



Conceptual Fire Design and assessment

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Part I

CONCEPTUAL FIRE DESIGN

(Fabienne ROBERT)



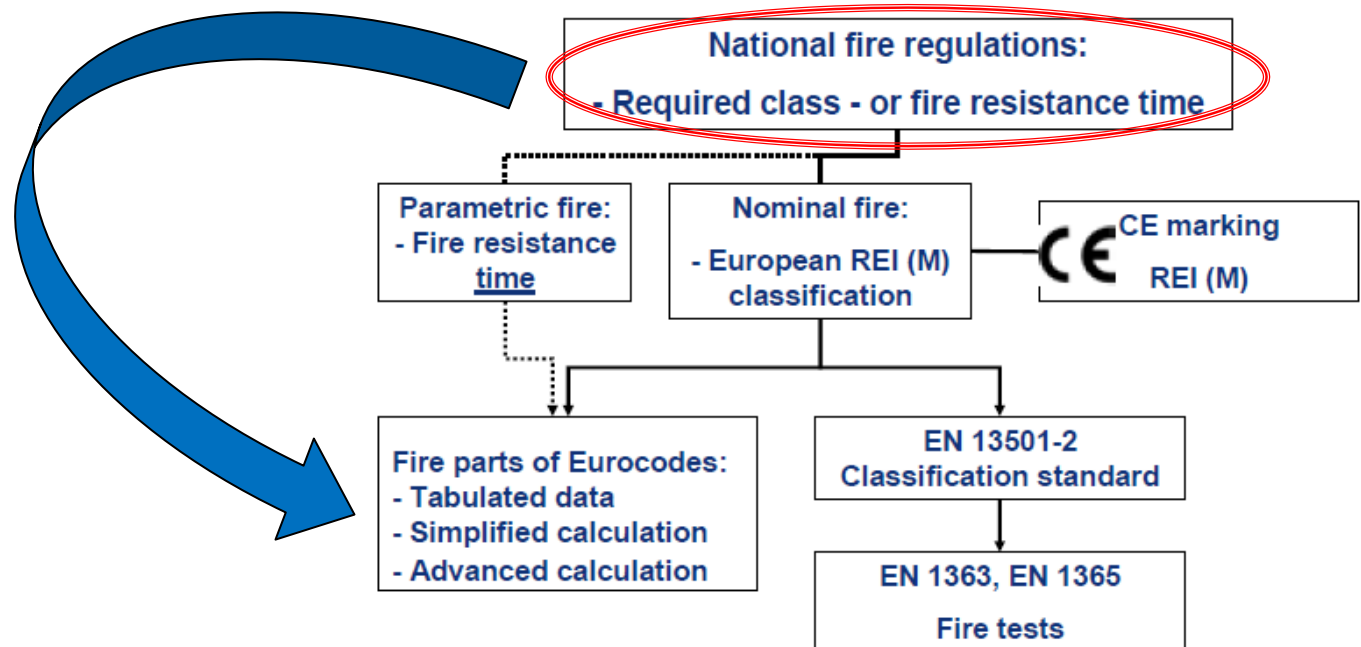
The construction works must be designed and build in such a way, that in the event of an outbreak of fire :

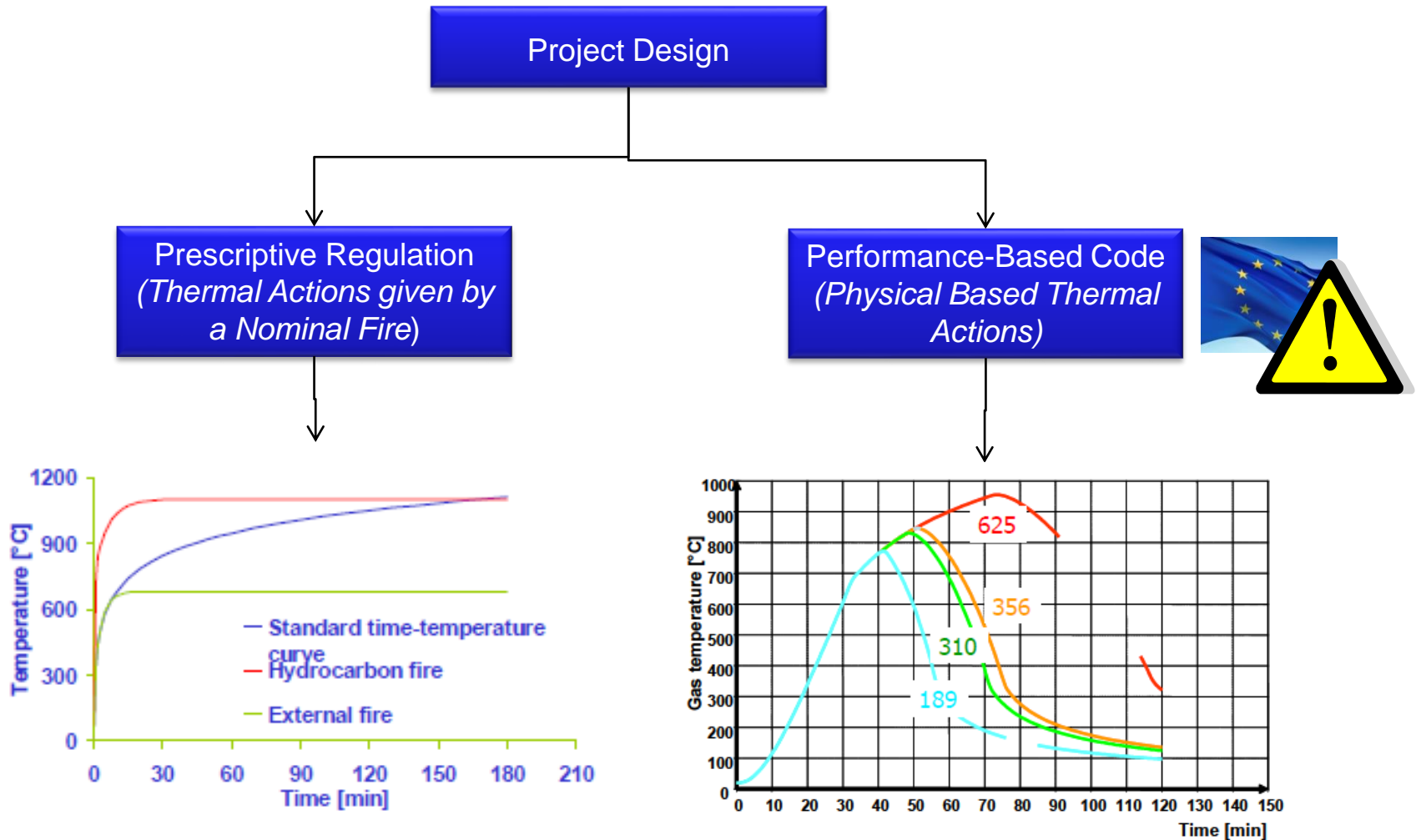
- the load bearing resistance of the construction can be assumed for a specified period of time
- the generation and spread of fire and smoke within the works are limited
- the spread of fire to neighbouring construction works is limited
- the occupants can leave the works or can be rescued by other means
- the safety of rescue teams is taken into consideration

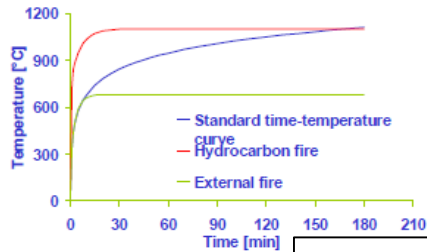


To prove compliance with Essential Requirements :

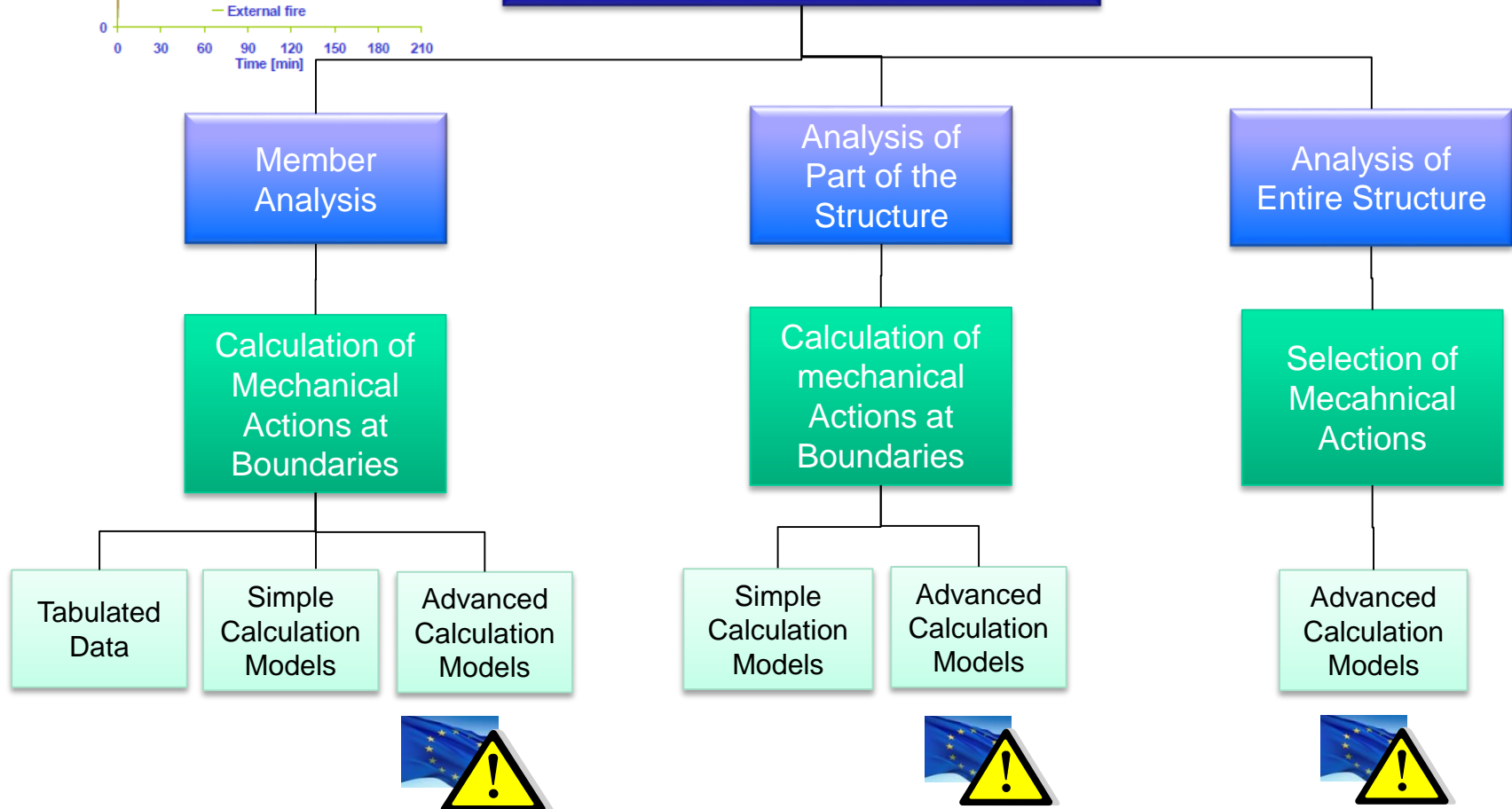
- Tests + extended applications of results
- calculation and/or design methods
- combination of tests and calculations

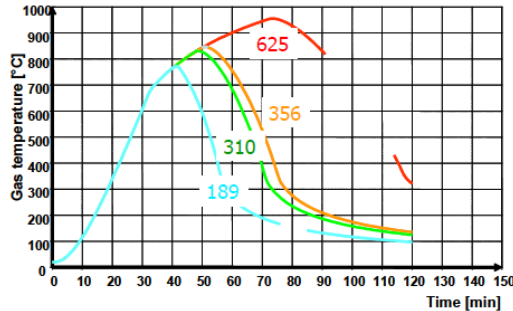






Prescriptive Rules (Thermal Actions by Nominal Fire)





Performance-Based Code
(Physically based Thermal Actions)

Selection of Simple or Advanced Fire
Development Models



Member
Analysis

Calculation of
Mechanical
Actions at
Boundaries

Simple
Calculation
Models
(if available)

Advanced
Calculation
Models

Analysis of
Part of the
Structure

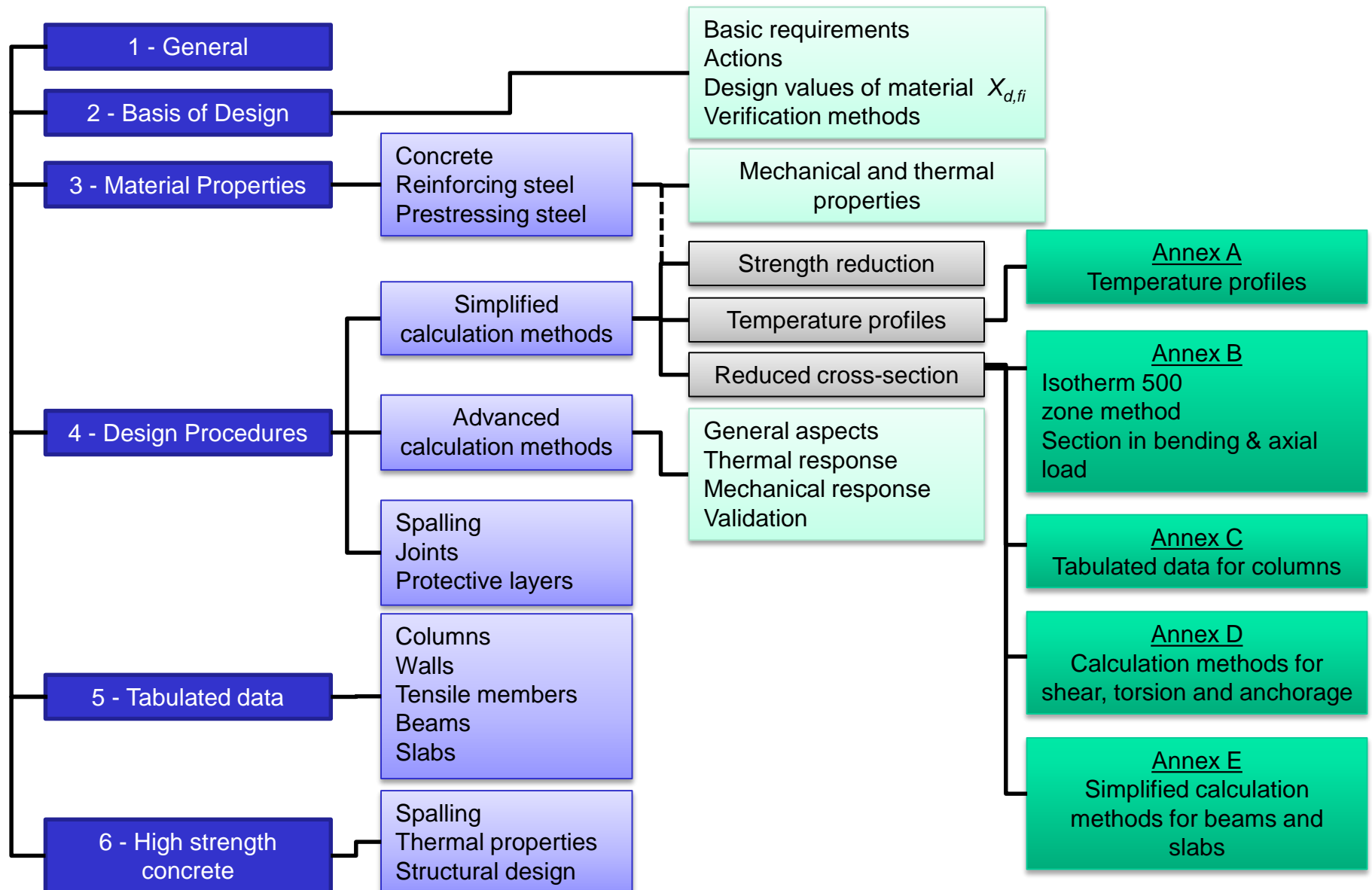
Calculation of
mechanical
Actions et
Boundaries

