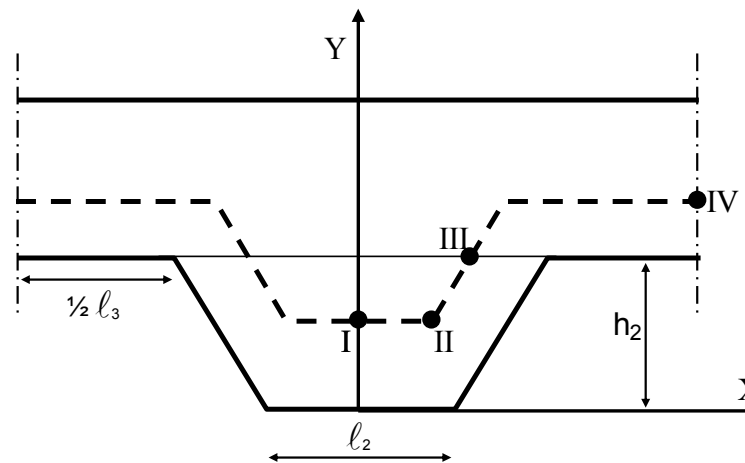
$$b = \frac{1}{2} l_1 \sin \alpha \left(1 - \frac{\sqrt{a^2 - 4a + c}}{a} \right)$$

$$a = \left(\frac{1}{z} - \frac{1}{\sqrt{h_2}} \right)^2 l_1 \sin \alpha$$

$$\alpha = \arctan \left(\frac{2 h_2}{l_1 - l_2} \right)$$

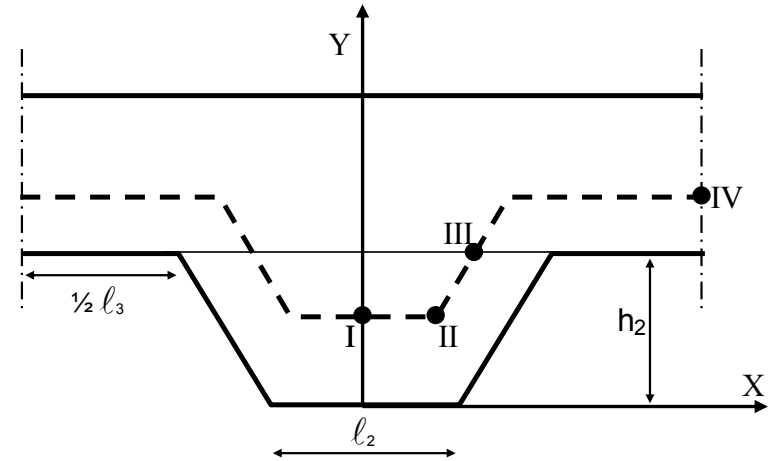
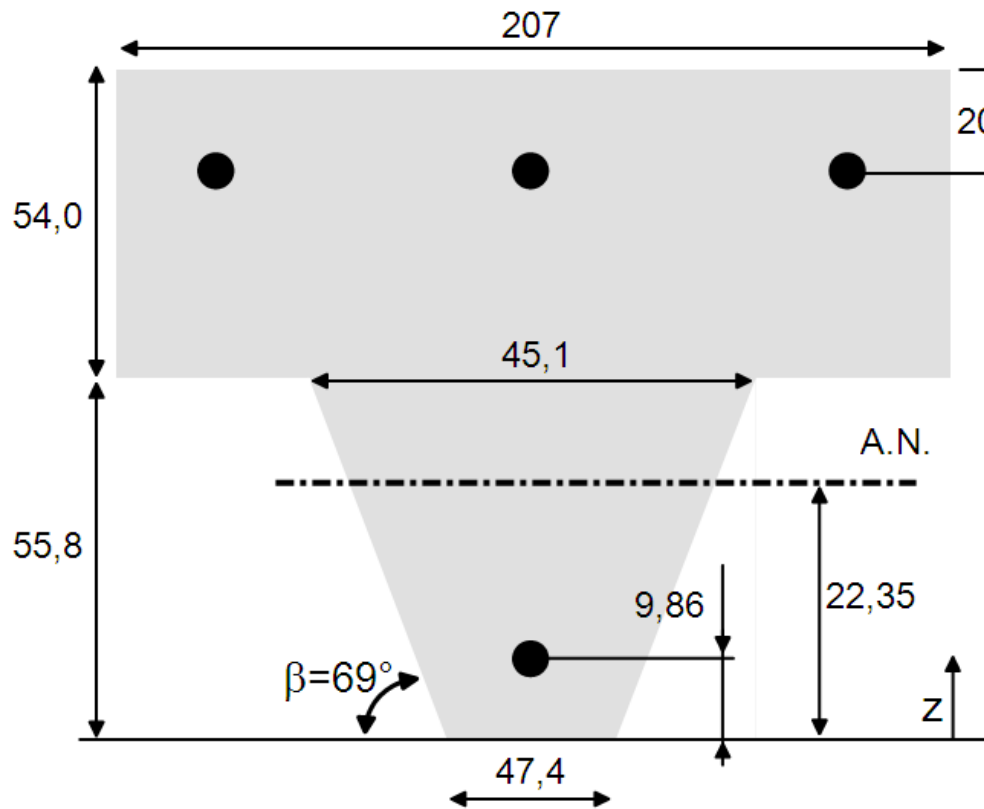
$$c = -8 \left(1 + \sqrt{1+a} \right) \text{ si } a \geq 8$$

$$c = +8 \left(1 + \sqrt{1+a} \right) \text{ si } a < 8$$



Verification of the composite slab

Determination of the plastic neutral axis :



	Temperature θ_i [°C]	Reduction factor $k_{y,i}$ [-]	Partial area A_i [cm ²]	$f_{y,i,\theta}$ [kN/cm ²]	F_i [kN]
Mesh ST25	$\theta < \theta_{lim}$	1,0	0,532	50	26,60

The horizontal equilibrium gives :

$$\sum F_i = \left(\frac{1}{\text{tg}\beta} \cdot z_{pl}^2 + 47,4 \cdot z_{pl} \right) \cdot 0,85 \cdot f_c$$

$$\Rightarrow z_{pl} = 22,35\text{mm}$$

Moment resistance of each part of the rib :

	F_i [kN]	z_i [cm]	M_i [kNcm]
Mesh ST25	26,60	8,9	239,01
Concrete rib	-26,60	4,5	-120,32

The negative moment resistance of the composite slab, for a rib width of 207mm is given by :

$$\sum M_i = 118,7 \text{ kNcm}$$

Than, for a slab width equal to 1m,

$$M_{fi,Rd}^- = \frac{\sum M_i}{\text{rib width}} = \frac{1,187}{0,207} = 5,734 \text{ kNm / m}$$

Bearing capacity of the continuous slab

The applied load is :

$$E_{fi,d} = G_k + \psi_{1,1} Q_{k,1} \quad \longrightarrow \quad p_{fi,d} = 1,0 * (0,085 + 2,03 + 1,5) + 0,6 * 4 = 6,02 \text{ kN/m}^2$$

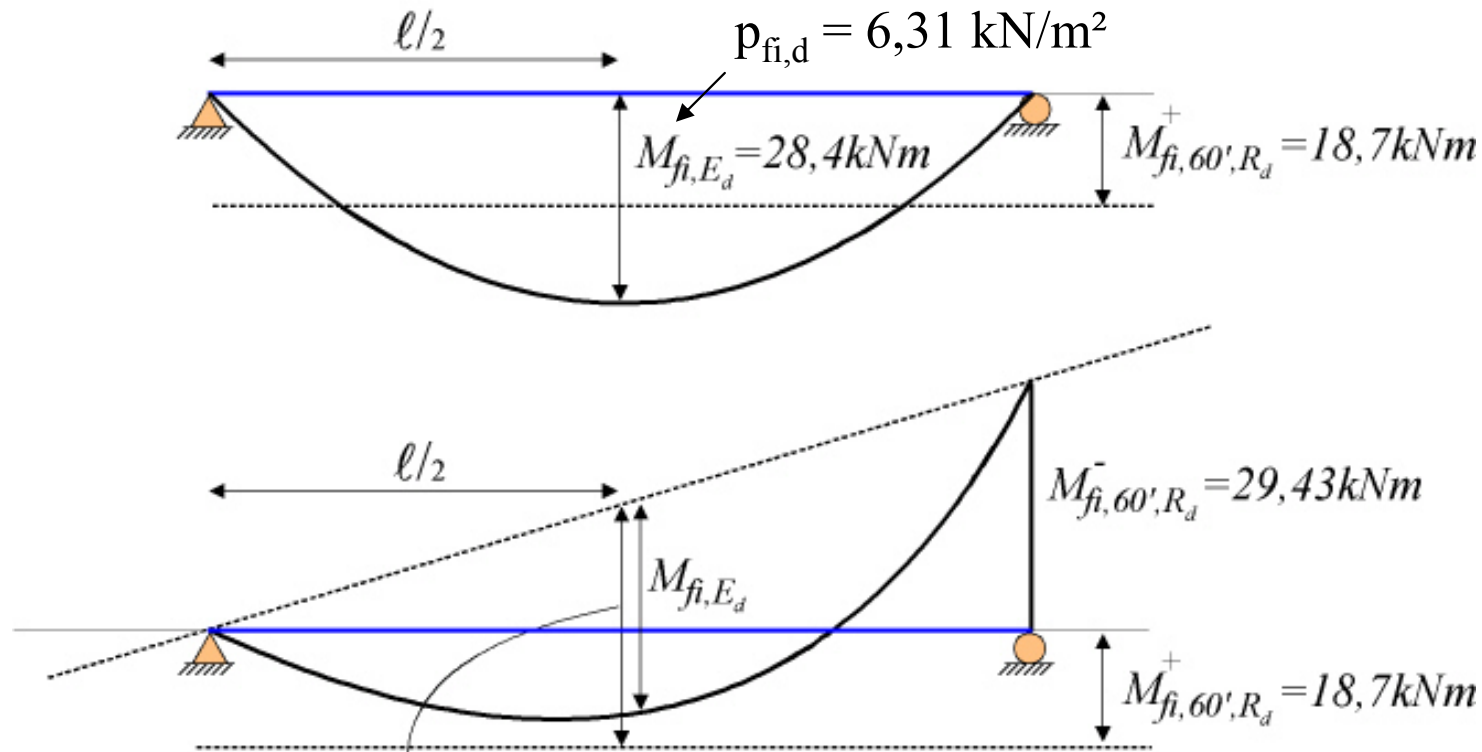
For a slab width equal to 1m, the bearing capacity may be deduced from the sagging and hogging moment by the following relation :

$$p_{fi,Rd} = \frac{2M_{fi,Rd}^- + 4M_{fi,Rd}^+}{\ell^2} + \frac{2}{\ell^2} \cdot \sqrt{(M_{fi,Rd}^- + 2M_{fi,Rd}^+)^2 - M_{fi,Rd}^-^2}$$
$$p_{fi,Rd} = \frac{2 \cdot 5,734 + 4 \cdot 8,5}{3^2} + \frac{2}{3^2} \cdot \sqrt{(5,734 + 2 \cdot 8,5)^2 - 5,734^2}$$
$$p_{fi,Rd} = 9,98 \text{ kN/m}^2 \quad > \quad p_{fi,d} = 6,02 \text{ kN/m}^2$$

The continuous slab has a fire resistance of 60 minutes

Verification of the composite slab

Bearing capacity of the continuous slab : Simplified formula

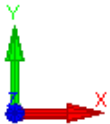
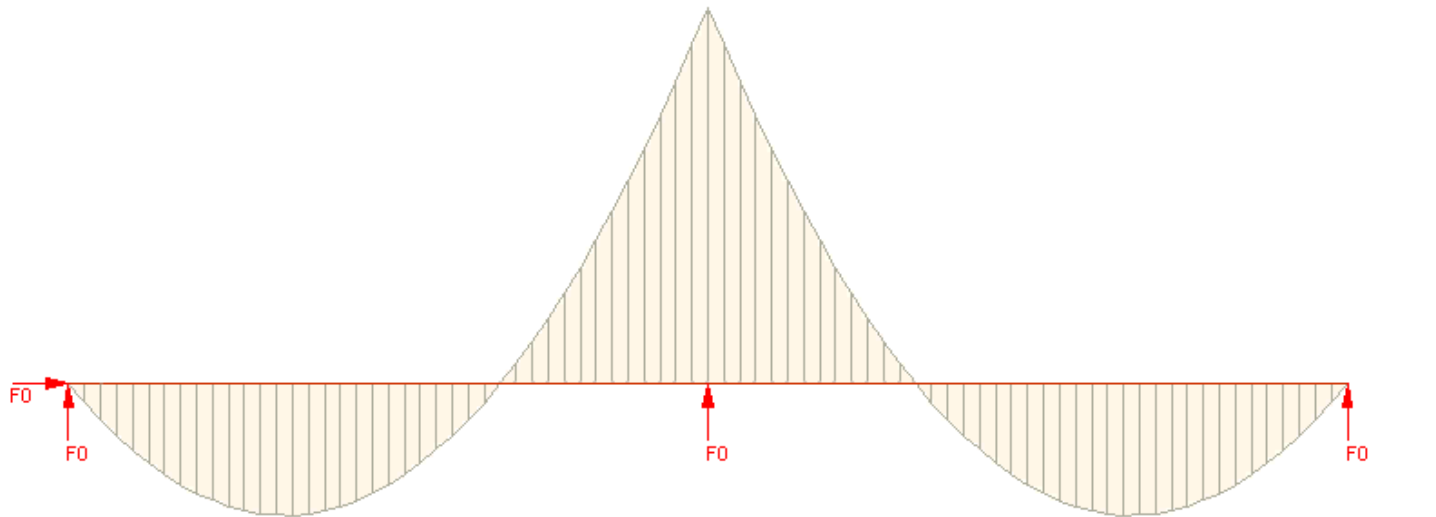


$$\frac{M_{fi,60',R_d}^-}{2} + M_{fi,60',R_d}^+ \geq M_{fi,E_d}$$

$$33,4 \text{ kNm} \geq 28,4 \text{ kNm}$$

$$p_{fi,Rd} = 7,33 \text{ kN/m}^2 \geq p_{fi,d} = 6,31 \text{ kN/m}^2$$

Evolution du moment fléchissant en fonction du temps



Diamond 2004 for SAFIR

FILE: displ-Poutre_01-30cvLR

NODES: 81

BEAMS: 40

TRUSSES: 0

SHELLS: 0

SOILS: 0

BEAMS PLOT

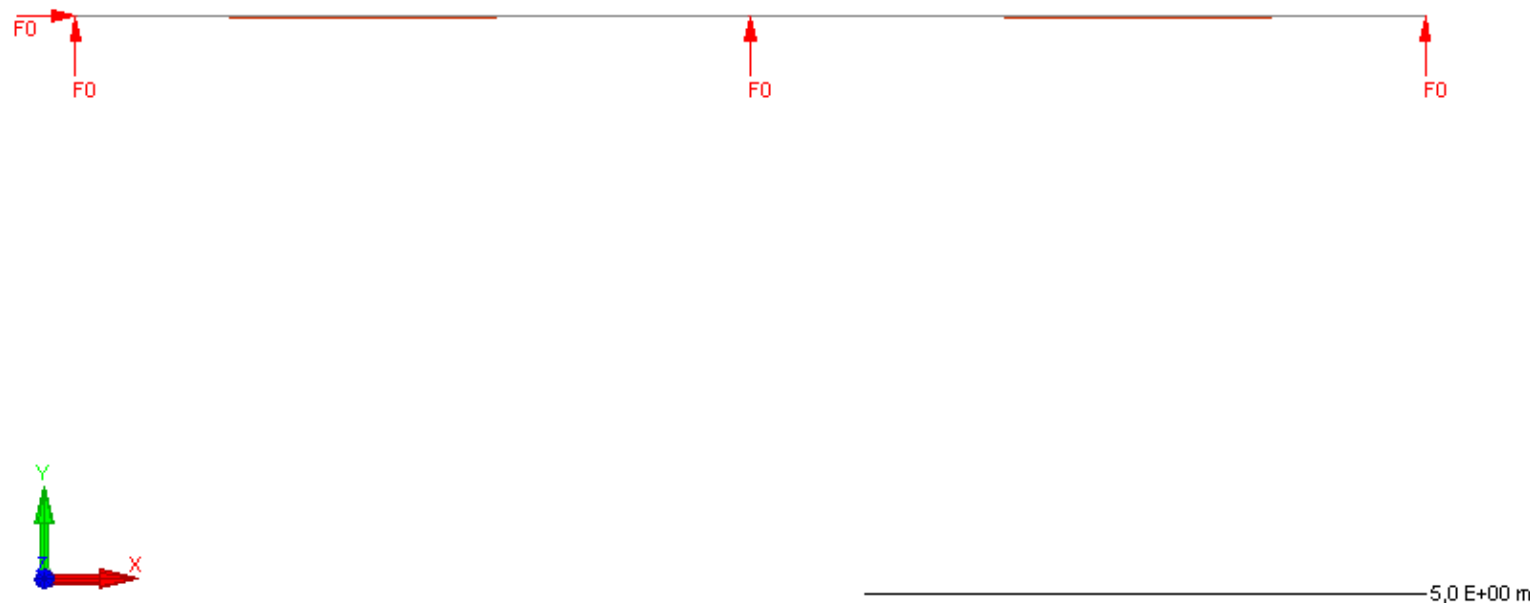
IMPOSED DOF PLOT

BENDING MOMENT PLOT

TIME: 20,97152 sec

5,0 E+03 Nm

Evolution de la déformée en fonction du temps



Diamond 2004 for SAFIR

FILE: displ-Poutre_01-30cvLR

NODES: 81

BEAMS: 40

TRUSSES: 0

SHELLS: 0

SOILS: 0

BEAMS PLOT

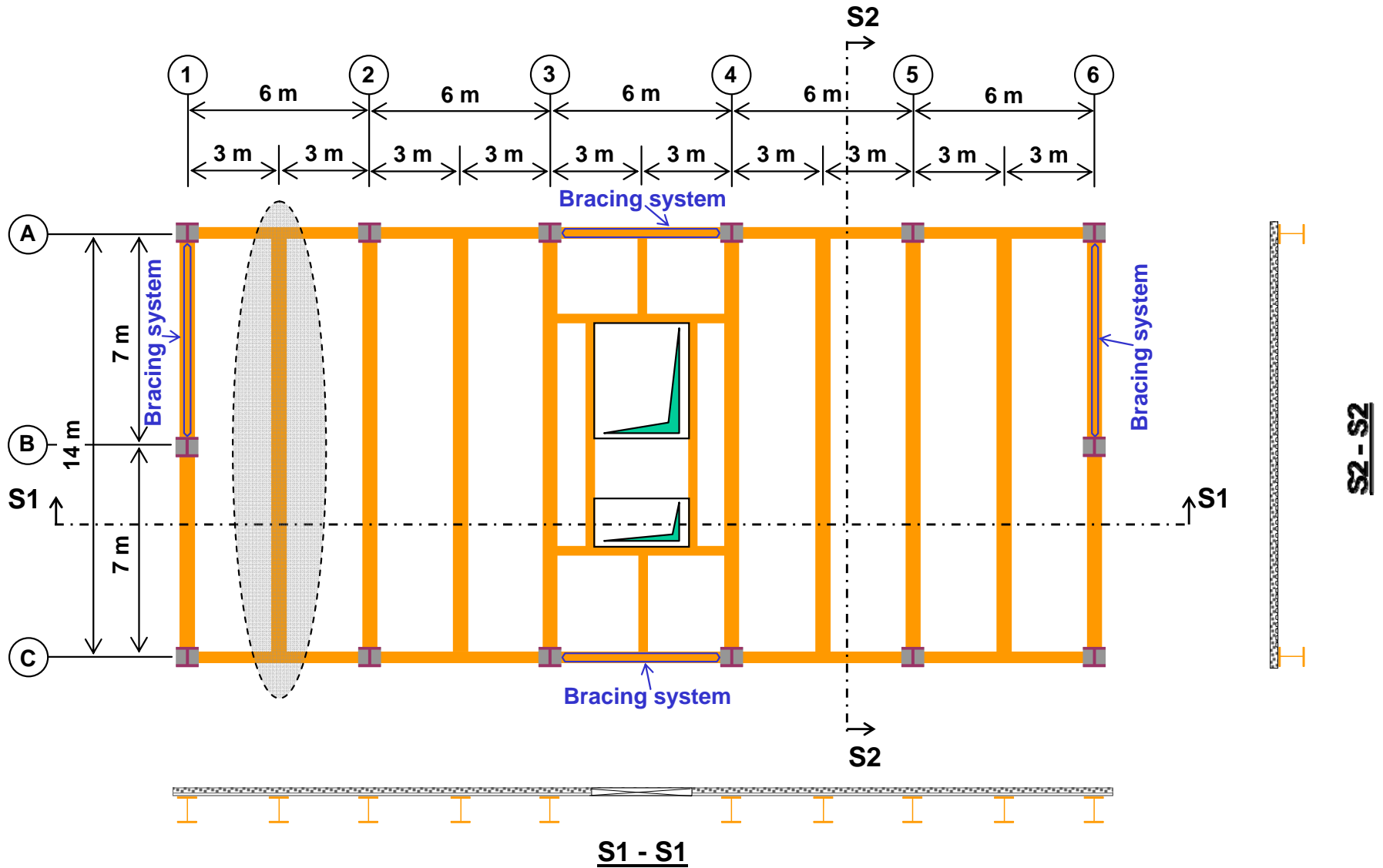
IMPOSED DOF PLOT

DISPLACEMENT PLOT (x 1)

TIME: 20,97152 sec

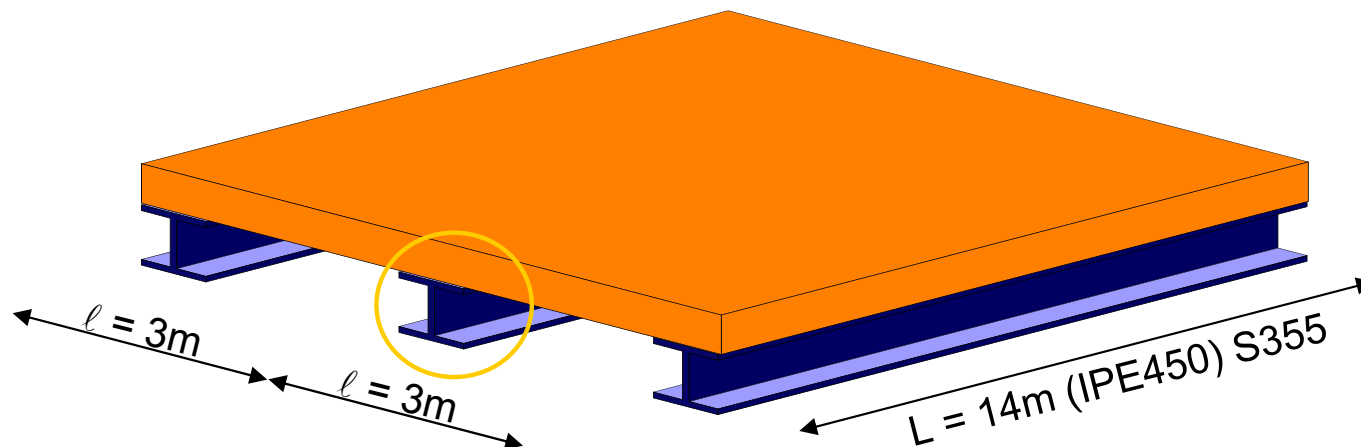
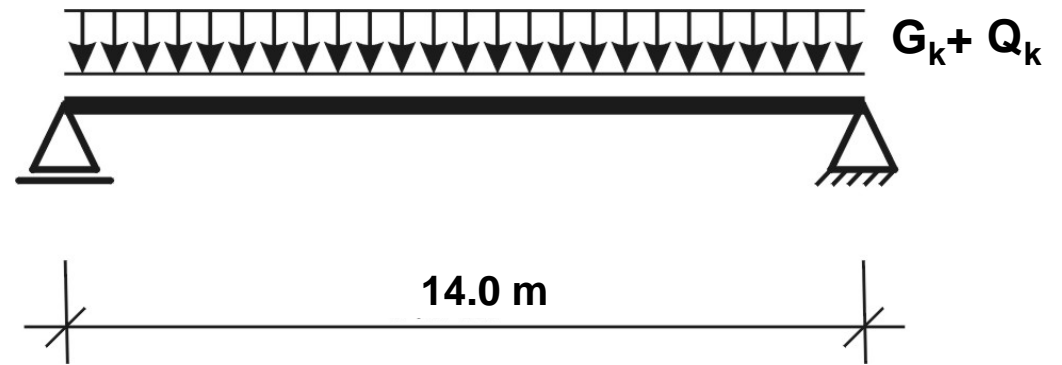
 Beam Element

Secondary composite beams



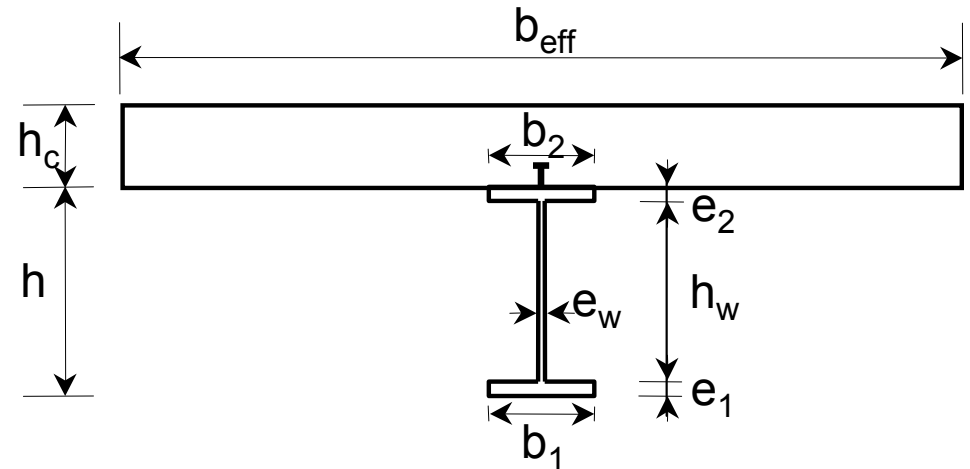
Data

- ⇒ Composite beam on 2 supports
- ⇒ Continuous slab on 3 supports
- ⇒ Beam span = 14m
- ⇒ Distance between beams = 3m
- ⇒ Required fire resistance R60