Advanced
Calculation
Models

Analysis of
Entire
Structure

Selection of
Mechanical
Actions

Advanced
Calculation
Models





Scope

- Design of concrete structures for fire exposure in conjunction with EN 1992-1-1 and EN 1991-1-2
- Applicable to normal weight concrete up to C 90/105 and lightweight concrete up to LC 50/60

□ Requirements

- ✓ **Design to maintain the load-bearing function (R) and/or**
- ✓ **Design and construction to maintain the separating function (E, I)**
 - **Nominal fire exposure during the required time period**
 - **Parametric fire exposure during the complete duration of fire (specific criterion for I in the decay phase)**



□ Design values of material properties

- Mechanical material properties

$$X_{d,fi} = k_{\theta} \cdot X_k / \gamma_{M,fi}$$

- Thermal material properties

$$X_{d,fi} = X_k / \gamma_{M,fi} \text{ (favourable)}$$

$$X_{d,fi} = X_k \cdot \gamma_{M,fi} \text{ (unfavourable)}$$

$$\gamma_{M,fi} = 1,0$$





- (1) The effect of actions should be determined for time $t = 0$ using combination factors $\psi_{1,1}$ or $\psi_{1,2}$ according to EN 1991-1-2 Section 4.
- (2) As a simplification to (1) the effects of actions may be obtained from a structural analysis for normal temperature design as:

$$E_{d,fi} = \eta_{fi} E_d$$

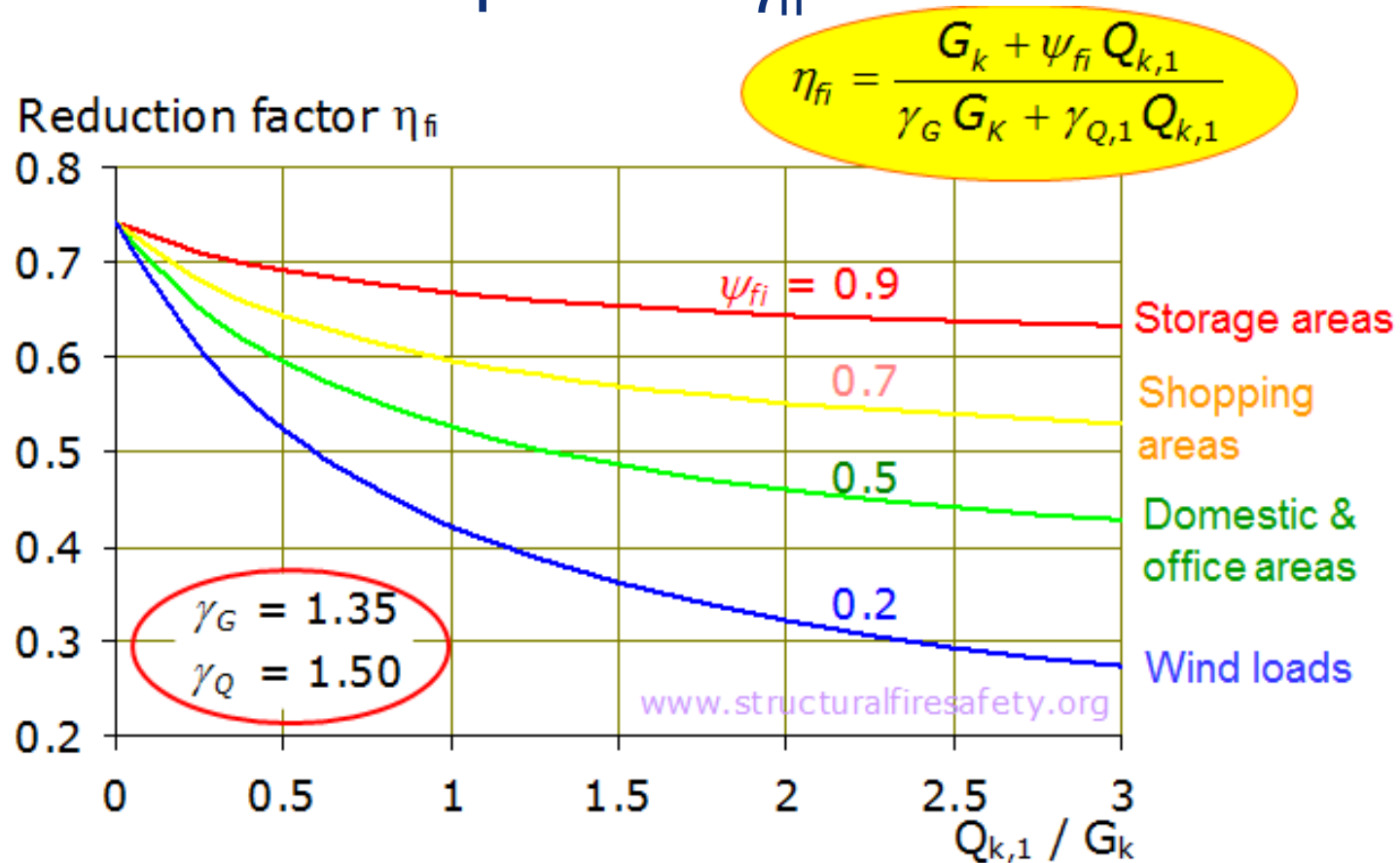
Where

E_d is the design value of the corresponding force or moment for normal temperature design, for a fundamental combination of actions (see EN 1990);

η_{fi} is the reduction factor for the design load level for the fire situation.



Example for η_{fi}



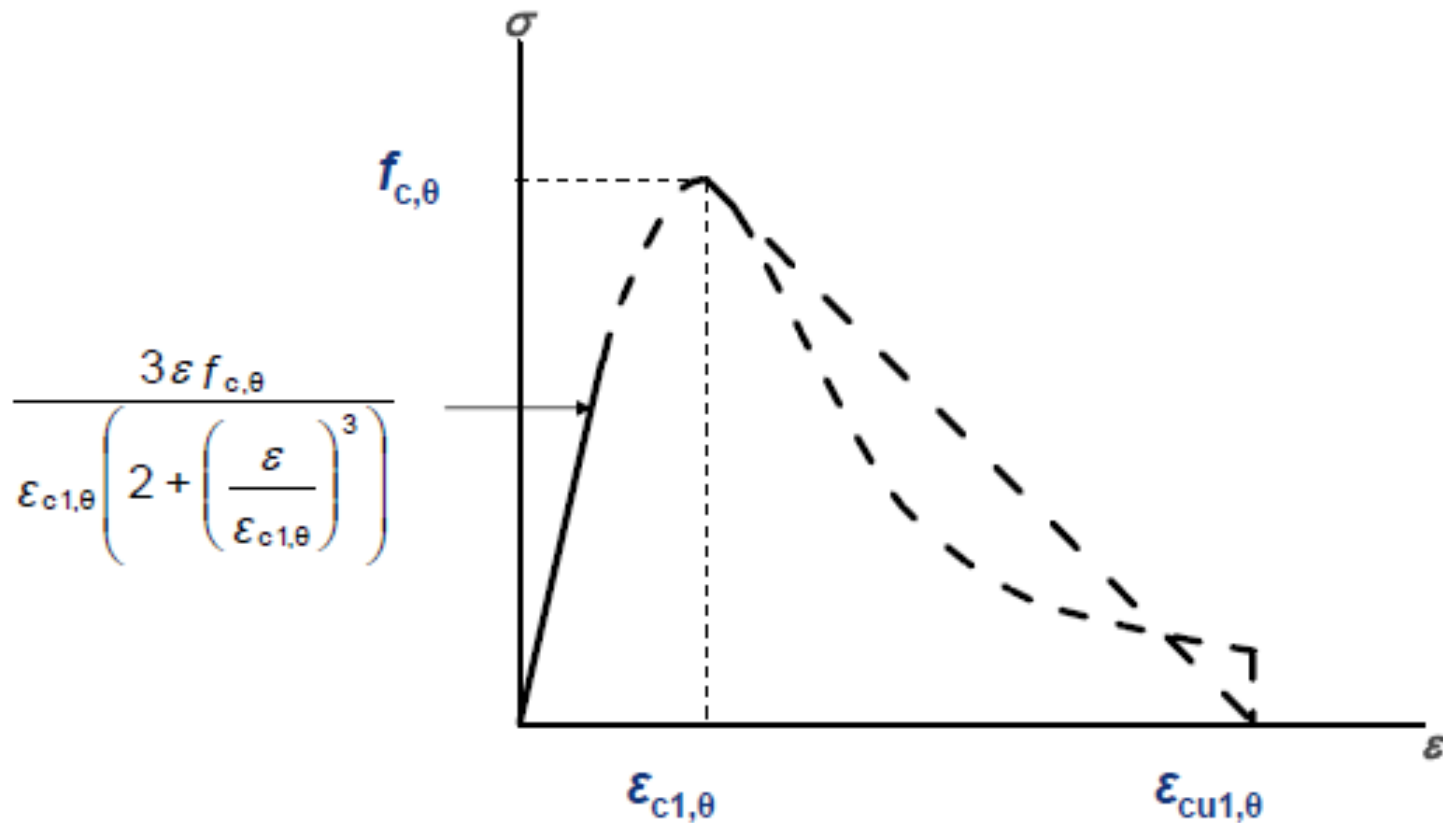
Note 2: As a simplification a recommended value of $\eta_{fi} = 0,7$ may be used.



- **Strength and deformation properties in Section 3** are given for simplified and advanced calculation methods
- **Strength reduction curves for Tabulated data (in Section 5) and Simplified calculation methods (in Section 4)** are derived from material properties in section 3
- **Thermal properties** are given in Section 3 for calculation of temperature distribution inside the structure
- Material properties for **lightweight concrete** are not given due to wide range of lightweight aggregates
 - **this does not exclude use of lightweight aggregate concrete, see e.g. Scope and Tabulated data**
- Strength and deformation properties are applicable to **heating rates** similar to standard fire curve (between 2 and 50 K/min)



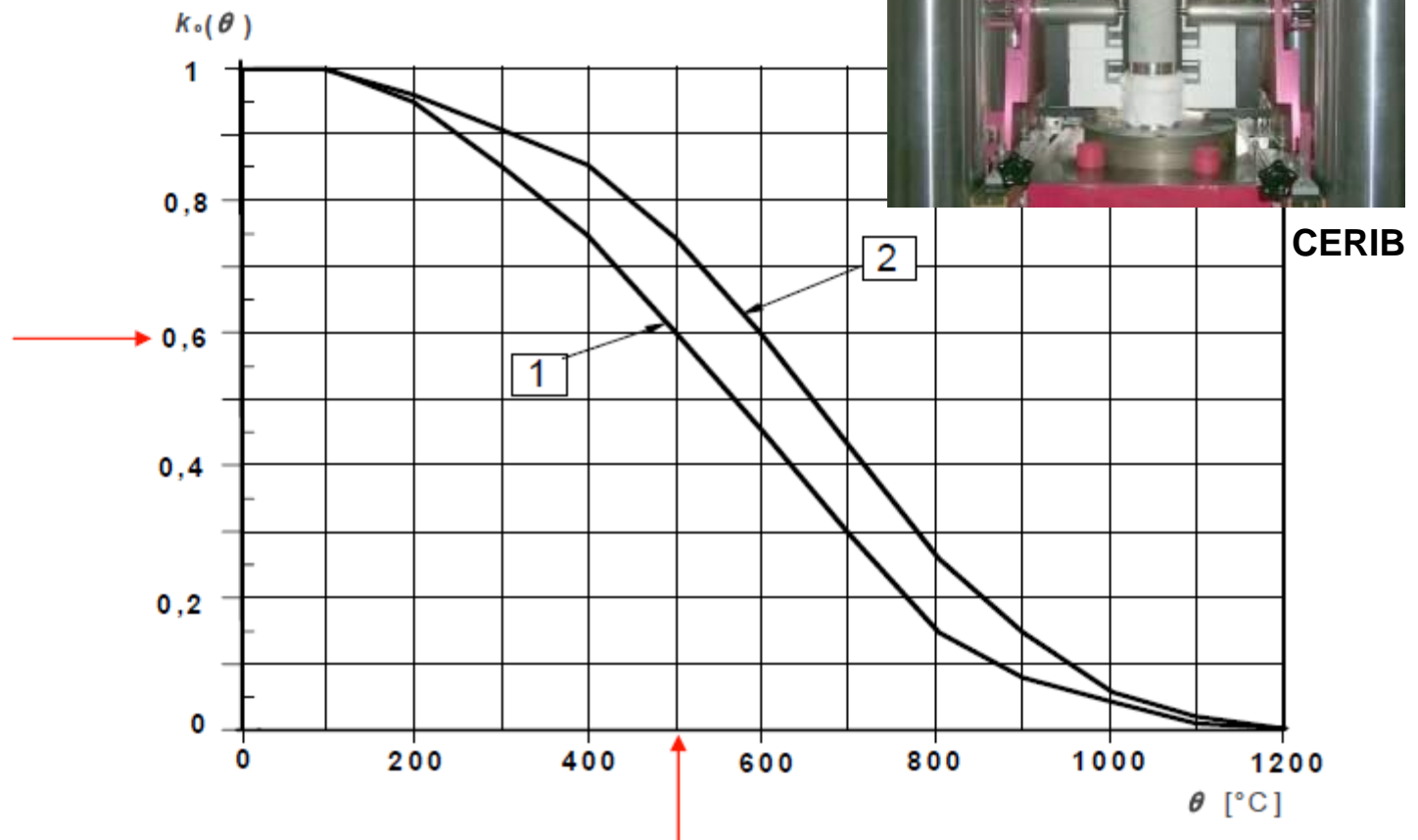
Mathematical model and parameters $f_{c,\theta}$, $\epsilon_{c1,\theta}$ and $\epsilon_{cu1,\theta}$
 $\alpha_{cc} = 1,0$ in fire design