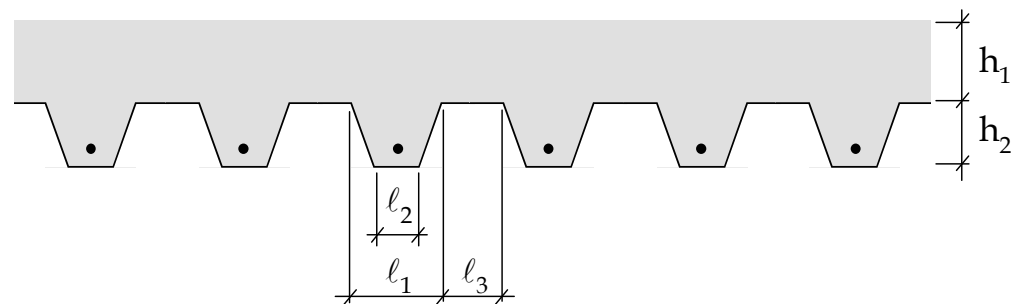
Geometrical characteristics and material properties

Beam : IPE450
 $h = 450 \text{ mm}$
 $b = b_1 = b_2 = 190 \text{ mm}$
 $e_w = 9,4 \text{ mm}$
 $e_f = e_1 = e_2 = 14,6 \text{ mm}$
 $f_y = 355 \text{ N/mm}^2$



Steel decking : $f_y = 350 \text{ N/mm}^2$

Concrete : $h_c = 120 \text{ mm}$
 $b_{\text{eff}} = 3000 \text{ mm}$
 C25/30
 $f_c = 25 \text{ N/mm}^2$

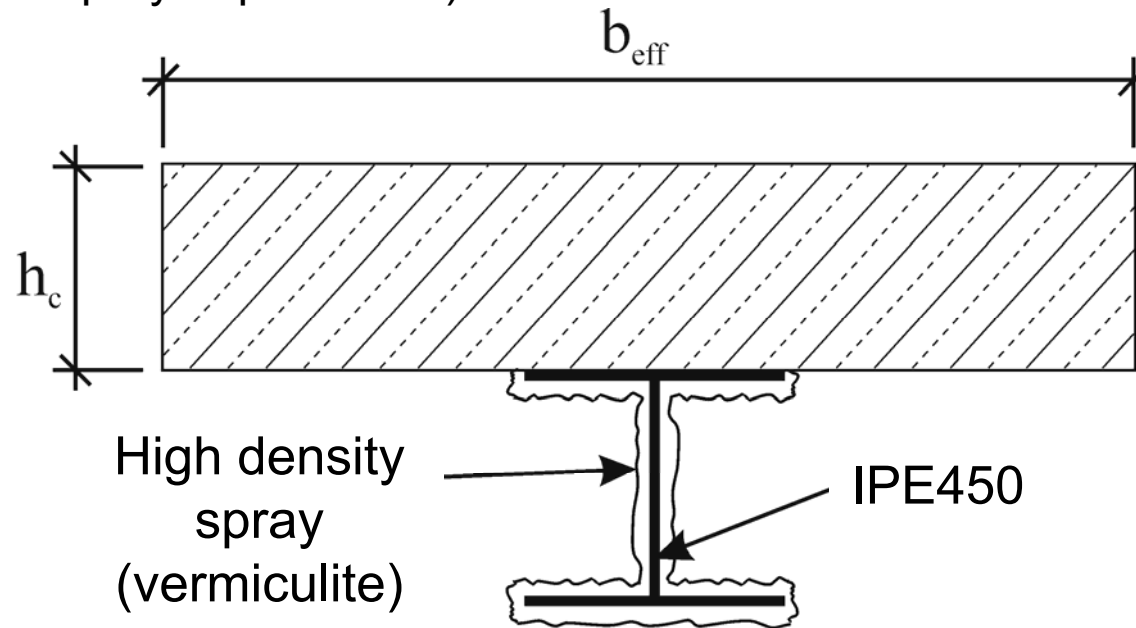


Connectors : $f_u = 450 \text{ N/mm}^2$
 Number = 136
 Diameter = 19 mm

$h_1 = 62 \text{ mm}$ $h_2 = 58 \text{ mm}$
 $l_1 = 101 \text{ mm}$ $l_2 = 62 \text{ mm}$ $l_3 = 106 \text{ mm}$

Geometrical characteristics and material properties

Fire protection (use of sprayed protection)



Fire protection material characteristics :

Thickness : $d_p = 15$ mm

Thermal conductivity : $\lambda_p = 0,12$ W/(m·K)

Specific heat : $c_p = 1100$ J/(kg·K)

Density: $\rho_p = 550$ kg/m³

Loads

Permanents loads:

Steel decking :	$g_{t,k} = 0,085 \text{ kN/m}^2$
Concrete :	$g_{b,k} = 2,03 \text{ kN/m}^2$
Permanent load :	$g_{c,k} = 1,5 \text{ kN/m}^2$
Self weight of the profile :	$G_{a,k} = 0,776 \text{ kN/ml}$

Variable load:

Variable load :	$q_k = 4,0 \text{ kN/m}^2$
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Determination of the load level in fire situation

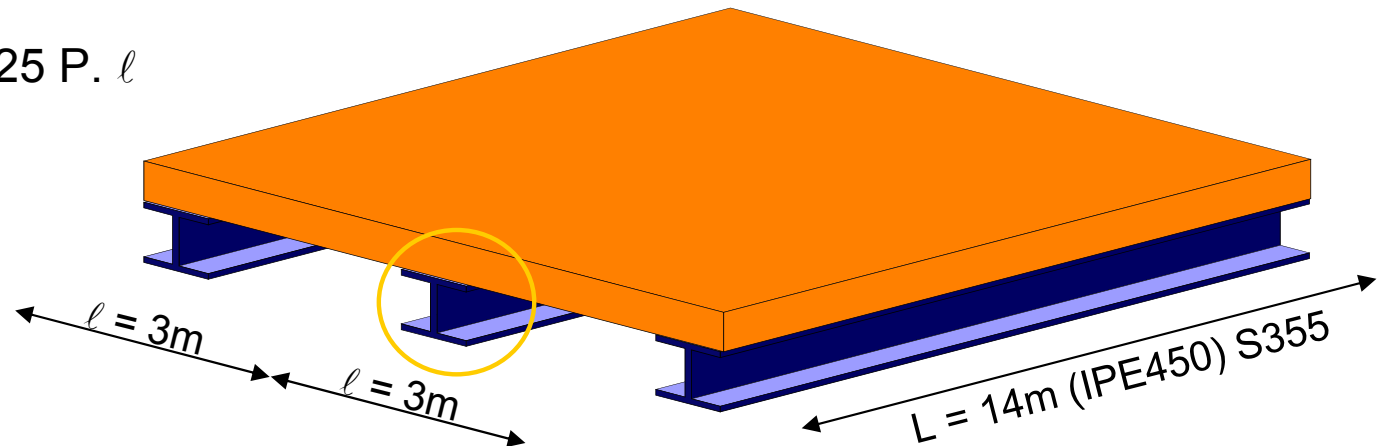
$$\eta_{fi,t} = \frac{E_{fi,d,t}}{R_d} = \frac{M_{fi,Ed}}{M_{Rd}}$$

Combination of the mechanical actions:

$$E_d = E \left\{ \sum_{j \geq 1} G_{k,j} + P + A_d + (\psi_{1,1} \text{ ou } \psi_{2,1}) Q_{k,1} + \sum_{i > 1} \psi_{2,i} Q_{k,i} \right\}$$

System considered:

Central support : reaction = 1,25 P . l



$$F_{fi,d} = 1,25 \cdot [(g_{k,1} + \psi_{2,1} \cdot q_{k,1}) \cdot l] + G_{a,k} = 1,25 \cdot [(3,62 + 0,6 \cdot 4) \cdot 3] + 0,776 = 23,332 \text{ kN/m}$$

Calculated moment:

$$\left. \begin{aligned} M_{fi,Ed} &= \frac{F_{fi,d} \cdot L^2}{8} = \frac{23,332 \cdot 14^2}{8} = 571,6 \text{ kNm} \\ M_{Rd} &= 1065,3 \text{ kNm (see Calculation Note)} \end{aligned} \right\} \longrightarrow \eta_{fi,t} = \frac{571,6}{1065,3} = 0,537$$

Critical temperature method

Determination of the critical T°

For R60 $\longrightarrow \eta_{fi,t} = f_{ay,\theta_{cr}} / f_{ay}$

$\longrightarrow \frac{f_{ay,\theta_{cr}}}{f_{ay}} = 0,537$

$\longrightarrow \theta_{cr} = 578^\circ\text{C}$

Resistance

% of the nominal value

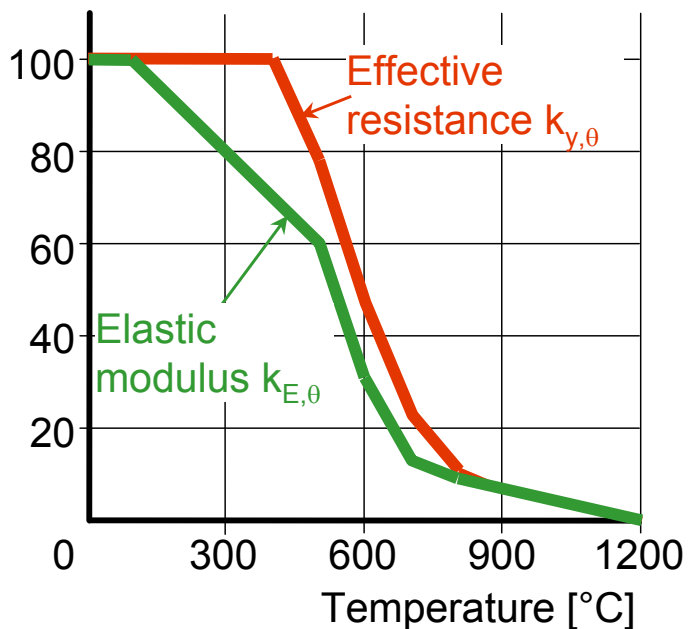


Table 3.2: Reduction factors k_θ for stress-strain relationships of structural steel at elevated temperatures.

Steel Temperature $\theta_a [^\circ\text{C}]$	$k_{E,\theta}$	$k_{p,\theta}$	$k_{y,\theta}$	$k_{u,\theta}$
20	1,00	1,00	1,00	1,25
100	1,00	1,00	1,00	1,25
200	0,90	0,807	1,00	1,25
300	0,80	0,613	1,00	1,25
400	0,70	0,420	1,00	
500	0,60	0,360	0,78	
600	0,31	0,180	0,47	
700	0,13	0,075	0,23	
800	0,09	0,050	0,11	
900	0,0675	0,0375	0,06	
1000	0,0450	0,0250	0,04	
1100	0,0225	0,0125	0,02	
1200	0	0	0	

Temperature calculation in the protected steel cross section

The increase of temperature of the various parts of the protected steel beam during the time interval may be determined by the following equation :

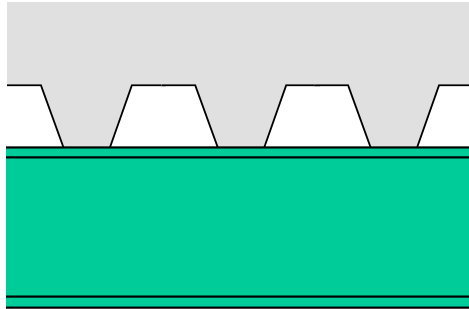
$$\Delta\theta_{a,t} = \left[\left(\frac{\lambda_p/d_p}{c_a\rho_a} \right) \left(\frac{A_{p,i}}{V_i} \right) \left(\frac{1}{1+w/3} \right) (\theta_t - \theta_{a,t}) \Delta t \right] - \left[(e^{w/10} - 1) \Delta\theta_t \right]$$

with :

- C_a specific heat of the steel ; varying according to the steel temperature [J/(kg.K)] (§3.3.1(4))
- ρ_a density of the steel [kg/m³] (§ 3.4(1))
- λ_p thermal conductivity of the fire protection material [W/m^oK]
- d_p thickness of the fire protection material [m]
- $A_{p,i}$ is the area of the inner surface of the fire protection material per unit length of the part i of the steel member [m²/m]
- V_i volume of the part i of the steel cross section per unit length [m³/m]
- $A_{p,i} / V_i$ section factor of the part i of the insulated steel cross-section [m⁻¹]
- Δt time interval (less than 5sec) [s]

$$w = \left(\frac{c_p\rho_p}{c_a\rho_a} \right) d_p \left(\frac{A_{p,i}}{V_i} \right) \quad \text{where} \quad \begin{array}{ll} c_p & \text{specific heat of the fire protection material [J/kg}^\circ\text{K]} \\ \rho_p & \text{density of the fire protection material [kg/m}^3\text{]} \end{array}$$