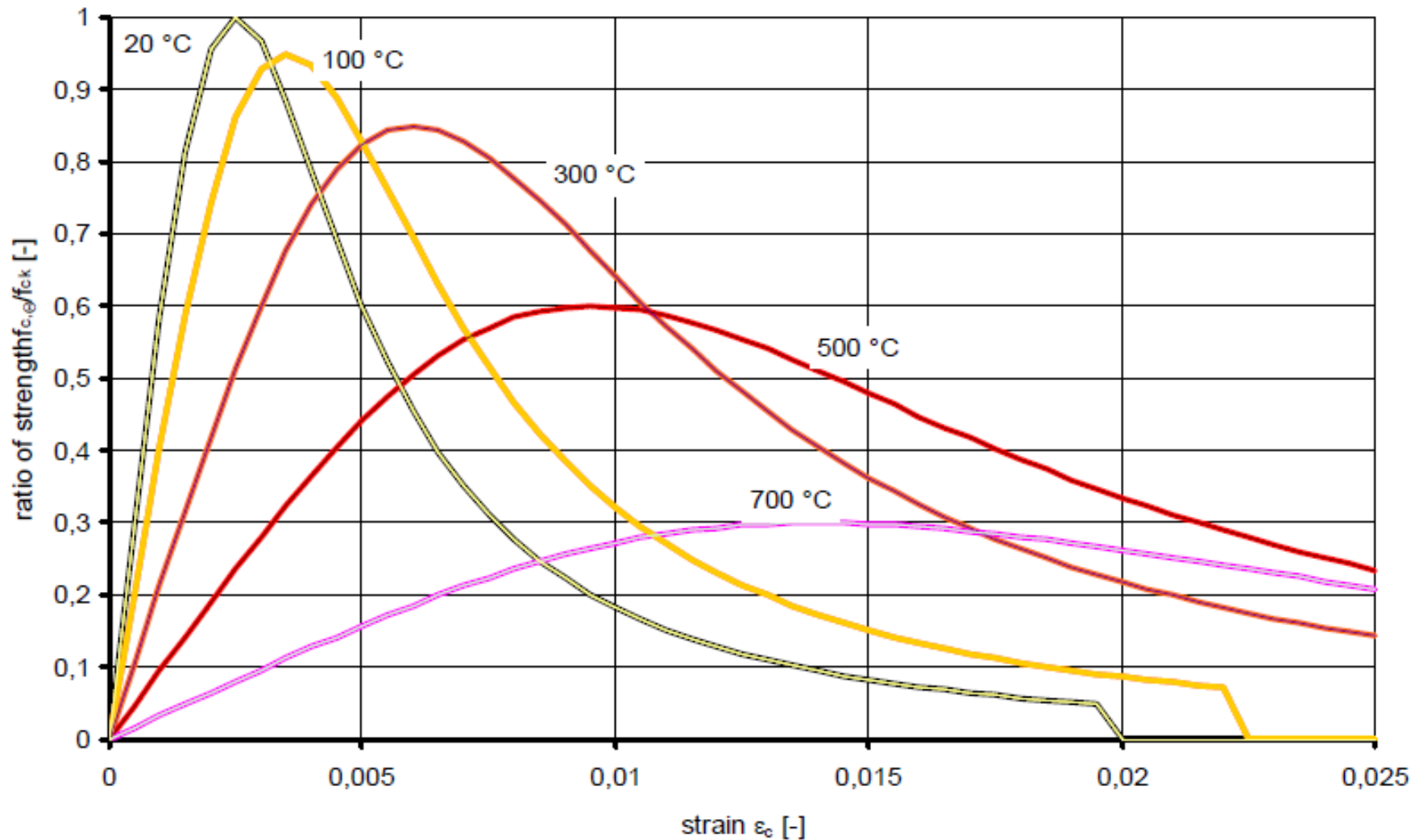




The same strength reduction values are given for simplified calculation methods in Section 4

1. Siliceous concrete
2. Calcareous concrete







$$\varepsilon_{sp,\theta} = f_{sp,\theta} / E_{s,\theta} \quad \varepsilon_{sy,\theta} = 0,02$$

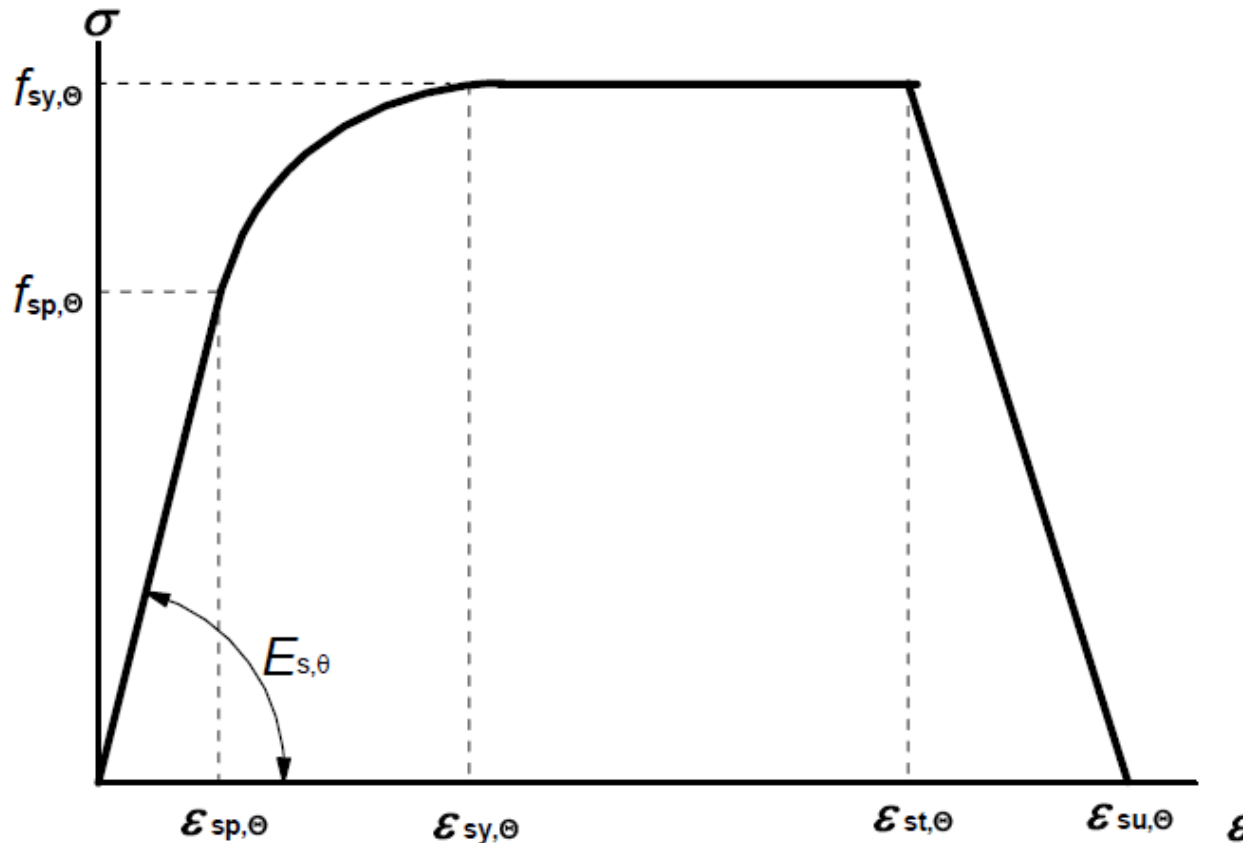
$$\varepsilon_{st,\theta} = 0,15$$

$$\varepsilon_{su,\theta} = 0,20$$

Class A reinforcement:

$$\varepsilon_{st,\theta} = 0,05$$

$$\varepsilon_{su,\theta} = 0,10$$





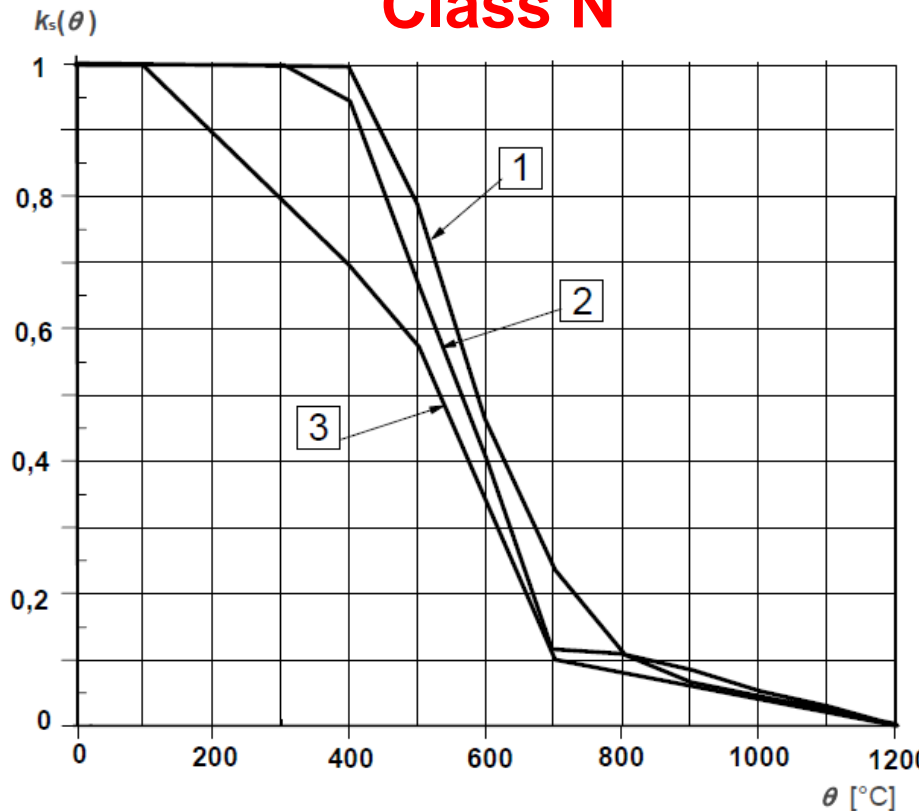
EUROCODE 2 Strength reduction (f_{yk}) for reinforcing steel

Background and Applications

Dissemination of information for training – Brussels, 20-21 October 2011

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Class N

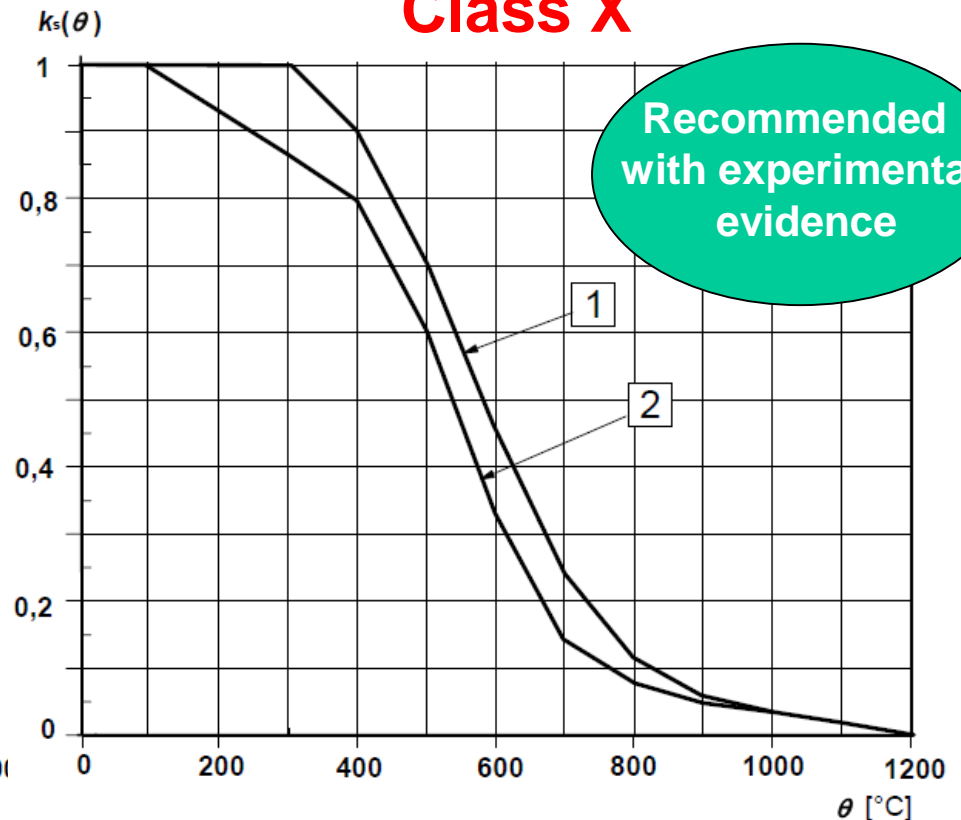


Curve 1 : Tension reinforcement (hot rolled) for strains $\varepsilon_{s,fi} \geq 2\%$

Curve 2 : Tension reinforcement (cold worked) for strains $\varepsilon_{s,fi} \geq 2\%$

Curve 3 : Compression reinforcement and tension reinforcement for strains $\varepsilon_{s,fi} < 2\%$

Class X

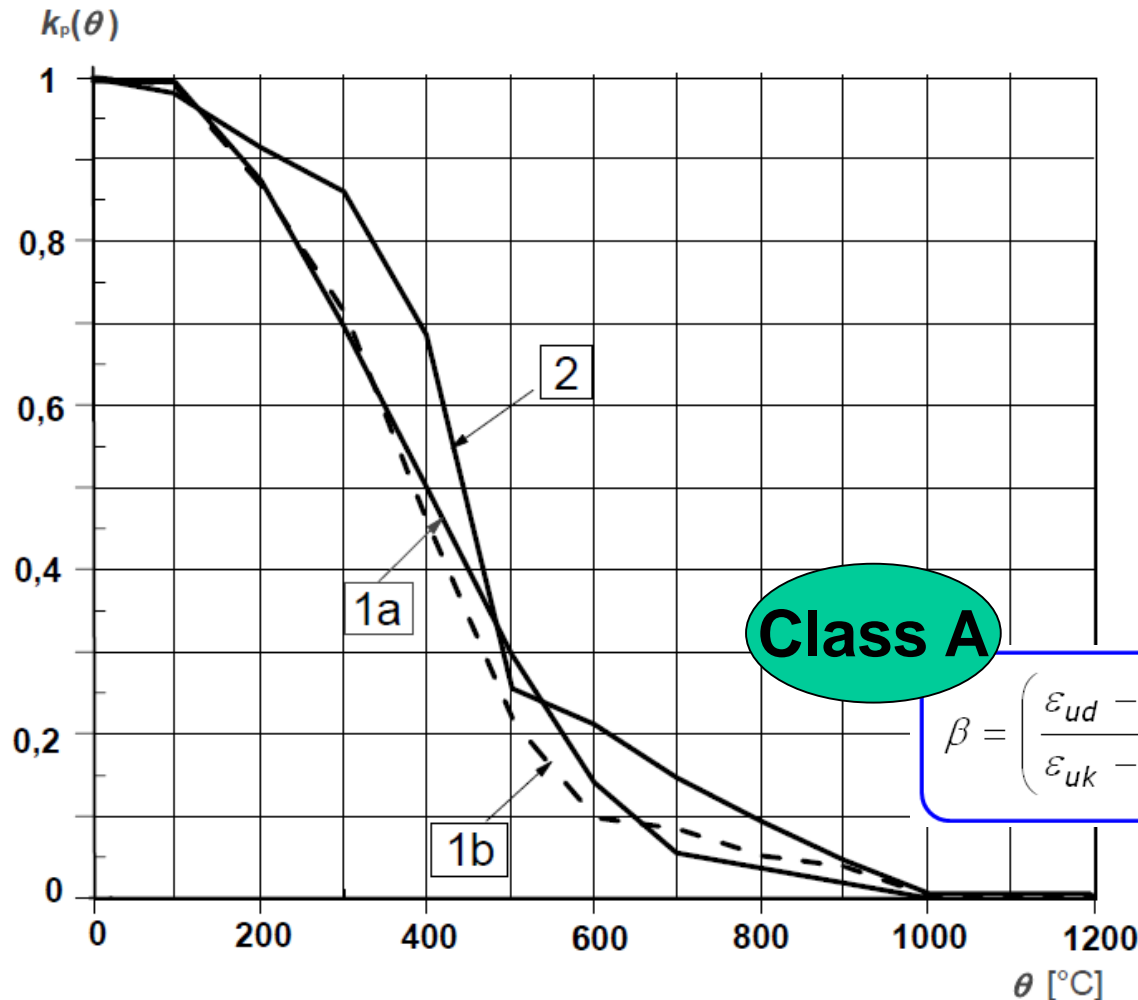


Curve 1 : Tension reinforcement (hot rolled and cold worked) for strains $\varepsilon_{s,fi} \geq 2\%$

Curve 2 : Compression reinforcement and tension reinforcement (hot rolled and cold worked) for strains $\varepsilon_{s,fi} < 2\%$



Strength reduction (βf_{pk}) for prestressing steel



Curve **1a** : Cold worked prestressing steel (wires and strands) Class A

Curve **1b** : Cold worked prestressing steel (wires and strands) Class B

Curve **2** : Quenched and tempered prestressing steel (bars)

$$\beta = \left(\frac{\varepsilon_{ud} - f_{p0.1k} / E_p}{\varepsilon_{uk} - f_{p0.1k} / E_p} \right) \times \left(\frac{f_{pk} - f_{p0.1k}}{f_{pk}} \right) + \frac{f_{p0.1k}}{f_{pk}}$$

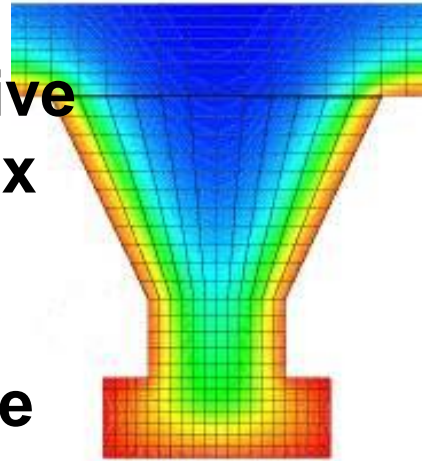
Class B

$$\beta = 0.9$$

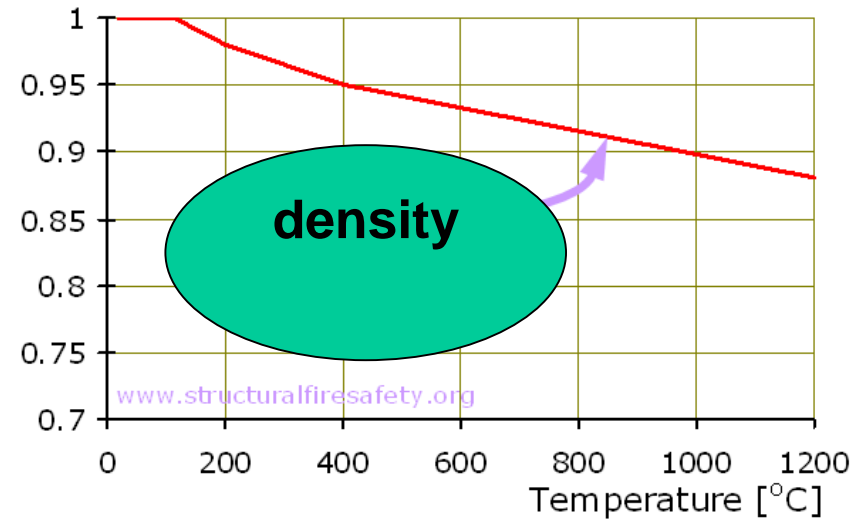


**Convective
heat flux**

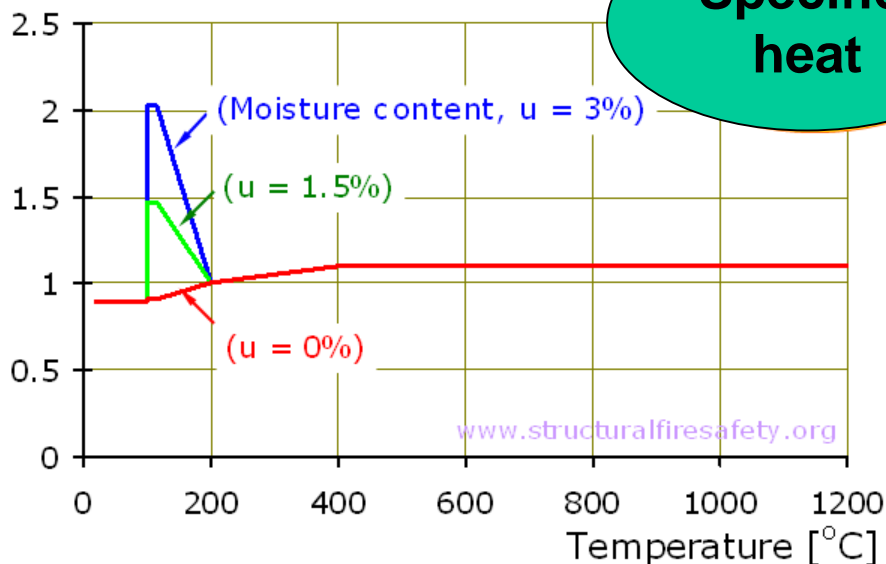
**Radiative
heat flux**



Percentage reduction of density



Specific heat [kJ/kg K]



W/m K]

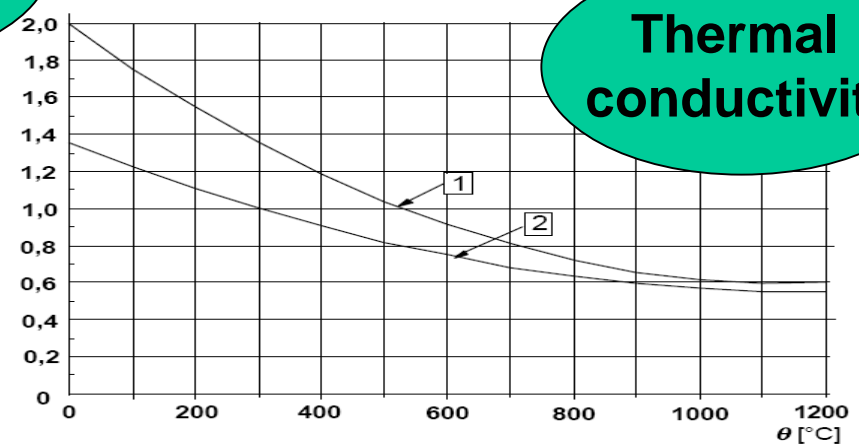
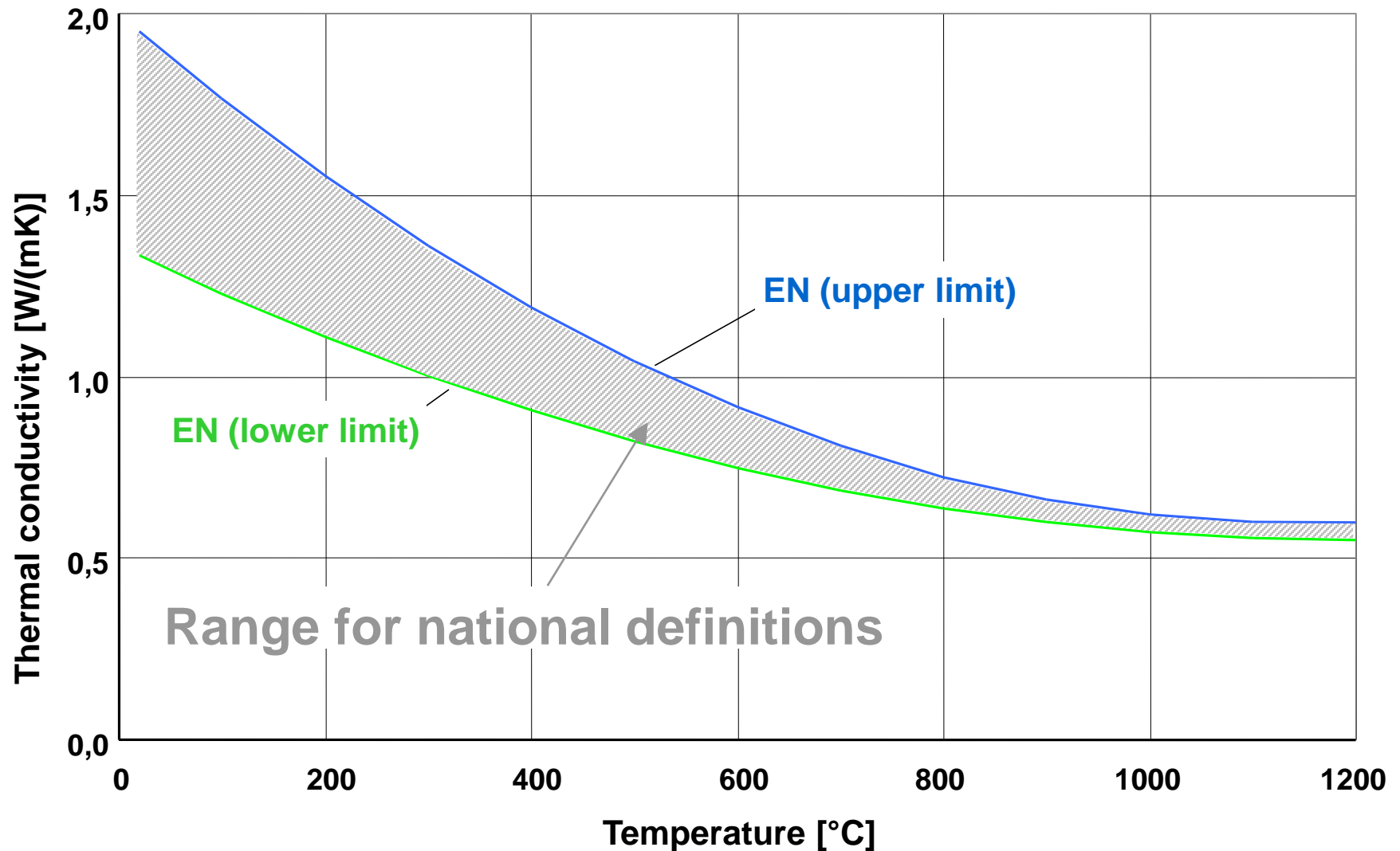
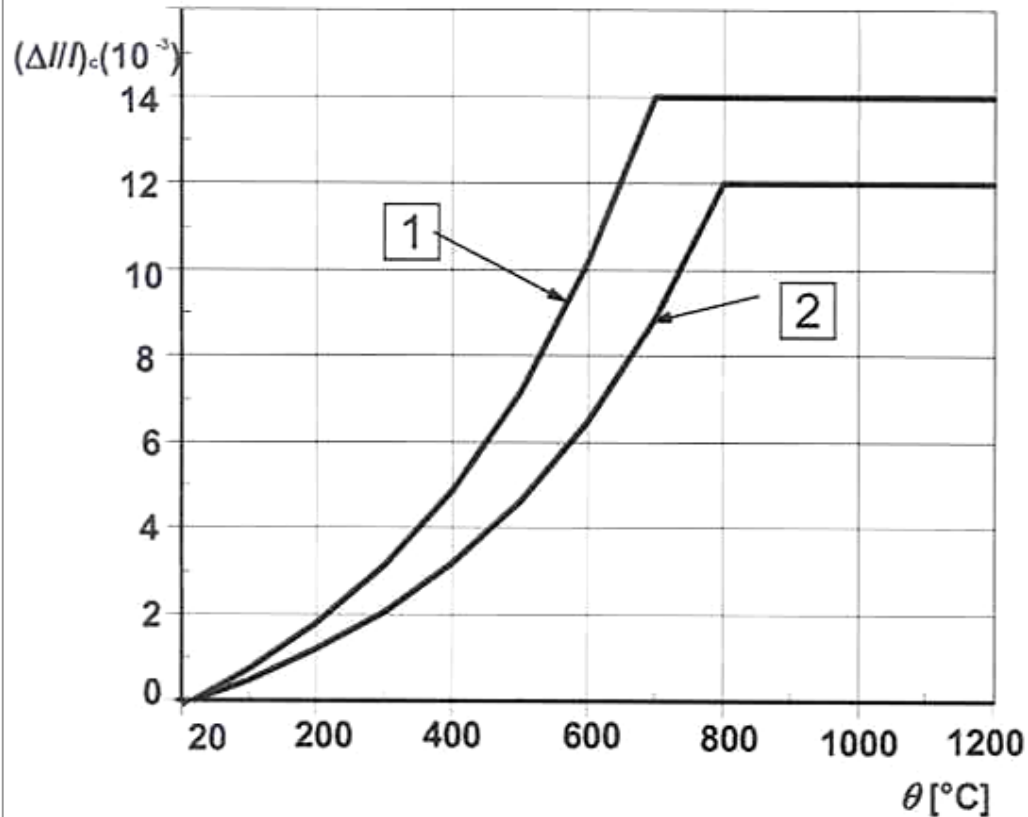