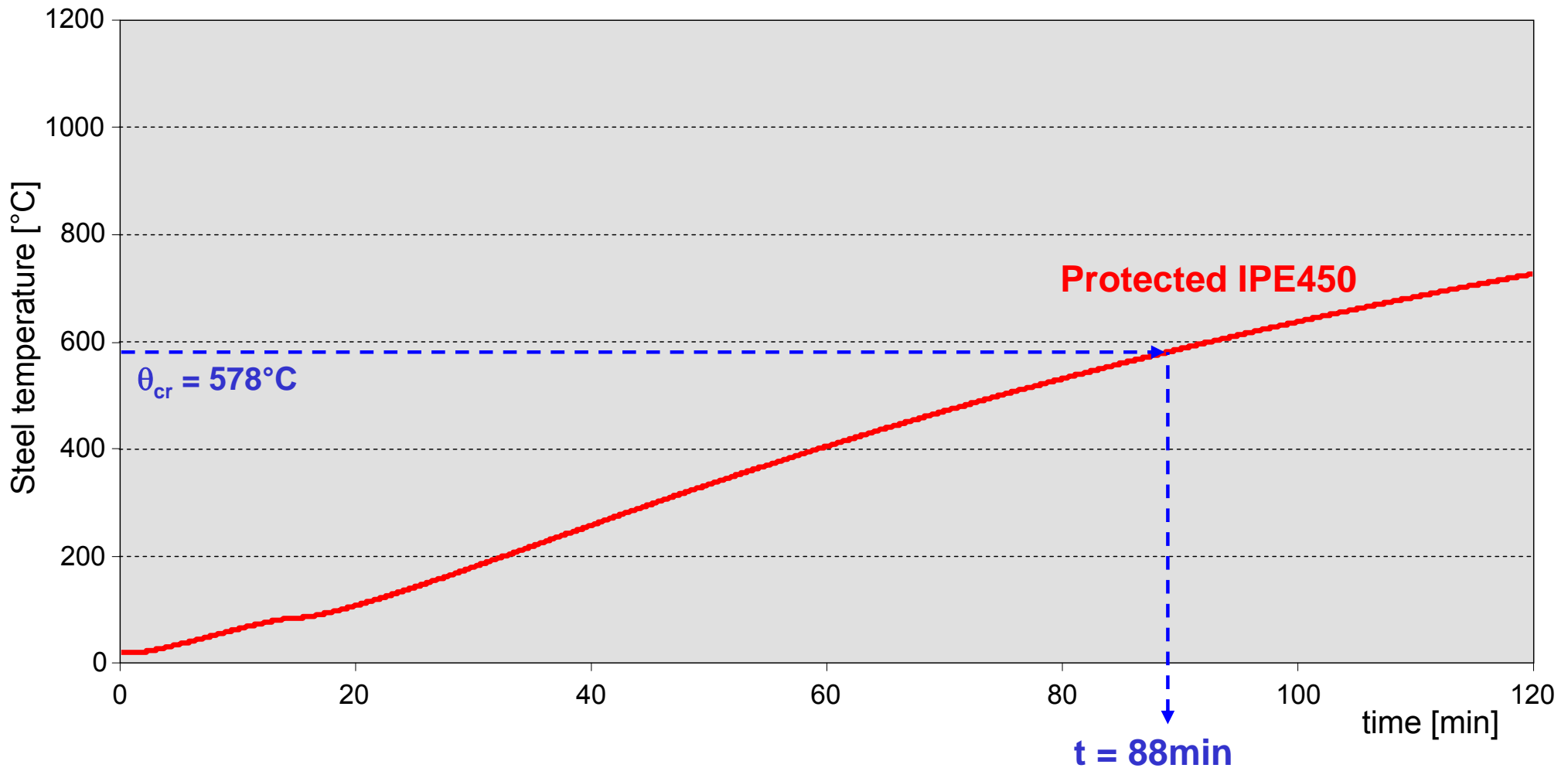
Temperature calculation in the protected steel cross section



T° lower flange \cong T° upper flange

	A_m/V [m ⁻¹]	Steel temperature after 60' [°C]
Upper flange	147,5	480
Web	212,8	588
Lower flange	147,5	480

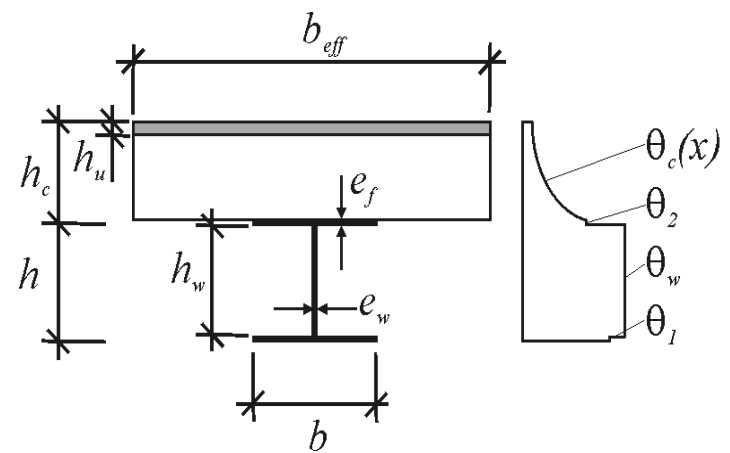
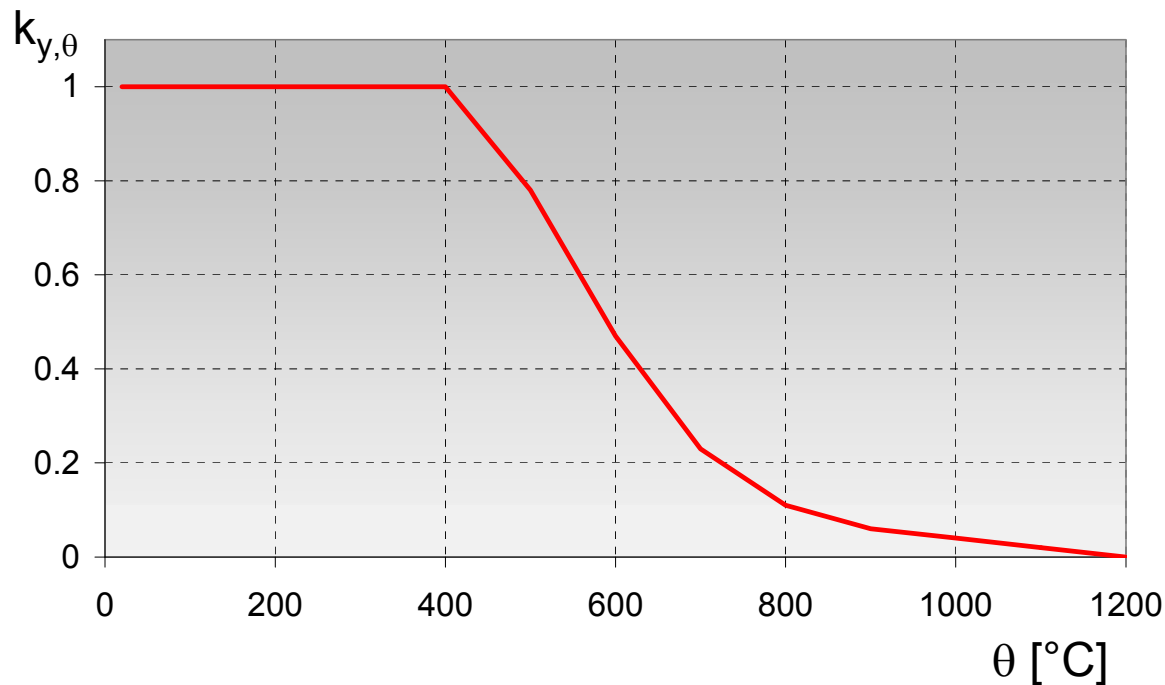
Determination of the failure time



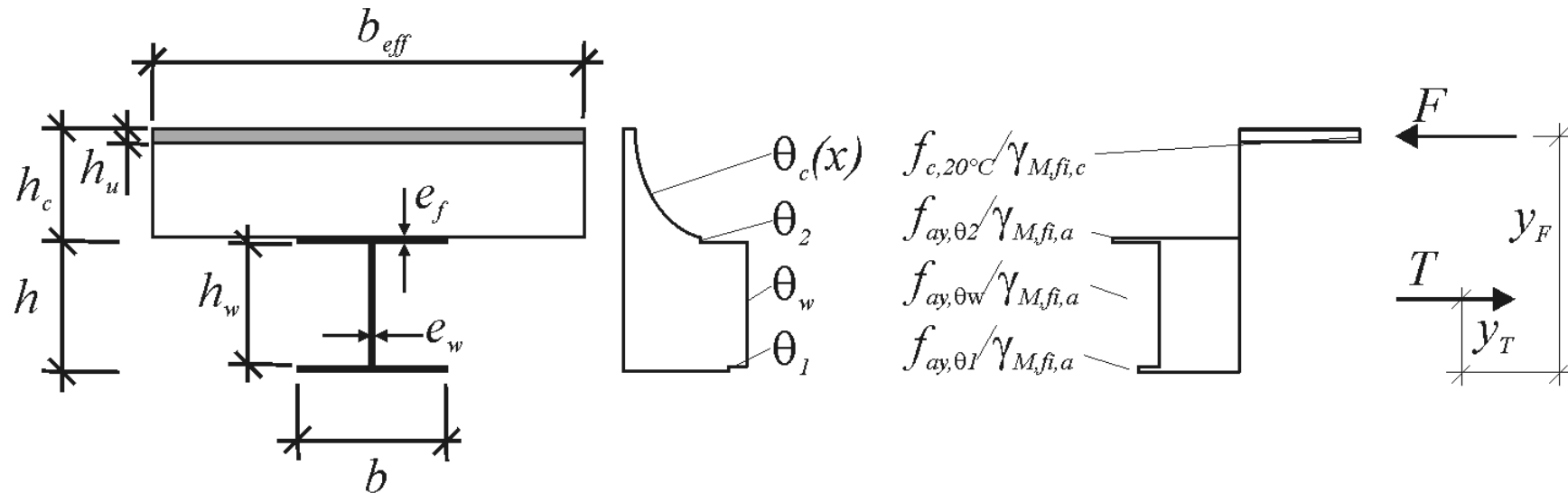
Verification of the composite beam

Verification of the resistance by the moment resistance method

	$\theta_{a,max,30}$ [°C]	$k_{y,\theta}$ [-]	$f_{ay,\theta}$ [N/mm ²]
Upper flange	480	0,824	292,5
Web	588	0,507	179,9
Lower flange	480	0,824	292,5



Determination of the tensile force in the profile



The steel profile is subjected to a tensile force T which could be calculated by the following way

$$T = \frac{f_{ay,\theta_1} \cdot b \cdot e_f + f_{ay,\theta_w} \cdot h_w \cdot e_w + f_{ay,\theta_2} \cdot b \cdot e_f}{\gamma_{M,fi,a}} = 2334,096 \text{ kN}$$

The location of the tensile force (with regard to the bottom flange) is given by the following equation :

$$y_T = \frac{f_{ay,\theta_1} \cdot \left(\frac{b \cdot e_f^2}{2} \right) + f_{ay,\theta_w} (h_w \cdot e_w) \left(e_f + \frac{h_w}{2} \right) + f_{ay,\theta_2} (b \cdot e_f) \left(h - \frac{e_f}{2} \right)}{T \cdot \gamma_{M,fi,a}} = 222,6 \text{ mm}$$

Limitation of the tensile force

→ $T \leq N \cdot P_{fi,Rd}$ with N is the number of connectors in the critical length of the beam
 $P_{fi,Rd}$ is the design shear resistance of one connector in fire situation

$$P_{fi,Rd} = \min \begin{cases} P_{fi,Rd,1} = 0,8 \cdot k_{u,\theta} \cdot P'_{Rd,1} \\ P_{fi,Rd,2} = k_{c,\theta} \cdot P'_{Rd,2} \end{cases}$$