Figure 3.7 – Conductivité thermique du béton





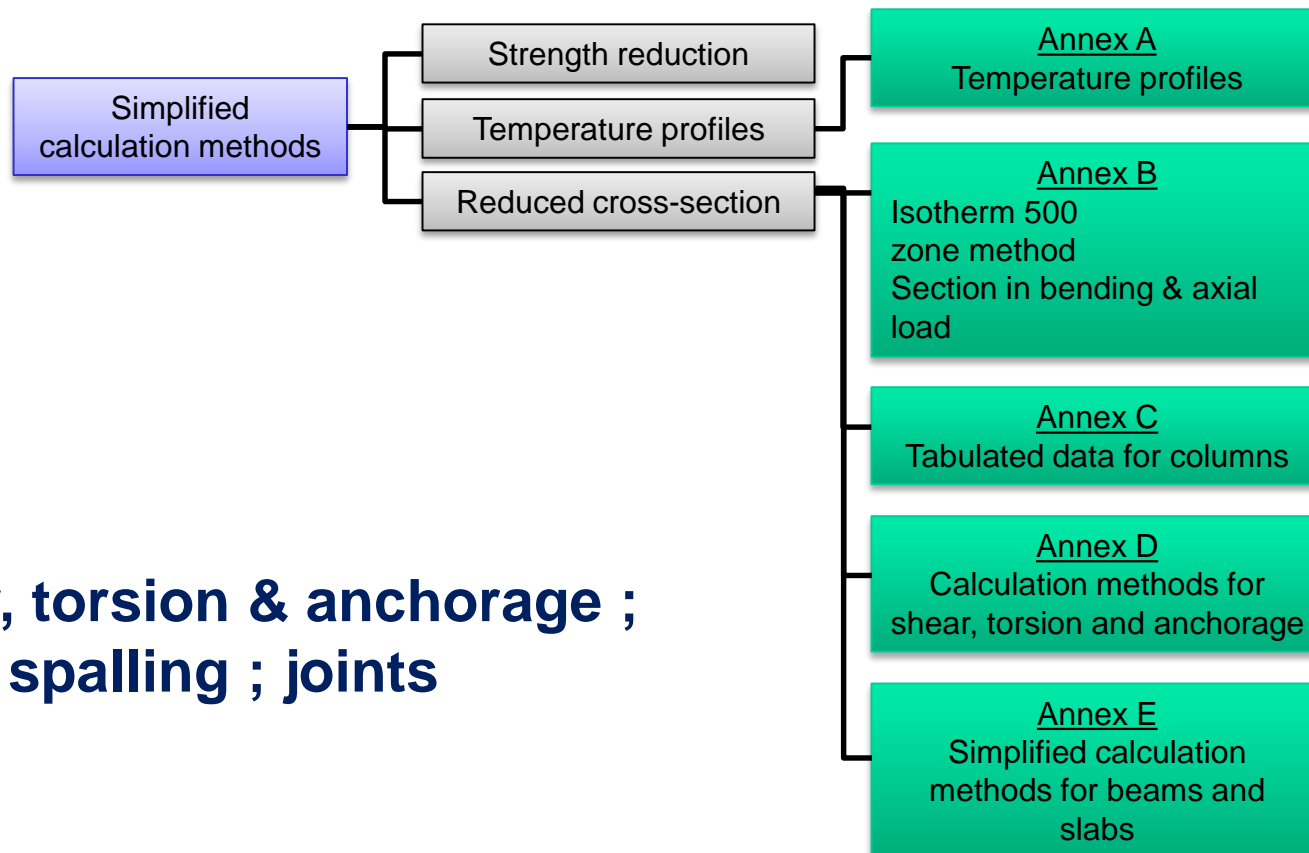
Curve 1: Siliceous aggregate

Curve 2: Calcareous aggregate

Total thermal elongation of concrete



- **advanced calculation methods** for simulating the behaviour of structural members, parts of the structure or the entire structure, see 4.3
 - only principles are given, no detailed design rules
- **simplified calculation methods** for specific types of members, see 4.2



- **shear, torsion & anchorage ;
spalling ; joints**



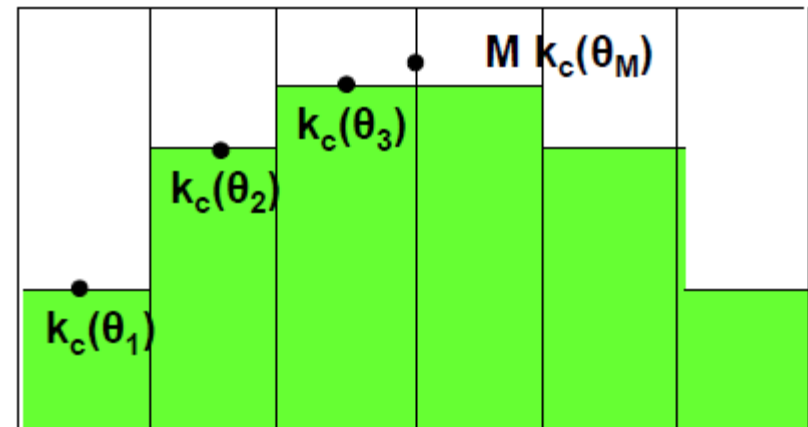
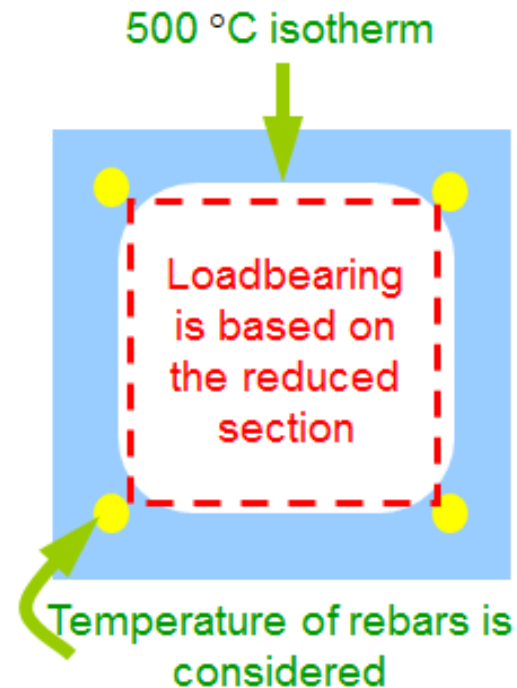
- **500°C isotherm method**

Concrete with temperature below 500°C retains full strength and the rest is disregarded

- **Zone method**

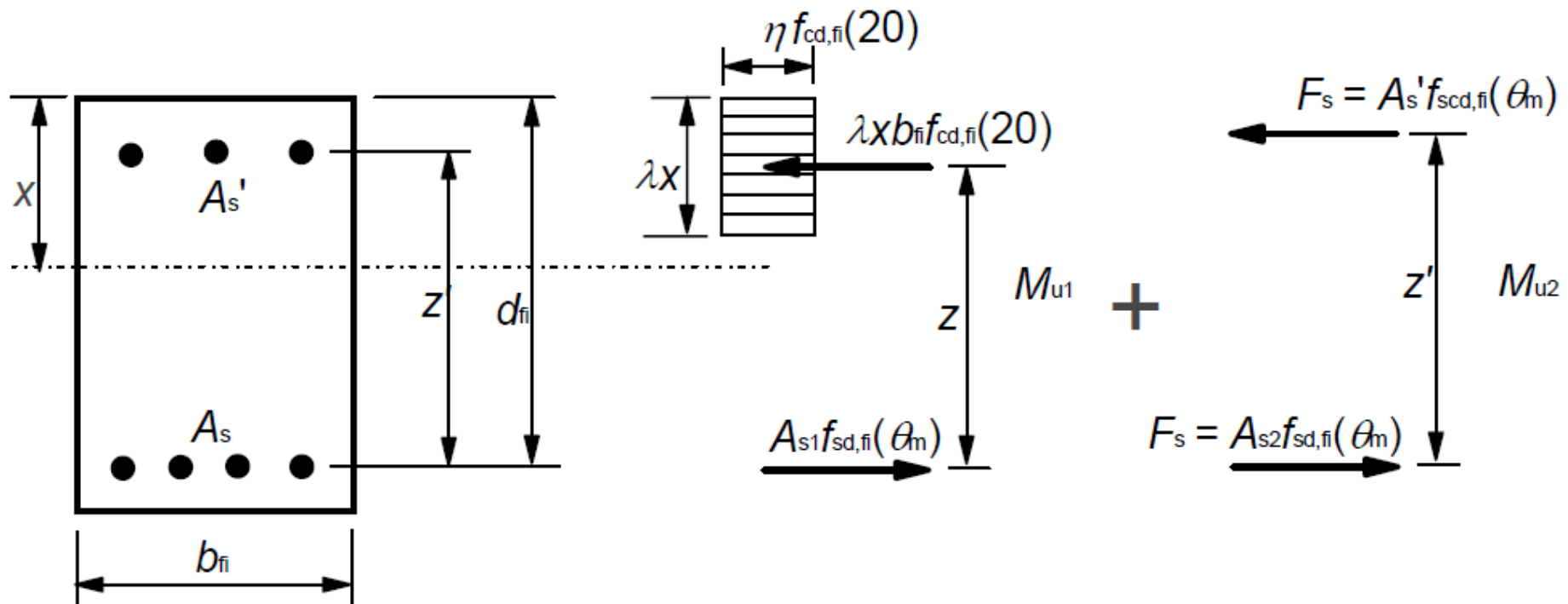
Cross section is divided in zones.
Mean temperature and corresponding strength of each zone is used

This method is more accurate for small cross sections than 500°C isotherm method



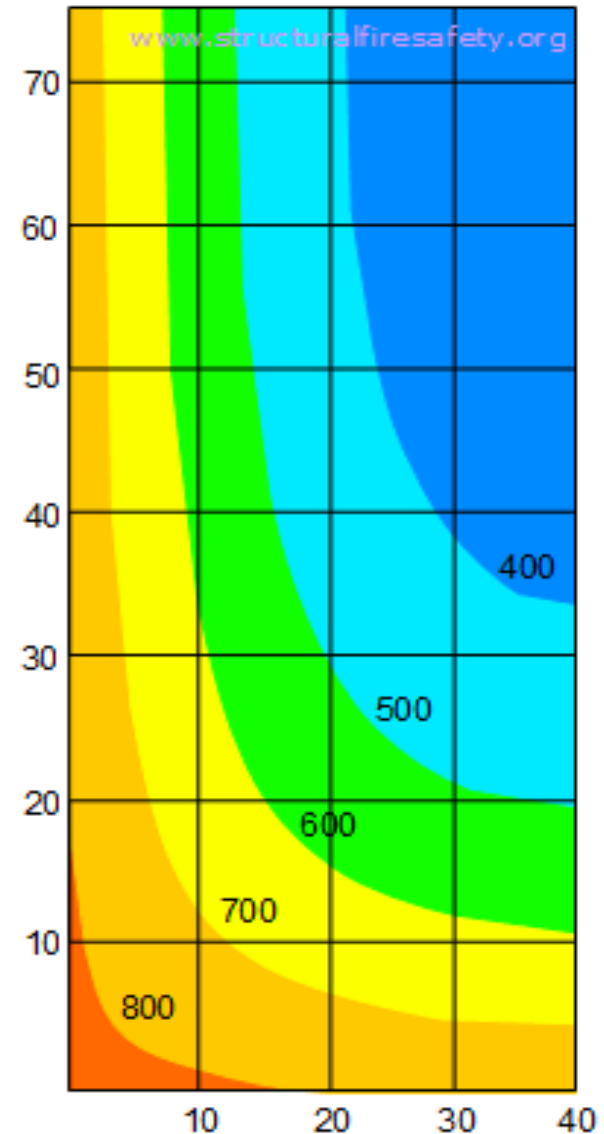


- Determine the 500°C isotherm and the reduced width b_{fi} and effective depth d_{fi}
- Determine the temperature of reinforcing bars and the reduced strength
- Use conventional calculation methods



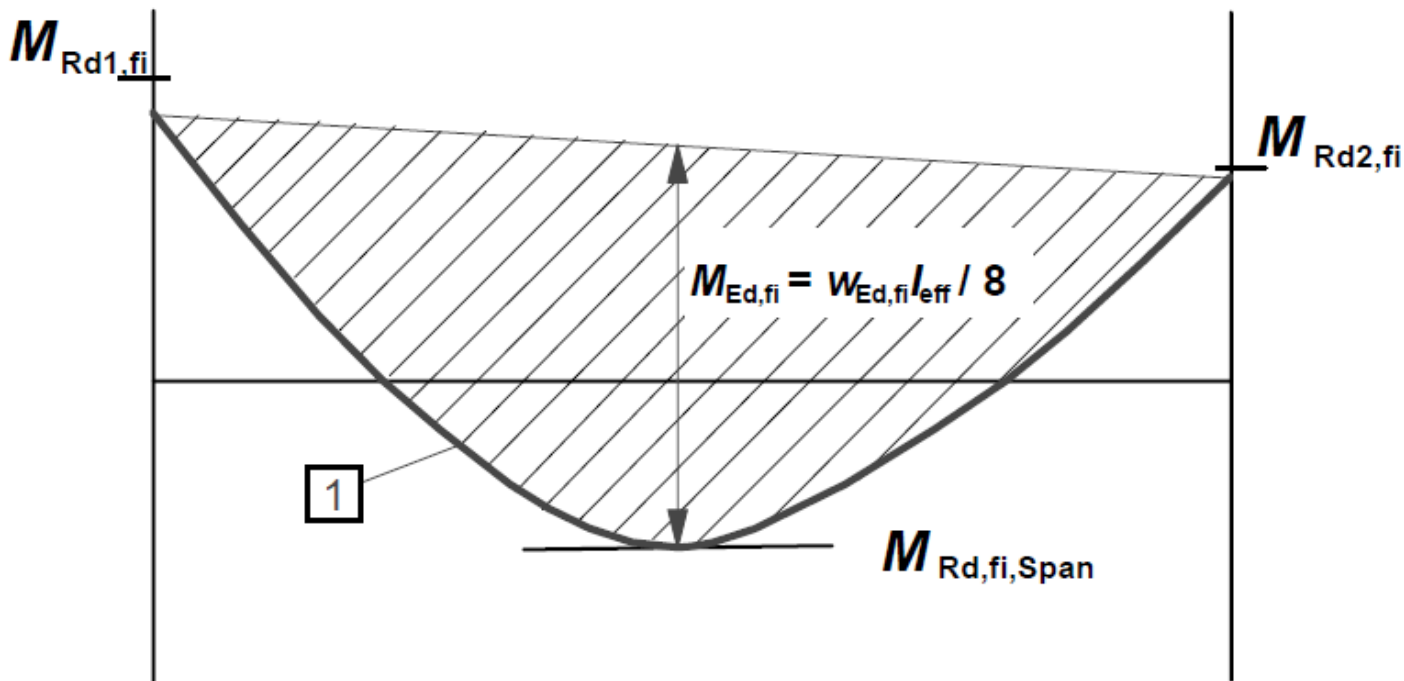


- **Temperature distribution in the cross section can be calculated from the thermal properties**
- **Annex A of EN 1992-1-2 gives temperature profiles for slabs, beams and columns**





- **Annex E**
- **Simplified method to calculate bending capacity for predominantly uniformly distributed loads**
- **This is some kind of extension of Tabulated data**



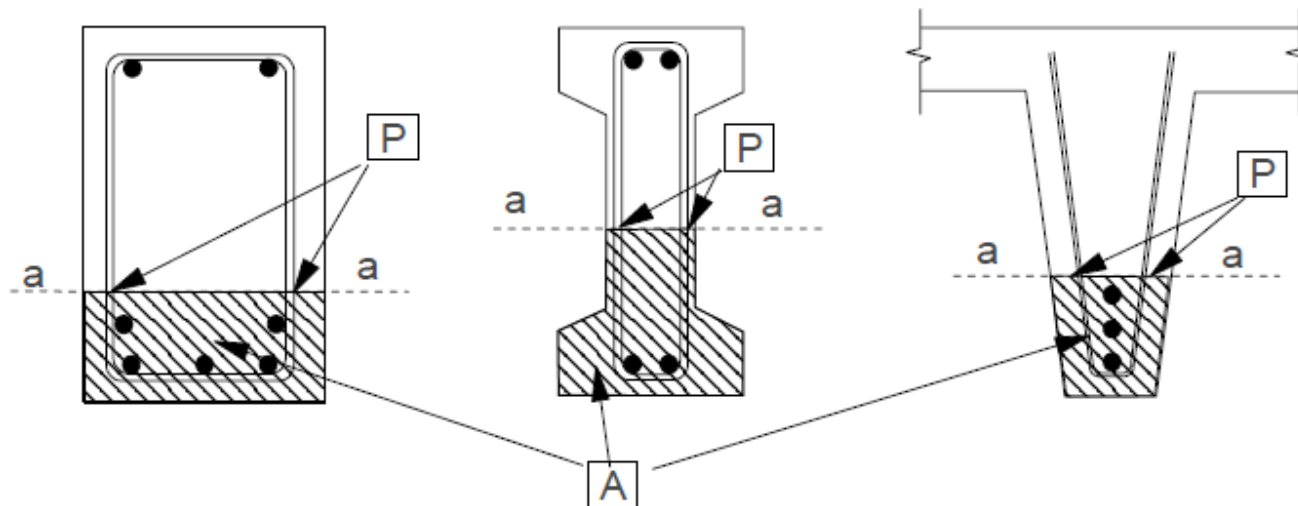
- 1 Free moment diagram for uniformly distributed load under fire conditions

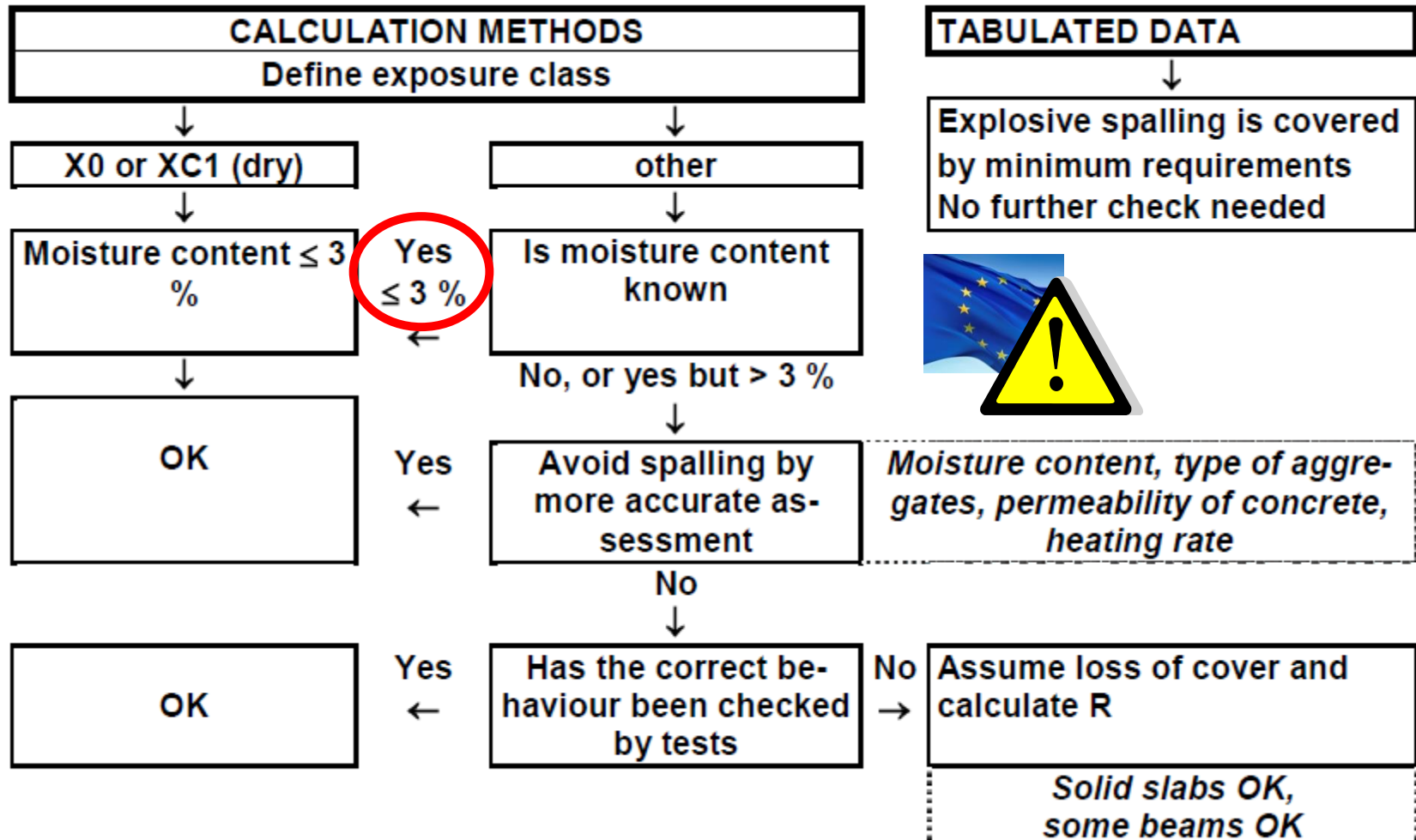


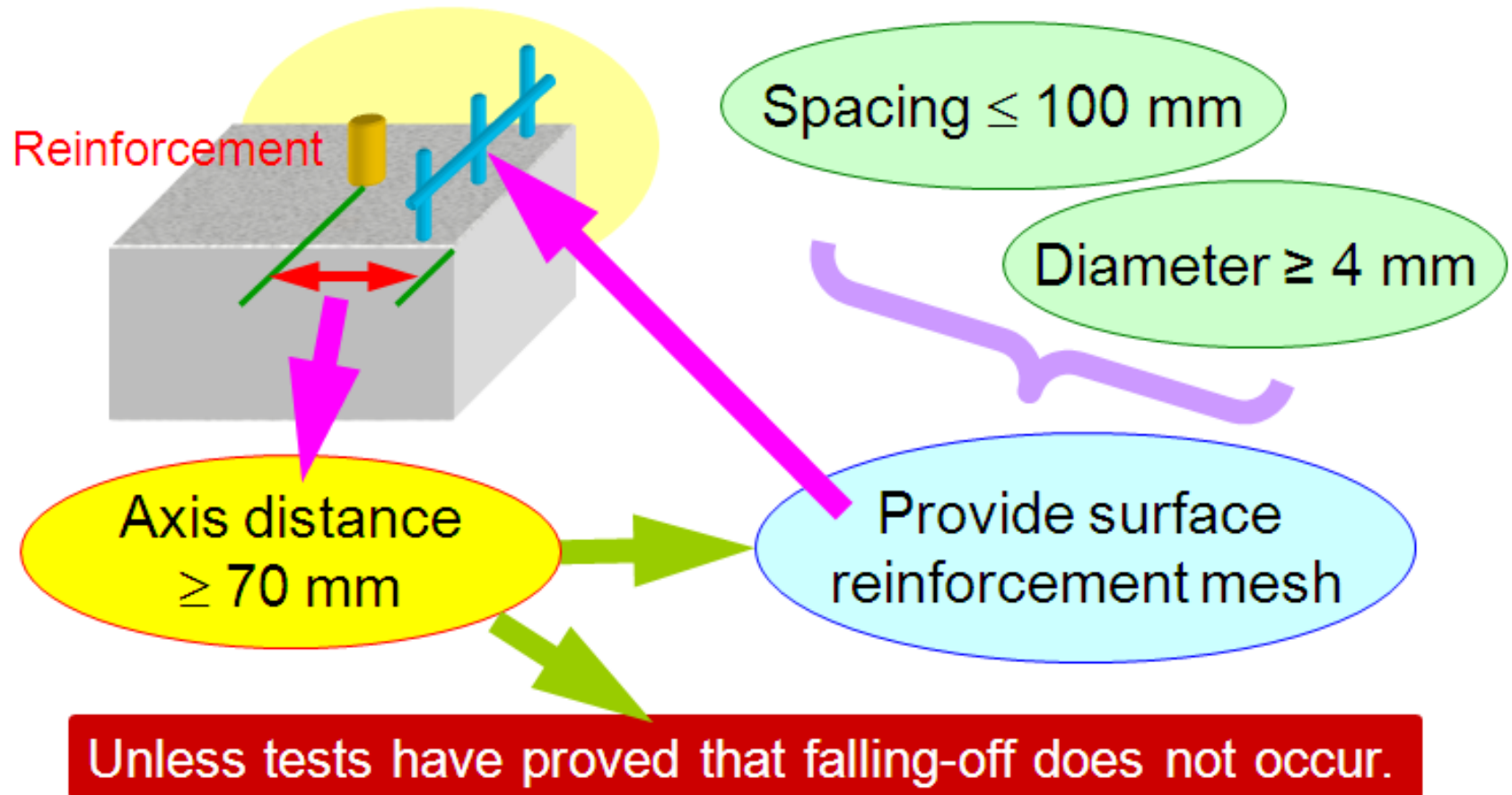
Annex D (informative)

- Shear failures due to fire are very uncommon. However, the calculation methods given in this Annex are not fully verified.

The reference temperature θ_p should be evaluated at points P along the line 'a-a' for the calculation of the shear resistance. The effective tension area A may be obtained from EN 1992-1 (SLS of cracking).









- (1) This section gives recognised design solutions for the **standard fire exposure up to 240 minutes**. The rules refer to **member analysis**.

Note: The tables have been developed on an empirical basis confirmed by experience and theoretical evaluation of tests. The data is derived from approximate conservative assumptions for the more common structural elements and is valid for the **whole range of thermal conductivity** in 3.3. More specific tabulated data can be found in the product standards for some particular types of concrete products or developed, on the basis of the calculation method in accordance with 4.2, 4.3 and 4.4.

- (2) The values given in the tables apply to **normal weight concrete** (2000 to 2600 kg/m³, made with **siliceous aggregates**.
If **calcareous aggregates** or lightweight aggregates are used in **beams or slabs** the **minimum dimension of the cross-section may be reduced by 10%**.
- (3) When using tabulated data **no further checks** are required concerning **shear and torsion capacity and anchorage details**.
- (4) When using tabulated data **no further checks** are required concerning **spalling, except for surface reinforcement**.



Tabulated data are based on a reference load level $\eta_{fi} = 0,7$, unless otherwise stated in the relevant clauses.

Note: Where the partial safety factors specified in the National Annexes of EN 1990 deviate from those indicated in 2.4.2, the above value $\eta_{fi} = 0,7$ may not be valid. In such circumstances the value of η_{fi} for use in a Country may be found in its National Annex.

For walls and columns load level η_{fi} or degree of utilisation μ_{fi} is included in the tables



TABULATED DATA FOR COLUMNS

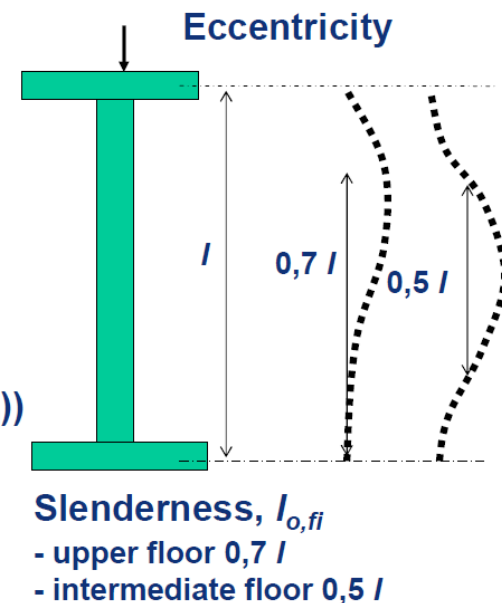
- **Two optional methods are given**
 - **Method A** is derived from test results, but field of application is limited to buckling length ≤ 3 m and first order eccentricity $\leq 0,15h$ to $0,4h$ (depending on the National Annex)
 - **Method B** is based on calculations, it is more conservative and many interpolations are needed. Limitations for normative table: eccentricity $\leq 0,25h$ and $\lambda_{fi} \leq 30$
9 pages of tables in Annex C

In Method A degree of utilisation:

$$\mu_{fi} = N_{Ed,fi} / N_{Rd}$$

In Method B load level is defined as:

$$n = N_{0Ed,fi} / (0,7(A_c f_{cd} + A_s f_{yd}))$$





TABULATED DATA FOR COLUMNS : tables for Method B

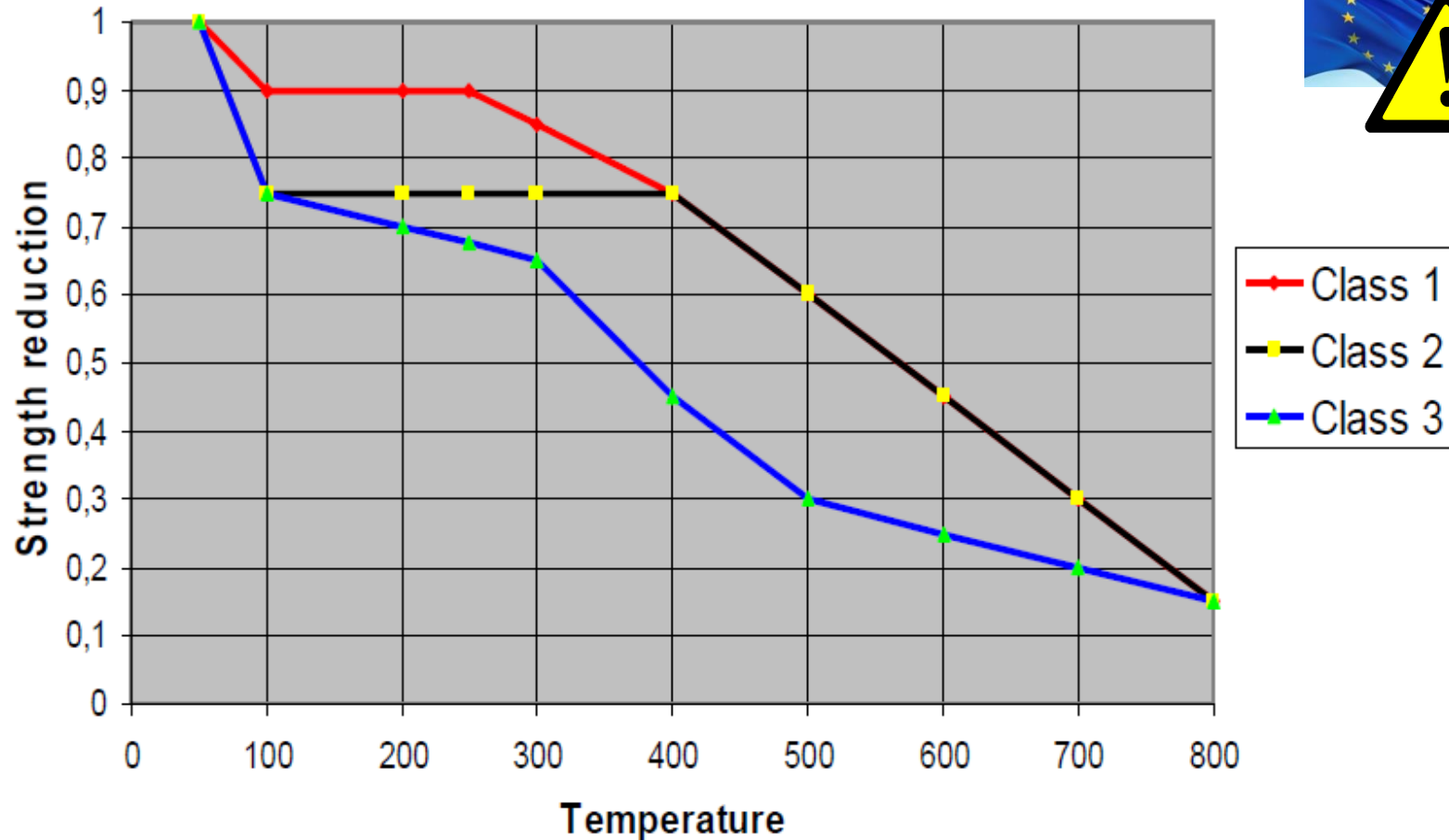
Standard fire resistance	Mechanical reinforcement ratio ω	Minimum dimensions (mm). Column width b_{min} /axis distance a			
		$n = 0,15$	$n = 0,3$	$n = 0,5$	$n = 0,7$
1	2	3	4	5	6
R 30	0,100	150/25*	150/25*	200/30:250/25*	300/30:350/25*
	0,500	150/25*	150/25*	150/25*	200/30:250/25*
	1,000	150/25*	150/25*	150/25*	200/30:300/25*
R 60	0,100	150/30:200/25*	200/40:300/25*	300/40:500/25*	500/25*
	0,500	150/25*	150/35:200/25*	250/35:350/25*	350/40:550/25*
	1,000	150/25*	150/30:200/25*	200/40:400/25*	300/50:600/30
R 90	0,100	200/40:250/25*	300/40:400/25*	500/50:550/25*	550/40:600/25*
	0,500	150/35:200/25*	200/45:300/25*	300/45:550/25*	500/50:600/40
	1,000	200/25*	200/40:300/25*	250/40:550/25*	500/50:600/45
R 120	0,100	250/50:350/25*	400/50:550/25*	550/25*	550/60:600/45
	0,500	200/45:300/25*	300/45:550/25*	450/50:600/25*	500/60:600/50
	1,000	200/40:250/25*	250/50:400/25*	450/45:600/30	600/60
R 180	0,100	400/50:500/25*	500/60:550/25*	550/60:600/30	(1)
	0,500	300/45:450/25*	450/50:600/25*	500/60:600/50	600/75
	1,000	300/35:400/25*	450/50:550/25*	500/60:600/45	(1)
R 240	0,100	500/60:550/25*	550/40:600/25*	600/75	(1)
	0,500	450/45:500/25*	550/55:600/25*	600/70	(1)
	1,000	400/45:500/25*	500/40:600/30	600/60	(1)
* Normally the cover required by EN 1992-1-1 will control.					
(1) Requires width greater than 600 mm. Particular assessment for buckling is required.					