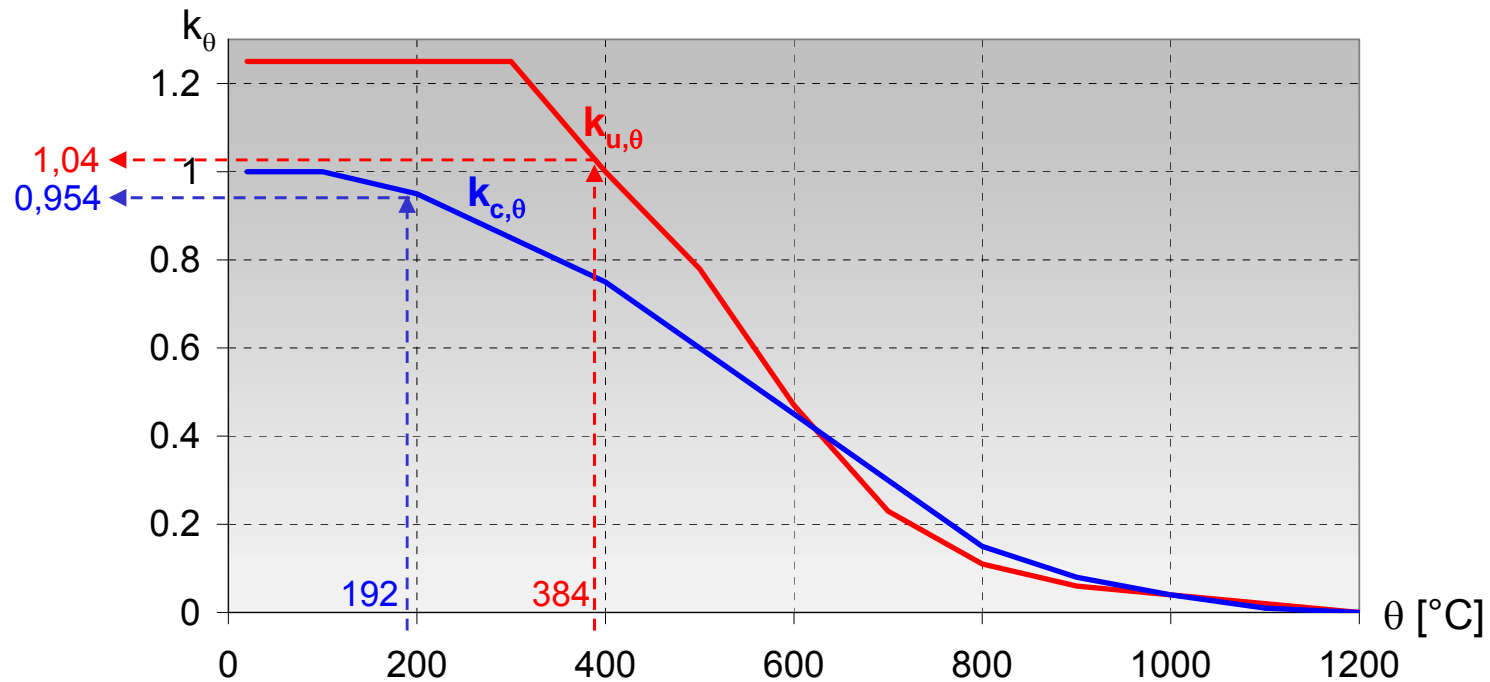
where $P'_{Rd,1} = 0,8 \cdot \frac{f_u}{Y_{M,fi,v}} \cdot \frac{\pi \cdot d^2}{4} = 0,8 \cdot \frac{450}{1,0} \cdot \frac{\pi \cdot 19^2}{4} = 102 \text{ kN}$

and $P'_{Rd,2} = 0,29 \cdot \alpha \cdot d^2 \cdot \frac{\sqrt{f_c \cdot E_{cm}}}{Y_{M,fi,v}} = 0,29 \cdot 1,0 \cdot 19^2 \cdot \frac{\sqrt{25 \cdot 30500}}{1,0} = 91 \text{ kN}$

Determination of the reduction factors

$$\theta_v \text{ (connectors)} = 80\% \theta_{\text{semelle}} = 0,8 \times 480 = 384^\circ\text{C} \Rightarrow k_{u,\theta} = 1,04$$

$$\theta_c \text{ (concrete)} = 40\% \theta_{\text{semelle}} = 0,4 \times 480 = 192^\circ\text{C} \Rightarrow k_{c,\theta} = 0,954$$



$$\Rightarrow P_{fi,Rd} = \min \begin{cases} P_{fi,Rd,1} = 0,8 \cdot k_{u,\theta} \cdot P'_{Rd,1} = 0,8 \cdot 1,04 \cdot 102 = 84,9 \text{ kN} \\ P_{fi,Rd,2} = k_{c,\theta} \cdot P'_{Rd,2} = 0,954 \cdot 91 = 87,21 \text{ kN} \end{cases}$$

Limit of the tensile force is fulfilled :

$$T \leq N \cdot P_{fi,Rd} \quad \Rightarrow \quad 2334,096 \text{ kN} < 68 \cdot 84,9 = 5774 \text{ kN} \quad \Rightarrow \quad \text{OK}$$

Determination of the compressive zone of the slab

Determination of the effective thickness of the slab

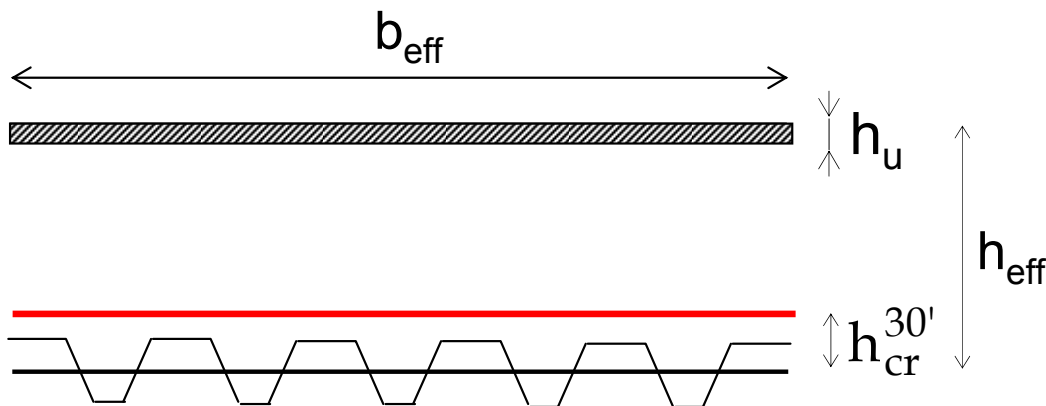
$$h_{\text{eff}} = 84,8 \text{ cm}$$

Determination of the critical height

$$h_{\text{cr}}^{60'} = 50 \text{ mm}$$

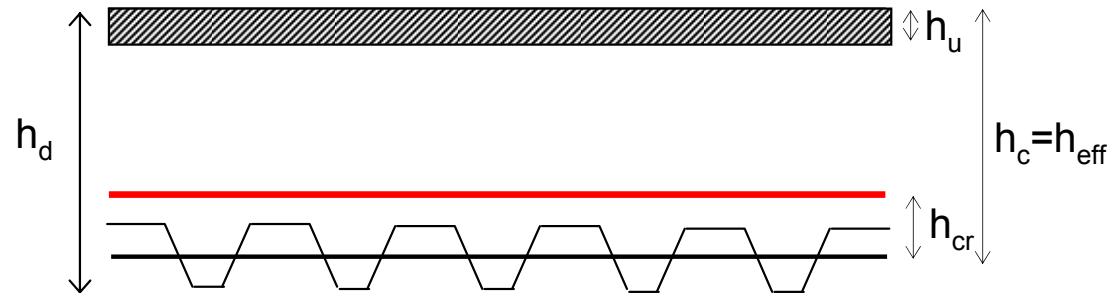
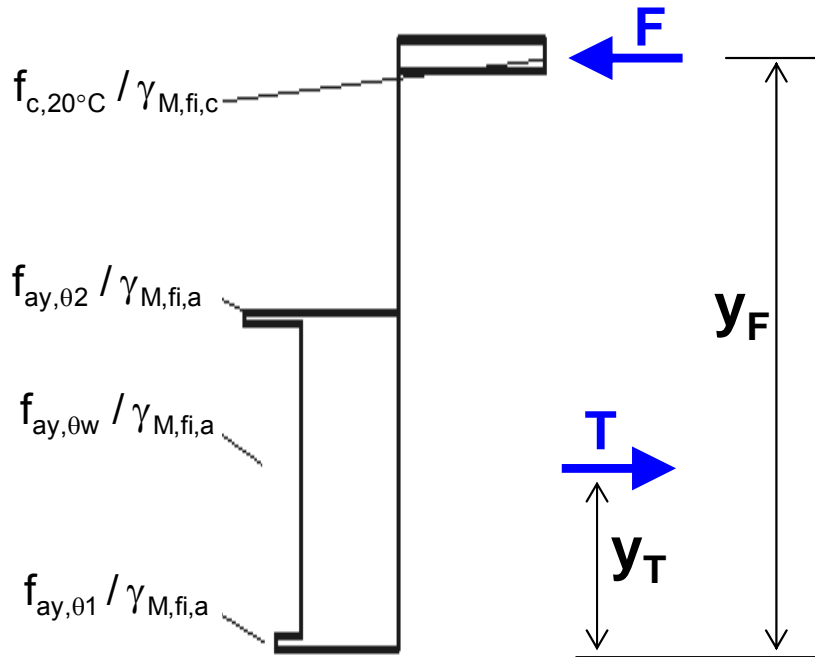
Determination of the thickness of the compressive zone of the concrete :

$$h_u = \frac{T}{b_{\text{eff}} \cdot f_c / \gamma_{M,\text{fi},c}} = \frac{2334,096}{3000 \cdot 25 / 1,0} = 31,12 \text{ mm}$$



h_{cr} [mm]	Temperature [°C]	
	30'	60'
5	535	705
10	470	642
15	415	581
20	350	525
25	300	469
30	250	421
35	210	374
40	180	327
45	160	289
50	140	250

Determination of the moment resistance



Location of the force F :

$$y_F \approx h + h_c - (h_u / 2) = 52 \text{ cm}$$

$$M_{fi,Rd} = T \cdot (y_F - y_T) = 692,4 \text{ kNm}$$

Verification :

$$\frac{M_{fi,Ed}}{M_{fi,Rd}} = \frac{571,6}{692,4} = 0,83 < 1$$

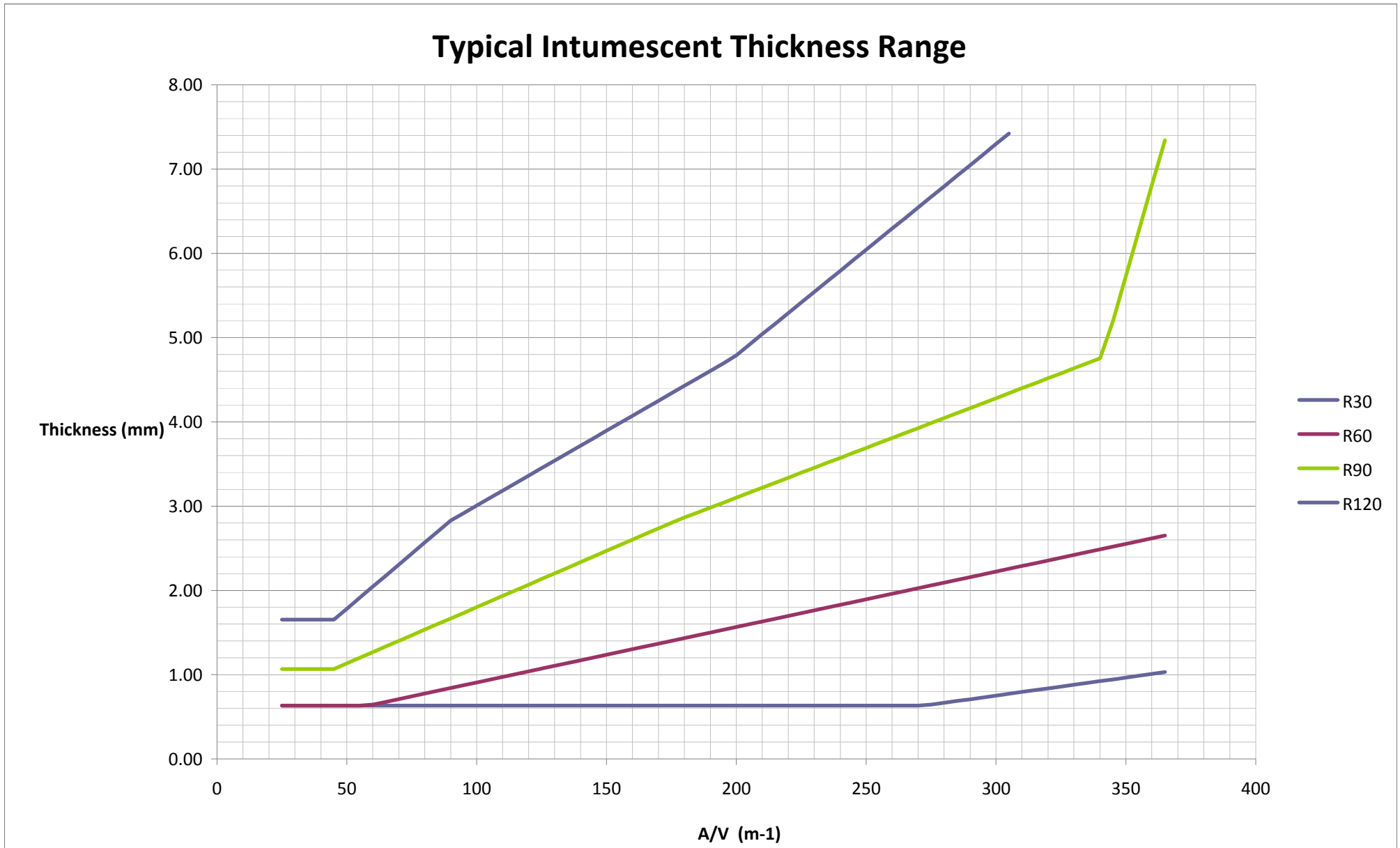
The stability of the beam in fire situation is fulfilled for R60

Verification of the shear resistance

$$V_{pl,fi,Rd} = A_v \cdot \frac{f_{ay,\theta}}{\sqrt{3} \cdot \gamma_{M,fi,a}}$$

$$V_{pl,fi,Rd} = 5090 \cdot \frac{292,5}{\sqrt{3} \cdot 1,0} = 859,5 \text{ kN} > V_{fi,Ed} = \frac{p \cdot l}{2} = 163,33 \text{ kN} \quad \Rightarrow \quad \text{OK}$$