- **Tables for loadbearing and non loadbearing wall**
- **Fire walls have been added**
 - Classification M, to be used only if there are national requirements
- **Tables for simply supported and continuous beams**
- **Tables for simply supported and continuous slabs, flat slabs, ribbed slabs**



Reduction of strength at elevated temperature



Concrete C 55/67 and C 60/75 is Class 1, concrete C 70/85 and C80/95 is Class 2 and **concrete C90/105 is Class 3.**



Spalling



Methods for concrete grades C 55/67 to C 80/95 with higher content of silica fume than 6% by weight of cement and for concrete grades $80/95 < C \leq$

Method A

Use reinforcement mesh with a nominal cover of 15 mm:

- Wire diameter ≥ 2 mm
- Pitch $\leq 50 \times 50$ mm
- Nominal cover to main reinforcement ≥ 40 mm

Method B

Use a type of concrete that will not spall under fire exposure – demonstrated by local experience or testing.

Method C

Use a protective layers which has been demonstrated that no spalling of concrete occurs under fire exposure.

Method D

Include in the concrete mix more than 2 kg/m^3 of monofilament propylene fibres.



- Thermal properties (thermal conductivity)
- specific structural design

Increase of minimum cross section by factor	Class 1	Class 2
- Walls and slabs exposed on one side	1,1	1,3
- Other structural members	1,2	1,6
Increase of axis distance by factor	1,1	1,3
Note: Factors are recommended values, and may be modified in National Annex		
Factor for axis distance in Class 2 seems to be too high, and it should not depend on the strength reduction		

Moment capacity reduction factors for beams and slabs	k_m	
	Class 1	Class 2
Beams	0,98	0,95
Slabs exposed to fire in the compression zone	0,98	0,95
Slabs exposed to fire in the tension side, $h_s \geq 120$ mm	0,98	0,95
Slabs exposed to fire in the tension side, $h_s = 50$ mm	0,95	0,85



- **Dissemination of information for training workshop, 18-20 February 2008, Brussels**
- **EN 1992-1-2 : 2004, The university of Manchester,**
www.structuralfiresafety.org
- **EN 1992-1-2 : 2004**



Part II

CASE STUDY (Caroline MORIN)



Objective

Apply the design methods presented in the Eurocode 2 ‘Design of concrete structures’ Part 1-2 ‘**Structural fire**’ on a structure exposed under fire

Methodology

Selection of 2 elements in the selected structure

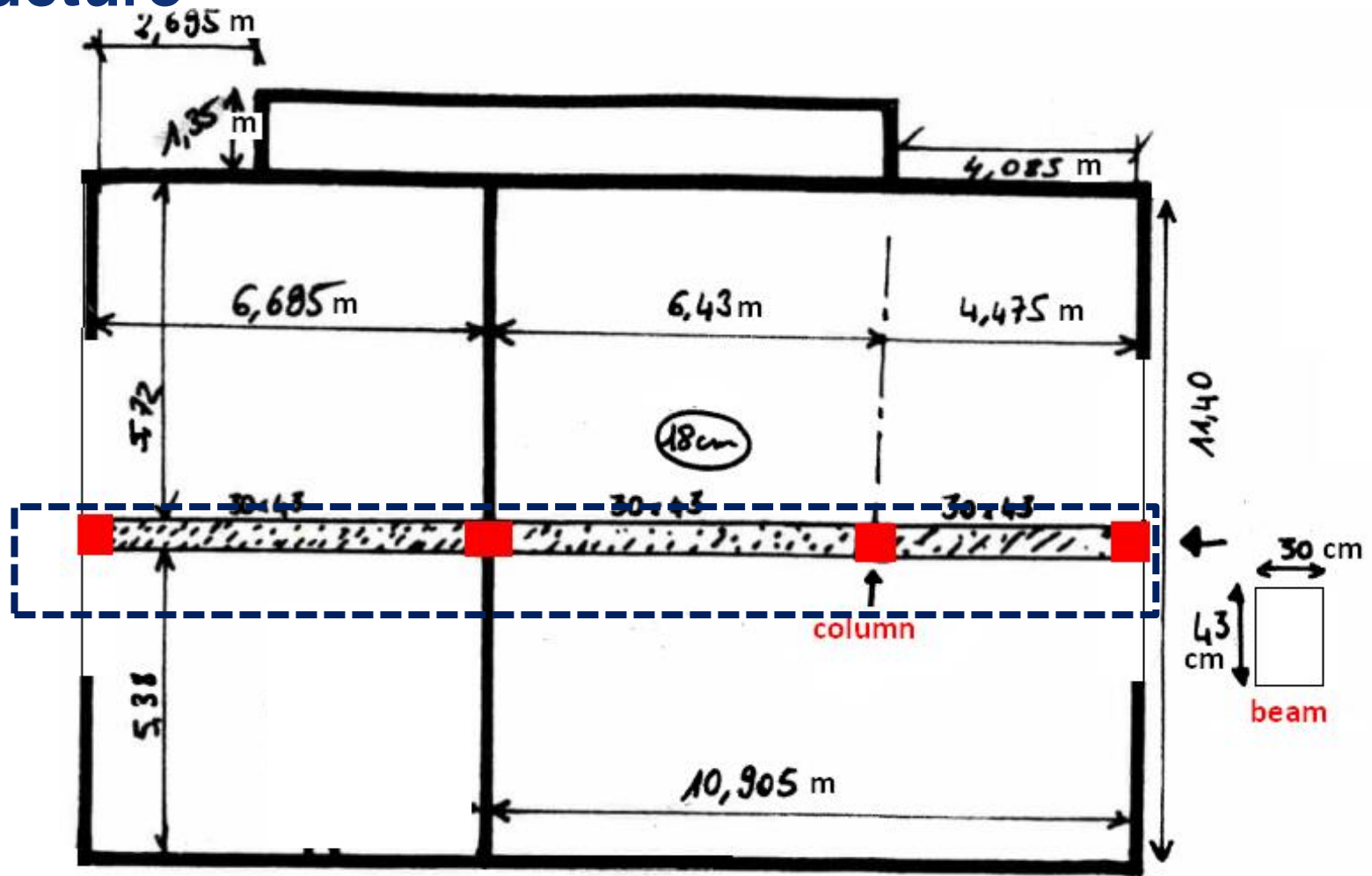
- A continuous beam
- A column

Verification of the design of the structure under a fire with:

- Tabulated data
- Simplified calculation method
- Advanced calculation method

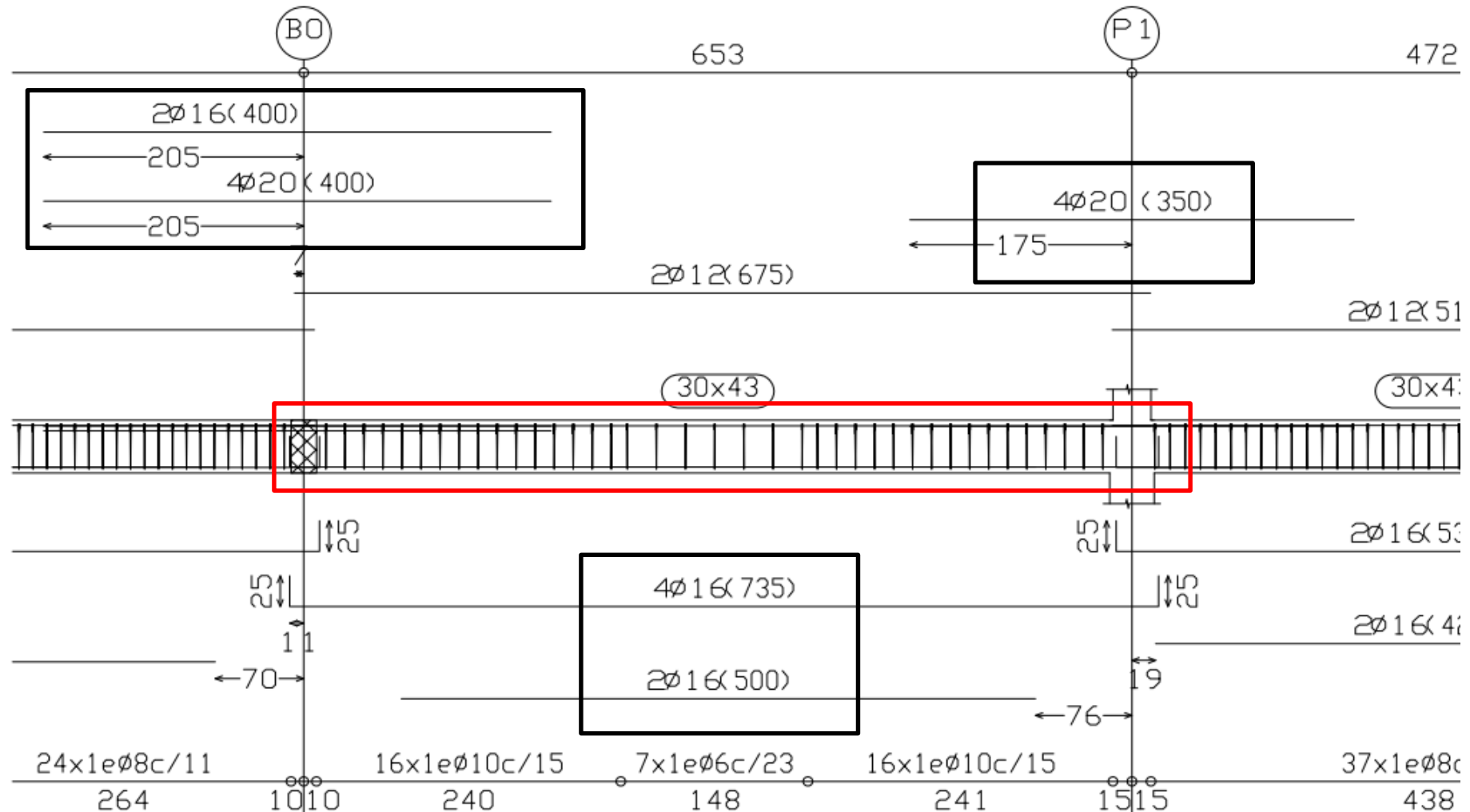


Structure





Reinforcing steel of the intermediate selected span





Sections

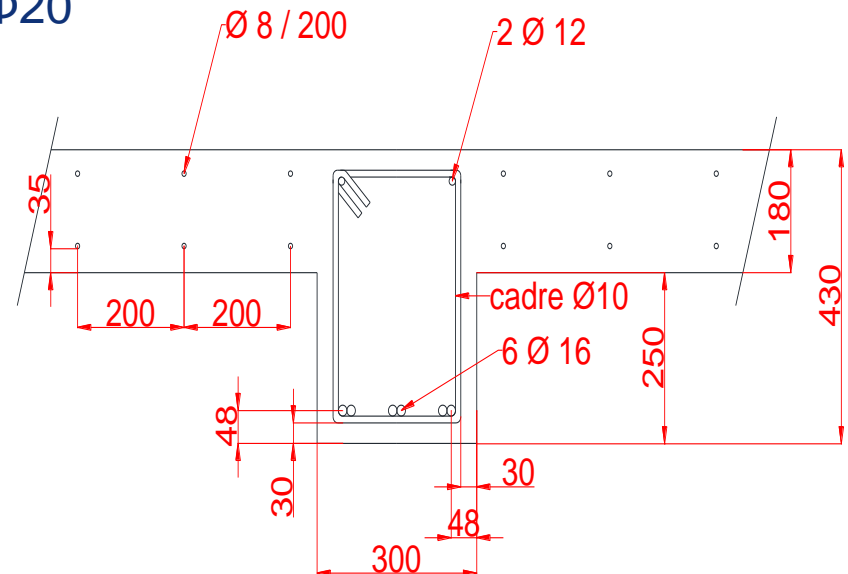
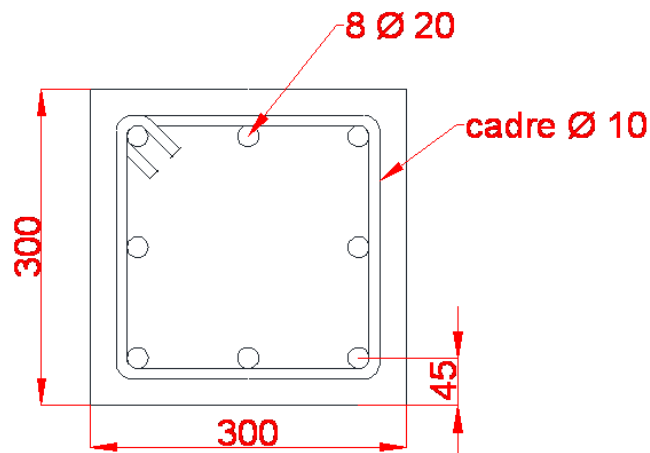
Beam

- $b=0.30 \text{ m} * h=0.43 \text{ m}$
- Bars in tension in the middle of the span: $6\Phi 16$, $a=48 \text{ mm}$
- Bars near the support (west side): $2\Phi 16$ ($a=68 \text{ mm}$) & $4\Phi 20$ ($a=50 \text{ mm}$)
- Bars near the support (east side): $4\Phi 20$ ($a=50 \text{ mm}$)