Alternative with reactive coating painted beam

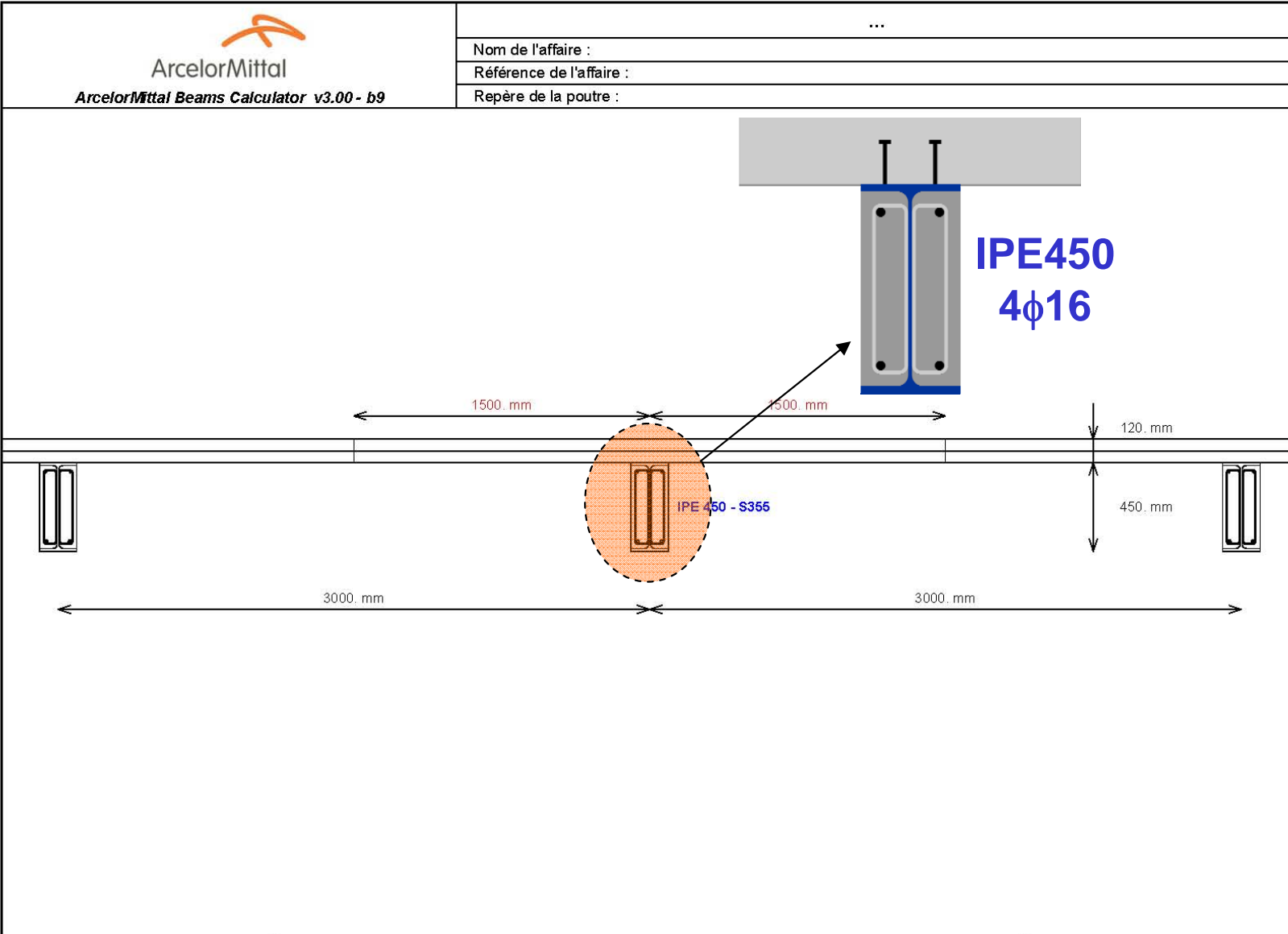


Verification of the composite beam



ABC calculation (Alternative AF solution without fire protection)

 ArcelorMittal ArcelorMittal Beams Calculator v3.00 - b9	...	
	Nom de l'affaire :	
	Référence de l'affaire :	
	Repère de la poutre :	



IPE450
4φ16

1500. mm

1500. mm

120. mm

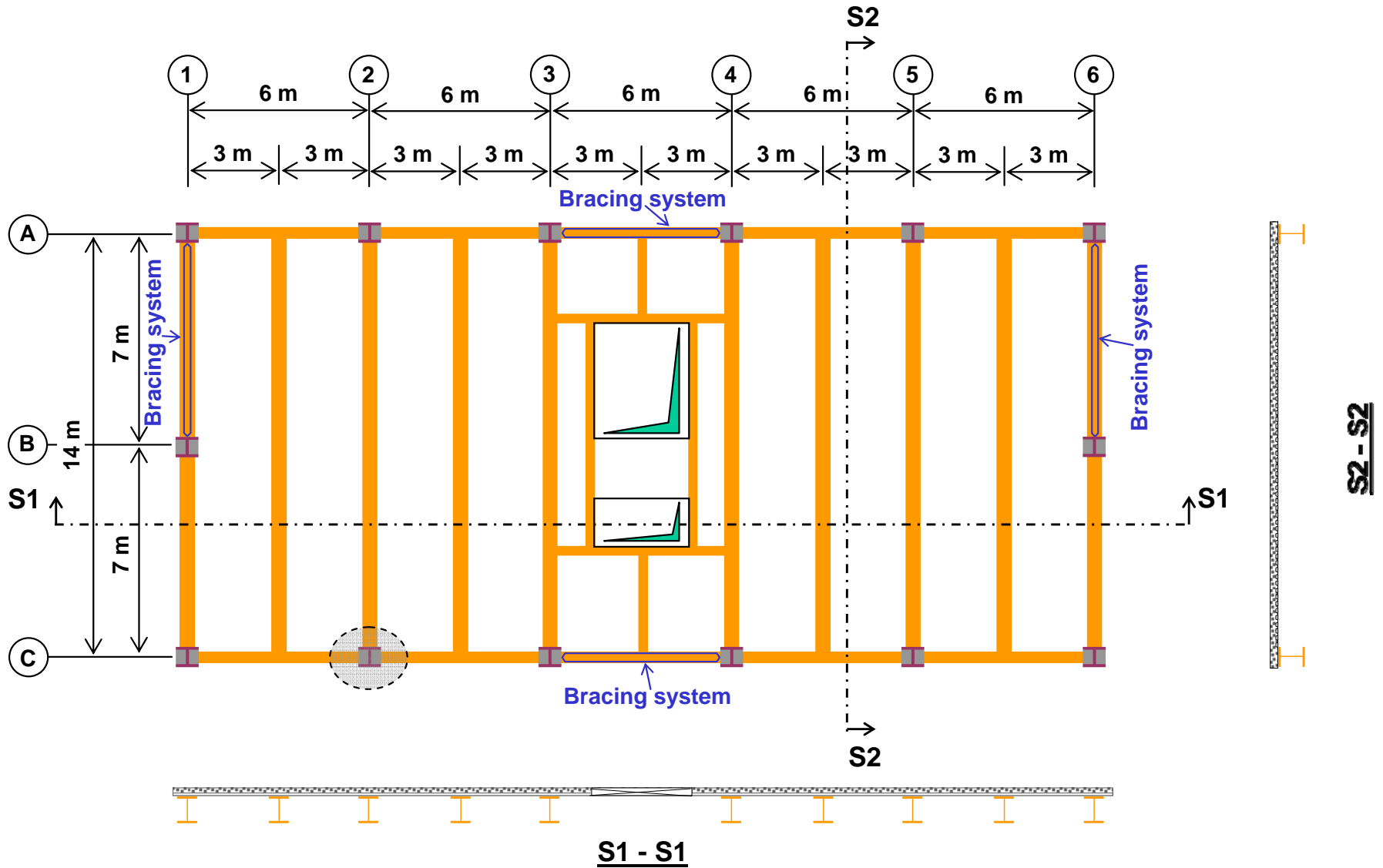
450. mm

IPE 450 - S355

3000. mm

3000. mm

Composite columns



Summary of data

→ Partially encased composite column

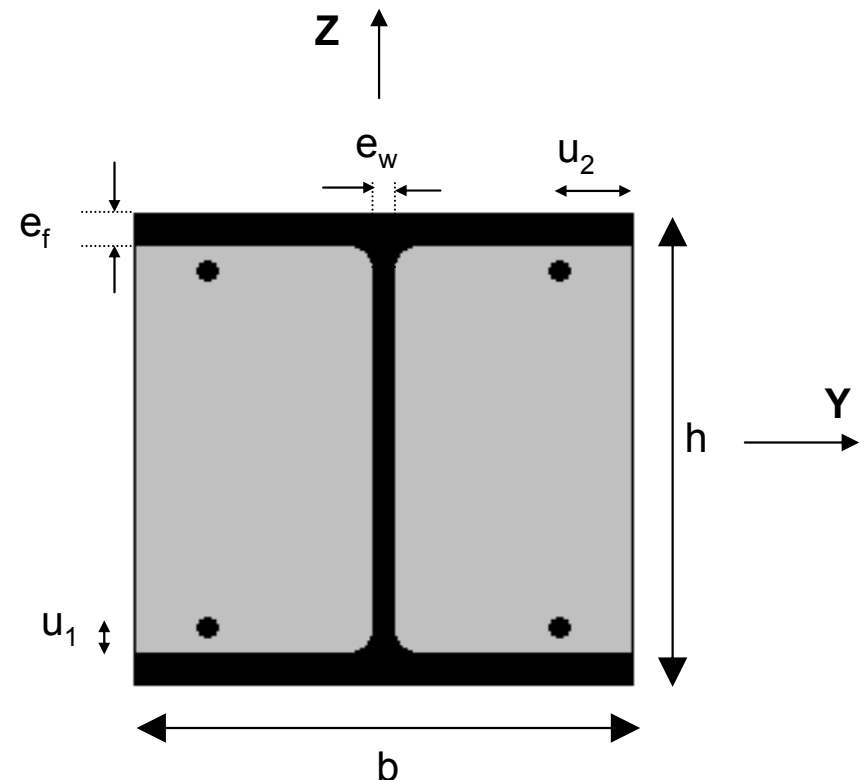
→ Height = 3,40 m

Geometrical characteristics and material properties

Profile : HEA 260
 $h = 250 \text{ mm}$
 $b = 260 \text{ mm}$
 $e_w = 7,5 \text{ mm}$
 $e_f = 12,5 \text{ mm}$
 $A_a = 8680 \text{ mm}^2$
 $f_y = 460 \text{ N/mm}^2$

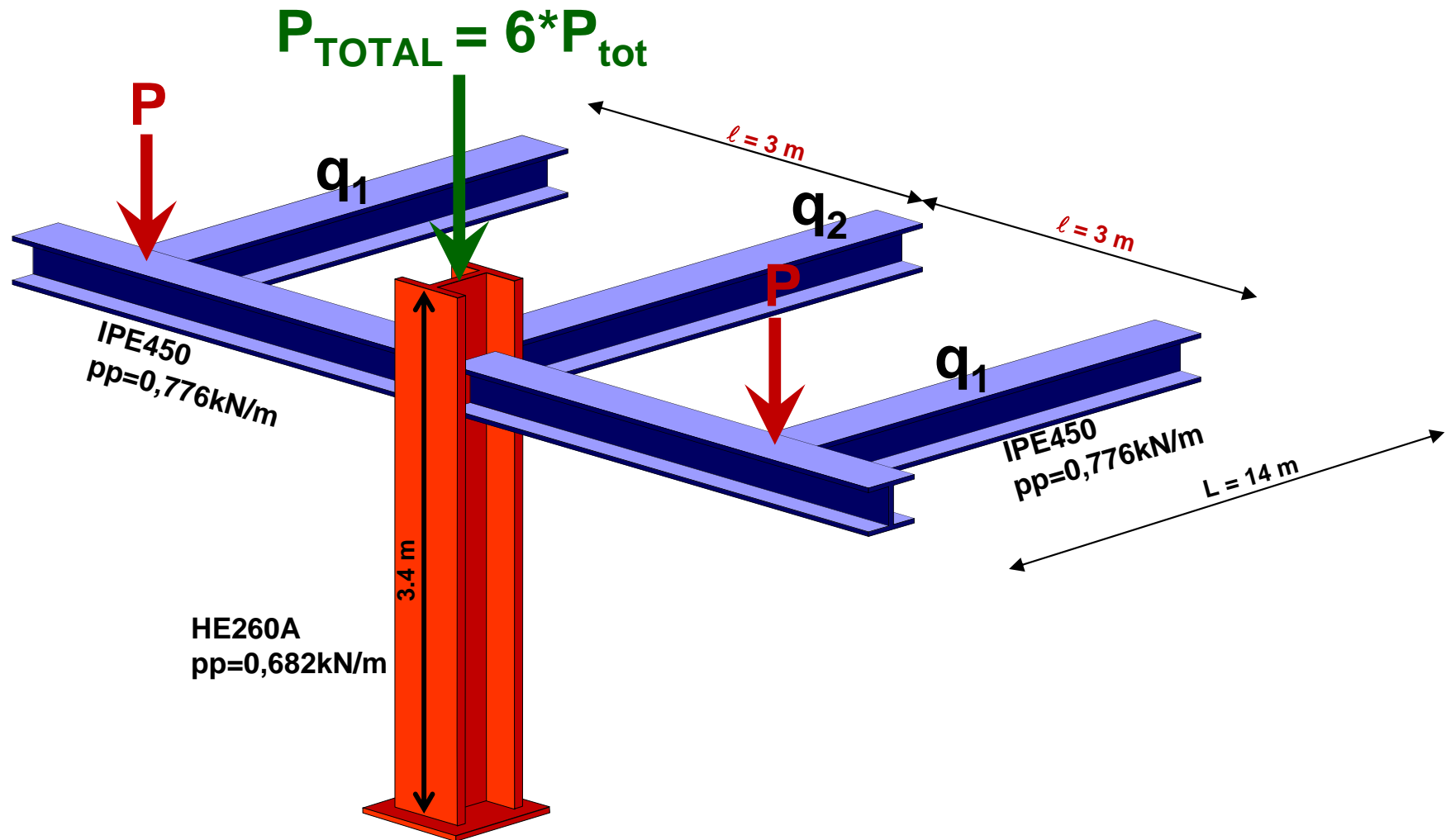
Concrete : C30/37 ; $f_c = 30 \text{ N/mm}^2$
 $A_c = 53860 \text{ mm}^2$

Rebars : 4 $\emptyset 28$; $A_s = 2463 \text{ mm}^2$
 $u_1 = 52 \text{ mm}$; $u_2 = 60 \text{ mm}$
 $f_s = 500 \text{ N/mm}^2$



Verification of the composite column

Load



For one level :

$$q_1 = 1,25 [(3,62+0,6*4,0)*3]+0,776 = 23,351 \text{ kN/m}$$
$$q_2 = 0,750 [(3,62+0,6*4,0)*3]+0,776 = 14,321 \text{ kN/m}$$
$$P_{tot} = (23,351*14/2)+ (14,321*14/2)+2*6+0,776*6+2,14*3,4 = 287,636 \text{ kN}$$

$$P_{TOTAL} = 6 * 287,636 = 1726 \text{ kN}$$

Inertia

Profile : $I_z = 3668 \text{ cm}^4$

$$I_y = 10450 \text{ cm}^4$$

Rebars : $I_{s,z} = 4 \cdot \left[\frac{\pi \cdot d^4}{64} + \frac{\pi \cdot d^2}{4} \left(\frac{b}{2} - u_2 \right)^2 \right] = 1324,6 \text{ cm}^4$

$$I_{s,y} = 4 \cdot \left[\frac{\pi \cdot d^4}{64} + \frac{\pi \cdot d^2}{4} \left(\frac{h}{2} - u_1 \right)^2 \right] = 1218,9 \text{ cm}^4$$

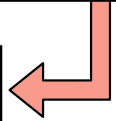
Concrete : $I_{c,z} = \frac{h \cdot b^3}{12} - I_z - I_{s,z} = 31730 \text{ cm}^4$

$$I_{c,y} = \frac{b \cdot h^3}{12} - I_y - I_{s,y} = 22080 \text{ cm}^4$$

Use of tabulated data ($0,28 < \eta_{fi,t} < 0,47$)

Allowed parameters R60	Existing parameters	Fulfilled conditions ?
$e_w / e_f > 0,5$	$7,5 / 12,5 = 0,6$	YES
h and $b > 300$ mm	$h = 250$ mm $b = 260$ mm	NO
u_1 and $u_2 > 50$ mm	$u_1 = 52$ mm $u_2 = 60$ mm	YES
$\frac{A_s}{A_c + A_s} > 4\%$	$\frac{2463}{538,6 + 2463} = 4,4\%$	YES

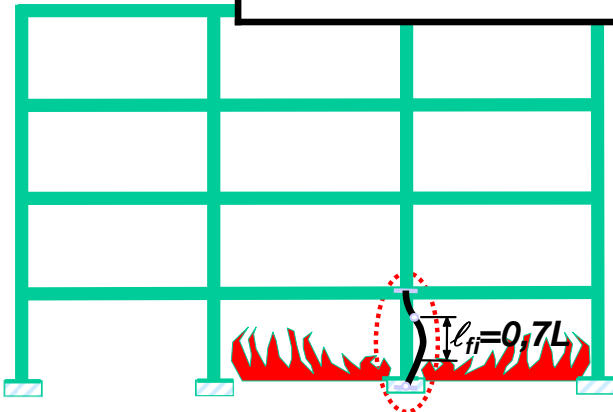
Method not applicable



Simplified method : Application field

Allowed parameters R60	Existing parameters	Fulfilled conditions ?
$l_{\theta} \leq 13,5b = 13,5 \cdot 0,26 = 3,51\text{m}$	$l_{\theta z} = l_{\theta y} = 0,7 \cdot 3,4 = 2,38 \text{ m}$	YES
$230\text{mm} \leq h \leq 1100\text{mm}$	$h = 250 \text{ mm}$	YES
$230\text{mm} \leq b \leq 500$	$b = 260 \text{ mm}$	YES
$1\% \leq A_s / (A_c + A_s) \leq 6\%$	$24,63 / (538,6 + 24,63) = 4,4\%$	YES
max R120	R60	YES
l_{θ} limited to $10b$ if $230 \leq b < 300$	Weak axis : $l_{\theta z} = 2,38 < 10b = 2,6$	YES
	Strong axis : $l_{\theta y} = 2,38 < 10b = 2,6$	YES

Method applicable



Resistance to axial compression according to **weak axis**

Flanges of the profile

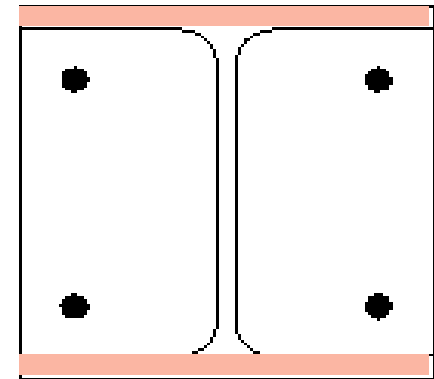
Mean temperature

Standard fire resistance	$\theta_{o,t}$ [°C]	k_t [m°C]
R 30	550	9,65
R 60	680	9,55
R 90	805	6,15
R 120	900	4,65

$$\theta_{f,t} = \theta_{o,t} + k_t \cdot A_m / V$$

$$\text{with } \frac{A_m}{V} = \frac{2(h+b)}{h \cdot b} = 15,7 \text{ m}^{-1}$$

$$\theta_{f,t} = 680 + 9,55 \cdot 15,7 = 830^\circ\text{C}$$



$$\Rightarrow \begin{cases} k_{y,\theta} = 0,095 \\ k_{E,\theta} = 0,083 \end{cases}$$

Plastic resistance :

$$N_{fi,pl,Rd,f} = 2 \cdot (b \cdot e_f \cdot f_{ay,f} \cdot k_{y,\theta}) / \gamma_{M,fi,a}$$

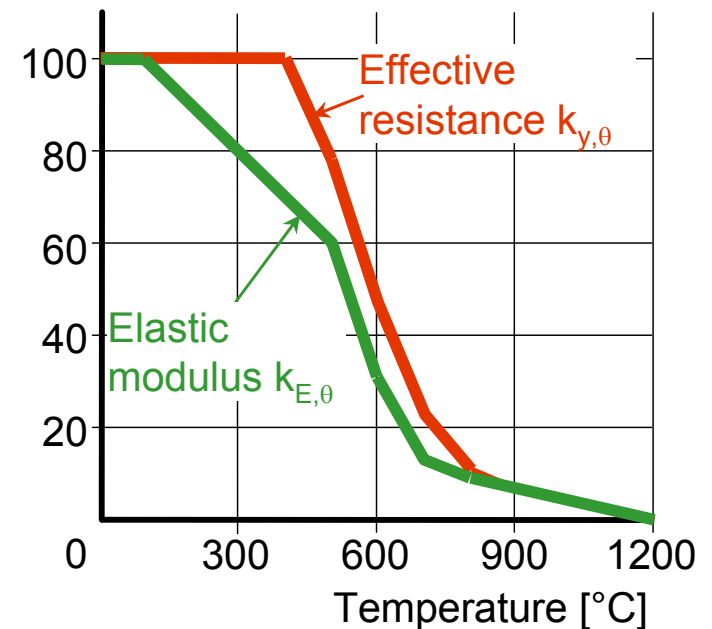
$$N_{fi,pl,Rd,f} = 2 \cdot (260 \cdot 12,5 \cdot 460 \cdot 0,095) / 1,0 = 284,3 \text{ kN}$$

Effective stiffness :

$$(EI)_{fi,f,z} = E_{a,f} \cdot k_{E,\theta} \cdot (e_f \cdot b^3) / 6$$

$$(EI)_{fi,f,z} = 210000 \cdot 0,083 \cdot (12,5 \cdot 260^3) / 6 = 640,4 \text{ kN.m}^2$$

% of the nominal value



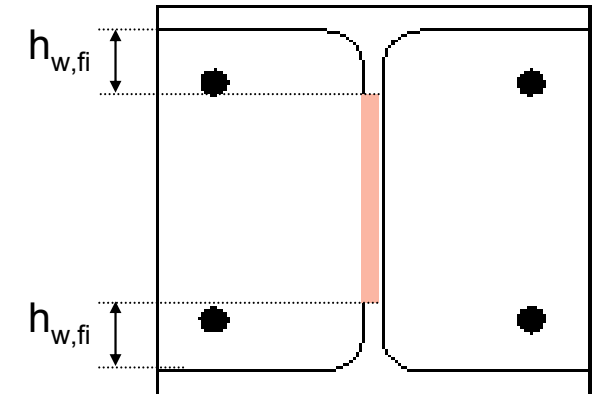
Web of the profile

Reduced height of web :

$$h_{w,fi} = 0,5 \cdot (h - 2 \cdot e_f) \cdot \left(1 - \sqrt{1 - 0,16 \cdot (H_t / h)}\right)$$

$$h_{w,fi} = 0,5 \cdot (250 - 2 \cdot 12,5) \left(1 - \sqrt{1 - 0,16(770/250)}\right) = 32,4 \text{ mm}$$

Standard fire resistance	H_t [mm]
R 30	350
R 60	770
R 90	1100
R 120	1250



Level of maximum stress : $f_{ay,w,t} = f_{ay,w} \sqrt{1 - (0,16H_t/h)}$

$$f_{ay,w,t} = 460 \sqrt{1 - (0,16 \cdot 770 / 250)} = 327,6 \text{ MPa}$$

Plastic resistance :

$$N_{fi,pl,Rd,w} = \left[e_w (h - 2e_f - 2h_{w,fi}) f_{ay,w,t} \right] / \gamma_{M,fi,a}$$

$$N_{fi,pl,Rd,w} = (7,5(250 - 2 \cdot 12,5 - 2 \cdot 32,4)327,6) / 1,0 = 393,7 \text{ kN}$$

Effective stiffness :

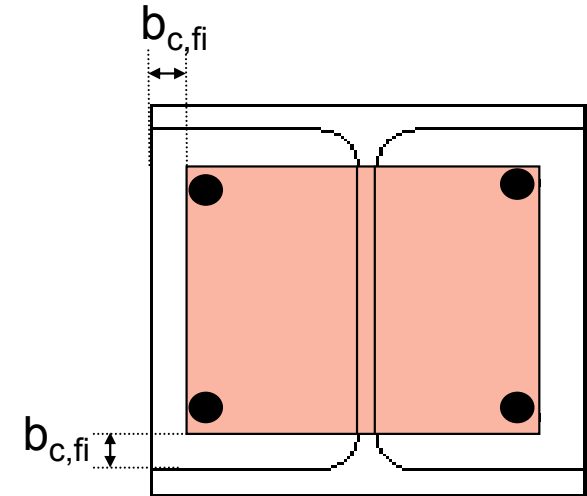
$$(EI)_{fi,w,z} = \left[E_{a,w} (h - 2e_f - 2h_{w,fi}) e_w^3 \right] / 12$$

$$(EI)_{fi,w,z} = (210000(250 - 2 \cdot 12,5 - 2 \cdot 32,4)7,5^3) / 12 = 1,18 \text{ kN.m}^2$$

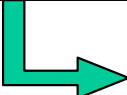
Concrete

Reduced thickness of concrete : $b_{c,fi}$

Standard fire resistance	$b_{c,fi}$ [mm]
R30	4,0
R60	15,0
R90	$0,5(A_m/V)+22,5$
R120	$2,0(A_m/V)+24,0$



R30		R60		R90		R120	
A_m/V [m ⁻¹]	$\theta_{c,t}$ [°C]	A_m/V [m ⁻¹]	$\theta_{c,t}$ [°C]	A_m/V [m ⁻¹]	$\theta_{c,t}$ [°C]	A_m/V [m ⁻¹]	$\theta_{c,t}$ [°C]
4	136	4	214	4	256	4	265
23	300	9	300	6	300	5	300
46	400	21	400	13	400	9	400
---	---	50	600	33	600	23	600
---	---	---	---	54	800	38	800
---	---	---	---	---	---	41	900
---	---	---	---	---	---	43	1000

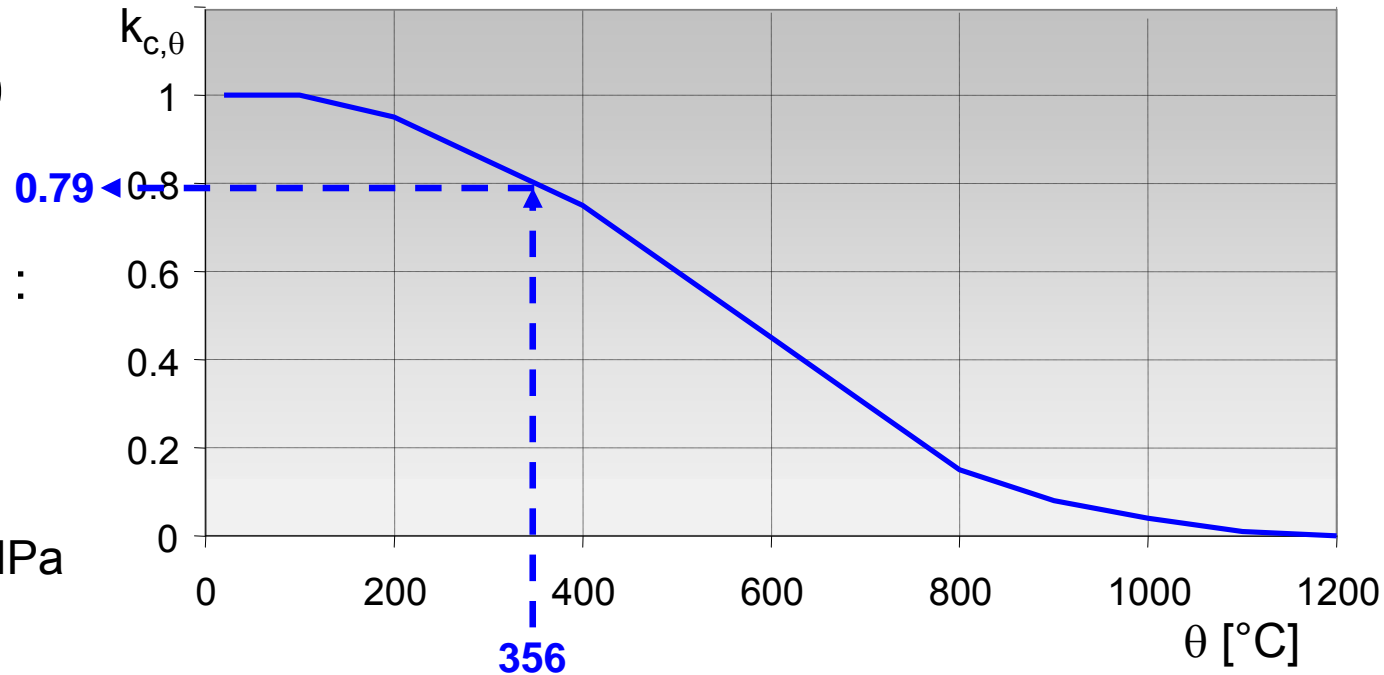

 $A_m/V = 15,7\text{m}^{-1} \Rightarrow$ Average temperature in the concrete $\theta_{c,t} = 356^\circ\text{C}$

$$\theta_{c,t} = 356^{\circ}\text{C} \quad \rightarrow \quad k_{c,\theta} = 0,79$$

Secant modulus of concrete :

$$E_{c,\text{sec},\theta} = \frac{f_{c,\theta}}{\varepsilon_{\text{cu},\theta}} = \frac{f_c \cdot k_{c,\theta}}{\varepsilon_{\text{cu},\theta}}$$

$$E_{c,\text{sec},\theta} = \frac{30 \cdot 0,79}{8,68 \cdot 10^{-3}} = 2746,4 \text{ MPa}$$



Plastic resistance :

$$N_{\text{fi,pl,Rd,c}} = 0,86 \left\{ (h - 2e_f - 2b_{c,\text{fi}})(b - e_w - 2b_{c,\text{fi}}) - A_s \right\} f_{c,\theta} / \gamma_{\text{M,fi,c}}$$

$$N_{\text{fi,pl,Rd,c}} = 0,86 \cdot \left\{ (250 - 2 \cdot 12,5 - 2 \cdot 15)(260 - 7,5 - 2 \cdot 15) - 2463 \right\} \cdot 25 \cdot 0,79 / 1,0 = 839 \text{ kN}$$

Effective stiffness :

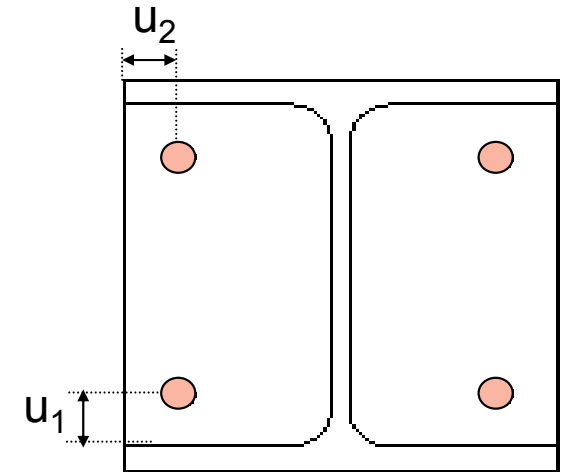
$$(EI)_{\text{fi,c,z}} = E_{c,\text{sec},\theta} \left[\left\{ (h - 2e_f - 2b_{c,\text{fi}}) \left((b - 2b_{c,\text{fi}})^3 - e_w^3 \right) / 12 \right\} - I_{s,z} \right]$$

$$(EI)_{\text{fi,c,z}} = 2746,4 \left[\left\{ (250 - 2 \cdot 12,5 - 2 \cdot 15) \left((260 - 2 \cdot 15)^3 - 7,5^3 \right) / 12 \right\} - 1324,6 \cdot 10^4 \right] = 509,5 \text{ kN} \cdot \text{m}^2$$

Reinforcing bars

Reduction factor for yield strength : $k_{y,t}$					
Standard fire resistance	u [mm]				
	40	45	50	55	60
R30	1	1	1	1	1
R60	0,789	0,883	0,9763	1	1
R90	0,314	0,434	0,572	0,696	0,822
R120	0,170	0,223	0,288	0,367	0,436

Reduction factor for Young modulus : $k_{E,t}$					
Standard fire resistance	u [mm]				
	40	45	50	55	60
R30	0,830	0,865	0,88	0,914	0,935
R60	0,604	0,647	0,689	0,729	0,763
R90	0,193	0,283	0,406	0,522	0,619
R120	0,110	0,128	0,173	0,233	0,285



$$u = \sqrt{u_1 \cdot u_2} = \sqrt{52 \cdot 60} = 55,86 \text{ mm}$$

Plastic resistance : $N_{fi,pl,Rd,s} = A_s \cdot k_{y,t} \cdot f_{s,y} / \gamma_{M,fi,s}$

$$N_{fi,pl,Rd,s} = 2463 \cdot 1,0 \cdot 500 / 1,0 = 1231,5 \text{ kN}$$

Effective stiffness : $(EI)_{fi,s,z} = k_{E,t} \cdot E_s \cdot I_{s,z}$

$$(EI)_{fi,s,z} = 0,735 \cdot 210000 \cdot 1218,9 \cdot 10^4 = 1881,4 \text{ kN.m}^2$$

Plastic resistance of the composite section

$$N_{fi,pl,Rd} = N_{fi,pl,Rd,f} + N_{fi,pl,Rd,w} + N_{fi,pl,Rd,c} + N_{fi,pl,Rd,s}$$

$$N_{fi,pl,Rd} = 284,3 + 393,7 + 839 + 1231,5 = 2748 \text{ kN}$$

Effective stiffness of the composite section

$$(EI)_{fi,eff,z} = \varphi_{f,\theta} (EI)_{fi,f,z} + \varphi_{w,\theta} (EI)_{fi,w,z} + \varphi_{c,\theta} (EI)_{fi,c,z} + \varphi_{s,\theta} (EI)_{fi,s,z}$$

Standard fire resistance	$\varphi_{f,\theta}$	$\varphi_{w,\theta}$	$\varphi_{c,\theta}$	$\varphi_{s,\theta}$
R30	1,0	1,0	0,8	1,0
R60	0,9	1,0	0,8	0,9
R90	0,8	1,0	0,8	0,8
R120	1,0	1,0	0,8	1,0

$$(EI)_{fi,eff,z} = 0,9 \cdot 640,4 + 1,0 \cdot 1,18 + 0,8 \cdot 509,5 + 0,9 \cdot 1881,4 = 2678,4 \text{ kN.m}^2$$

Determination of the axial buckling load at elevated temperatures

Euler buckling load :

$$N_{fi,cr,z} = \frac{\pi^2 \cdot (EI)_{fi,eff,z}}{\ell_{\theta z}^2} \quad \text{with } \ell_{\theta z} = 2,38 \text{ m}$$

$$N_{fi,cr,z} = \frac{\pi^2 \cdot 2678,4}{2,38^2} = 4667 \text{ kN}$$

Slenderness ratio :

$$\bar{\lambda}_{\theta} = \sqrt{\frac{N_{fi,pl,R}}{N_{fi,cr,z}}} = \sqrt{\frac{2748}{4667}} = 0,767 \quad \longrightarrow \quad \text{c curve} \rightarrow \chi_z = 0,683$$

Axial buckling resistance :

$$N_{fi,Rd,z} = \chi_z \cdot N_{fi,pl,Rd}$$

$$N_{fi,Rd,z} = 0,683 \cdot 2748 = 1876 \text{ kN} > N_{fi,Rd} = 1726 \text{ kN}$$

Resistance to axial compression according to strong axis

Same method as for weak axis, excepted of the inertia !

Plastic resistance of the composite section

$$N_{fi,pl,Rd} = N_{fi,pl,Rd,f} + N_{fi,pl,Rd,w} + N_{fi,pl,Rd,c} + N_{fi,pl,Rd,s} = 2748 \text{ kN}$$

Effective stiffness of the composite section

$$(EI)_{fi,eff,y} = \varphi_{f,\theta} (EI)_{fi,f,y} + \varphi_{w,\theta} (EI)_{fi,w,y} + \varphi_{c,\theta} (EI)_{fi,c,y} + \varphi_{s,\theta} (EI)_{fi,s,y} = 4097,1 \text{ kN.m}^2$$

Euler buckling load

$$N_{fi,cr,y} = \frac{\pi^2 \cdot (EI)_{fi,eff,y}}{l_{\theta y}^2} = 7138,8 \text{ kN}$$

Slenderness ratio

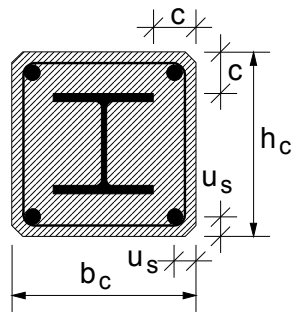
$$\bar{\lambda}_{\theta} = \sqrt{\frac{N_{fi,pl,R}}{N_{fi,cr,y}}} = 0,62$$

Axial buckling resistance

$$N_{fi,Rd,y} = \chi_y \cdot N_{fi,pl,Rd} = 2124,8 \text{ kN} > N_{fi,Rd} = 1726 \text{ kN}$$

A3C calculation (Alternative solution : Fully encased HEB160)

Tabulated data



Standard Fire Resistance

		R30	R60	R90	R120	R180	R240
1.1	Minimum dimensions h_c and b_c [mm]	150	180	220	300	350	400
1.2	minimum concrete cover of steel section c [mm]	40	50	50	75	75	75
1.3	minimum axis distance of reinforcing bars u_s [mm]	20*	30	30	40	50	50
or							
2.1	Minimum dimensions h_c and b_c [mm]	-	200	250	350	400	-
2.2	minimum concrete cover of steel section c [mm]	-	40	40	50	60	-
2.3	minimum axis distance of reinforcing bars u_s [mm]	-	20*	20*	30	40	-

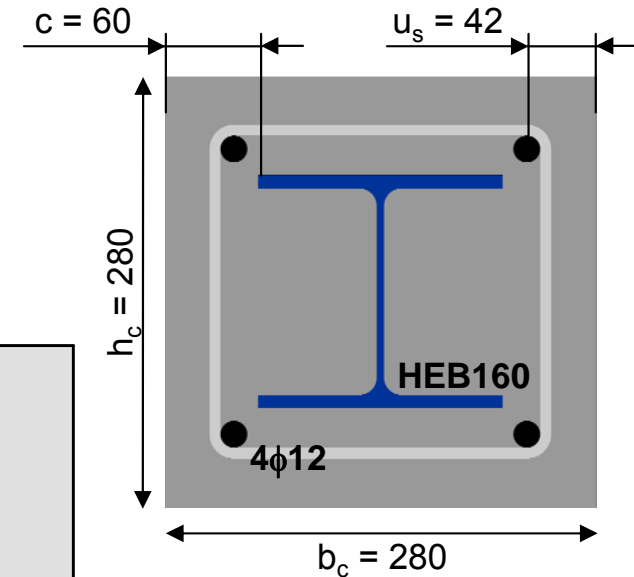


Table 4.4: Minimum cross-sectional dimensions, minimum concrete cover of the steel section and minimum axis distance of the reinforcing bars, of composite columns made of totally encased steel sections.