Column

- $b=0.30 \text{ m}$, $l=2.80 \text{ m}$, $a=45 \text{ mm}$
- Longitudinal reinforcing steel: $8\Phi 20$

measurements in mm





Scope (EN 1992-1-2, section 5.1 & 5.2)

Design solutions for the fire exposure **up to 240 minutes**

Normal weight concrete made with **siliceous aggregates**

No further checks are required concerning shear, torsion, anchorage

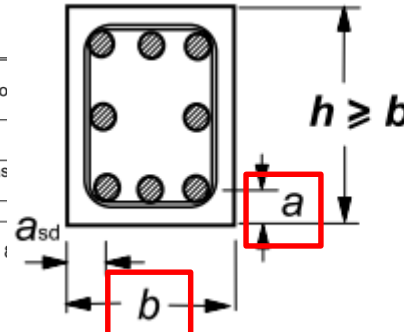
No further checks are required concerning spalling, except for surface reinforcement

General design rules

For load bearing function, minimum requirements concerning **section sizes** and **axis distance of steel reinforcement** are given

Symbol used in tables

Standard fire resistance	Minimum dimension					Class
	Possible combinations of a and b_{min} where a is the average axis distance and b_{min} is the width of beam					
	1	2	3	4	5	
1	2	3	4	5		
R 30	$b_{min}= 80$ $a = 15^*$	160 12*				

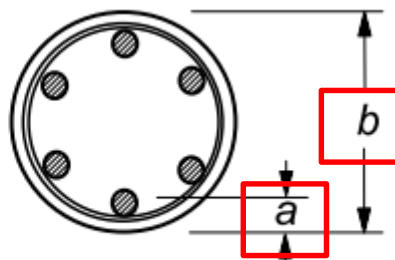


$h \geq b$

a_{sd}

a

b



a

b

Standard fire resistance	Mechanical reinforcement ratio ω	Minimum dimensions (mm). Column width b_{min} /axis distance a			
		$n = 0,15$	$n = 0,3$	$n = 0,5$	$n = 0,7$
1	2	3	4	5	6
R 30	0,100 0,500 1,000	150/25* 150/25* 150/25*	150/25* 150/25* 150/25*	200/30:250/25* 150/25* 150/25*	300/30:350/25* 200/30:250/25* 200/30:300/25*




Column characteristics

300/45, reinforcing steel $8\Phi 20$, length = 2.80 m

normal weight concrete made with **siliceous aggregates**

Standard fire exposure of 120 minutes, exposed on more than one side

Braced structure

$G = 232.3$ kN, $Q = 48.31$ kN et $\psi_{2,1} = 0.3$ ($\psi_{1,1} = 0.5$ EN 1992-1-2/NAF) 

Method A (Table 5.2a)

Validity of the method:

- Effective length of the column under fire conditions: $l_{0,fi} = 1.40$ m ≤ 3 m
- First excentricity under fire conditions: $e = 0.0021$ m $\leq 0.15b = 0.045$ m
- Amount of reinforcement: $A_s = 25,13$ cm² $\leq 0.04 A_c = 36$ cm²
- Reduction factor for the design level in the fire situation: $\mu_{fi} = N_{Ed,fi} / N_{Rd} = 0.1$

Standard fire resistance	Minimum dimensions (mm) Column width b_{min} /axis distance a of the main bars			
	Column exposed on more than one side			Exposed on one side
	$\mu_{fi} = 0.2$	$\mu_{fi} = 0.5$	$\mu_{fi} = 0.7$	$\mu_{fi} = 0.7$
1	2	3	4	5
R 120	250/40 350/35	Linear interpolation $\rightarrow 300/37.5$ 450/40** 450/51**		175/35



Column characteristics

300/45, reinforcing steel 8Φ20, length = 2.80 m

Normal weight concrete made siliceous aggregates

Standard fire exposure of 120 minutes, exposed on more than one side

Braced structures

G= 232.3 kN, Q= 48.31 kN

Method B (Table 5.2b)

Validity of the method:

- Load level at normal temperature conditions: **n=0.14**
- First excentricity under fire conditions: **e=0.0021 m**, **e/b=0.013 ≤ 0.25**
- Slenderness of the column under fire conditions: **λ_{fi}=l_{0,fi}/i=11.55 ≤ 30**
- Mechanical reinforcement ratio at normal temperatures conditions: **w=0.73**

$$n = N_{0Ed,fi} / (0,7(A_c f_{cd} + A_s f_{yd}))$$

$$\omega = \frac{A_s f_{yd}}{A_c f_{cd}} \quad e = M_{0Ed,fi} / (N_{0Ed,fi})$$

Standard fire resistance	Mechanical reinforcement ratio ω	Minimum dimensions (mm). Column width b_{min} /axis distance a			
		$n = 0,15$	$n = 0,3$	$n = 0,5$	$n = 0,7$
1	2	3	4	5	6
R 120	0,100	250/50:350/25*	400/50:550/25*	550/25*	550/60:600/45
	0,500	200/45:300/25*	300/45:450/25*	450/45:600/25*	500/60:600/50
	1,000	200/40:250/25*	250/50:400/25*	450/45:600/30	600/60

OK R120 (300/45)



Beam characteristics

300/48, reinforcing steel 6Φ16

Normal weight concrete made with siliceous aggregates,

Standard fire exposure of 120 minutes, exposed to fire on three sides

G= 40.85 kN.m, Q= 8.7 kN.m

Method for continuous beam (Table 5.6)

Minimum values of axis distance **a** to the soffit and sides of continuous beams together with minimum values of length **b**

Redistribution of bending moment for normal temperature design <15 %

Area of top reinforcement should be: $A_{s,req}(x) = A_{s,req}(0) \cdot (1 - 2,5x/l_{eff})$

Standard fire resistance	Minimum dimensions (mm)							
	Possible combinations of a and b_{\min} where a is the average axis distance and b_{\min} is the width of beam					Web thickness b_w		
						Class WA	Class WB	Class WC
1	2	3	4	5	6	7	8	
R 120	$b_{\min}= 200$ $a = 45$	300 35	450 35	500 30	300 35	300 35	300 35	

OK R120 (300/48)

OK R120 (300/48)



General (section 4.2)

Simplified cross-section calculations methods may be used to determine the **ultimate load-bearing capacity** of a heated cross section and **to compare the capacity with the relevant combination**

- **Informative Annex B:** 2 alternatives methods for calculating the resistance to bending moments: « **500°C isotherm method** » and « **Zone method** »

Standard fire exposure

Temperature profiles determined from calculation or tests

Reduced cross-section


Strength reduction of materials

Note: for shear and anchorage, when minimum dimensions given in tabulated data are followed, further checks for shear and anchorage are not required (section 4.4)



Continuous beam

Recall of data

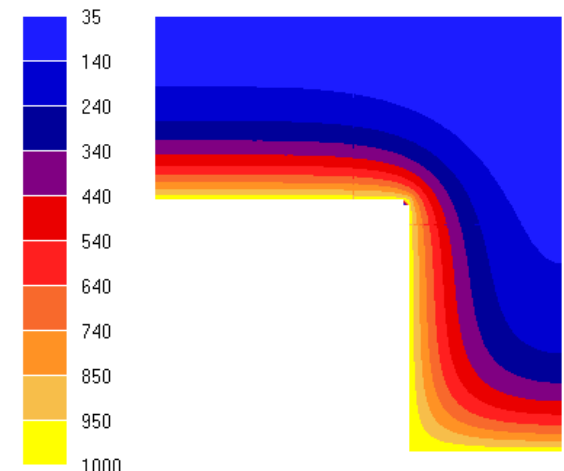
- $l=6.43$ m, $b=0.30$ m, $h=0.40$ m, $h_{\text{slab}}=0.18$ m
- Hot rolled reinforcing steel: $6\Phi 16$, $a=48$ mm
- West top reinforcement: $4\Phi 20 + 2\Phi 16$, $a_1=50$ mm et $a_2=68$ mm
- East top reinforcement: $4\Phi 20$, $a=50$ mm
- Siliceous aggregates, $f_{\text{ck}}=25$ MPa
- $G=40.85$ kN.m, $Q=8.7$ kN.m et $\psi_{1,1}=0.5$ 

Method B1 valid with a minimum cross-section $b=0.30$ m > 0.16 m

Fire resistance	R 60	R 90	R 120	R 180	R 240
Minimum width of cross-section mm	90	120	160	200	280

Temperature profiles: Fire exposure up to 120 min
Reduced cross section

- **500°C isotherm method** → $a_{500^\circ\text{C}}$
- $b_{\text{fi}}=0.210$ m
- $h_{\text{fi}}=0.365$ m





Continuous beam

Temperature of reinforcing bars in tension

Reduced strength of the reinforcement due to the temperature

- $k_{moy}=0.515$
- $f_{yd,fi}=k_{moy} * f_{yk} / \gamma_{s,fi} = 0.515 * 500 / 1 = 257.37 \text{ MPa}$
- $d_{fi}=d=0.390 \text{ m}$
- $A_s * f_{yd,fi} = A_s * k_{moy} * f_{yk} / \gamma_{s,fi} = 12.06 \text{E-4} * 257.37 = 0.310 \text{ MN}$

Reinforcement	x (mm)	y (mm)	T (°C)	Asi (mm²)	ksi	ks.As (mm²)	ai.ksi.Asi (mm3)
1	40	48	692	201	0,2492	50	2405
2	56	48	617	201	0,4292	86	4142
3	142	48	461	201	0,8658	174	8356
1'	260	48	692	201	0,2492	50	2405
2'	244	48	617	201	0,4292	86	4142
3'	158	48	461	201	0,8658	174	8356

Bending strength moment: $M_{Rd,fi} = z * A_s * k_{moy} * f_{yk} / \gamma_{s,fi} = 116.39 \text{ kN.m}$

Comparison with a software CIM'feu EC2: $M_{Rd,fi} = 121.04 \text{ kN.m (+4\%)}$



Continuous beam

Temperature of reinforcing bars (in the west side)

Reduced strength of the reinforcement due to the temperature

- $k_{moy}=1$
- $f_{yd,fi}=k_{moy} * f_{yk} / \gamma_{s,fi} = 1 * 500 / 1 = 500 \text{ MPa}$
- $d_{fi}=0.309 \text{ m}$
- $A_s * f_{yd,fi} = A_s * k_{moy} * f_{yk} / \gamma_{s,fi} = 17.59 \text{E-4} * 500 = 0.880 \text{ MN}$

Reinforcement	x (mm)	y (mm)	T (°C)	Asi (mm ²)	ksi	ks.As (mm ²)	ai.ksi.Asi (mm ³)
1	40	50	69	314	1	314	15708
2	140	50	43	314	1	314	15708
1'	160	50	43	314	1	314	15708
2'	260	50	69	314	1	314	15708
3	40	68	82	251	1	251	17090
3'	260	68	82	251	1	251	17090

Strength moment: $M_{Rd,w,fi} = z * A_s * k_{moy} * f_{yk} / \gamma_{s,fi} = 206.64 \text{ kN.m}$

Comparison with a software CIM'feu EC2: $M_{Rd,w,fi} = 199.57 \text{ kN (- 3 \%)}$



Continuous beam

Temperature of reinforcing bars (in the east side)

Reduced strength of the reinforcement due to the temperature

- $k_{moy}=1$
- $f_{yd,fi}=k_{moy} * f_{yk} / \gamma_{s,fi} = 1 * 500 / 1 = 500 \text{ MPa}$
- $d_{fi}=0.315 \text{ m}$
- $A_s * f_{yd,fi} = A_s * k_{moy} * f_{yk} / \gamma_{s,fi} = 12.56 \text{E-4} * 500 = 0.628 \text{ MN}$

Reinforcement	x (mm)	y (mm)	T (°C)	Asi (mm ²)	ksi	ks.As (mm ²)	ai.ksi.Asi (mm ³)
1	40	50	69	314	1	314	15700
2	140	50	43	314	1	314	15700
1'	160	50	43	314	1	314	15708
2'	260	50	69	314	1	314	15708

Strength moment: $M_{Rd,e,fi}=172.61 \text{ kN.m}$

Comparison with a software CIM'feu EC2: $M_{Rd,e,fi}=169.01 \text{ kN.m}$ (-2%)

Bending moment for a simply supported beam: $M_{Ed0,fi}=241 \text{ kN.m}$

Total bending strength: $M_{Rd,fi}=306 \text{ kN.m} > M_{Ed0,fi}=241 \text{ kN.m}$ OK R120

Comparison with CIM'feu EC2: $M_{Rd,fi}=305.33 \text{ kN.m}$ (-0.2%)



Column

General data

- $b=0.30$ m, $l=2.80$ m
- Hot rolled reinforcing steel: $8\Phi 20$, cover = 35 mm ($a=45$ mm)
- Siliceous aggregates, $f_{ck}=25$ MPa
- $N_G=232.3$ kN.m, $N_Q=48.31$ kN.m et $\psi_{1,1}=0.5$

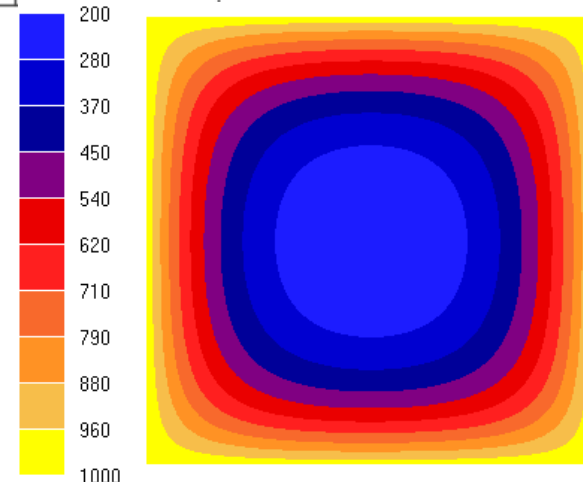
« 500 °C isotherm method », $b=0.30$ m $>$ 0.16 m

Fire resistance	R 60	R 90	R 120	R 180	R 240
Minimum width of cross-section mm	90	120	160	200	280

Temperature profiles: Fire exposure up to 120 min

Reduced cross section

- 500°C isotherm method $\rightarrow a_{500^\circ\text{C}}=55$ mm
- $b_{fi}=0.190$ m





Column

Taking into account of the 2nd order effect? $\lambda_{lim} = 20 \cdot A \cdot B \cdot C / \sqrt{n}$

- $A=0.7$
- Mechanical reinforcement ratio under fire exposure $\omega=0.77 \rightarrow B=1.597$
- $C=0.7$
- $n=N_{ed,fi}/A_c \cdot f_{cd}=0.284$
- Limit slenderness $\lambda_{lim}=29.36$
- Slenderness $\lambda=l_{0,fi}/i=25.52 < \lambda_{lim} \rightarrow$ we can neglect the 2nd order effect

Strength of the cross-section: $N_{Rd,fi}=1.60$ MN

Design normal effort: $N_{Ed,fi}=0.256$ MN

$N_{Ed,fi}=0.256$ MN $< N_{Rd,fi}=1.60$ MN \rightarrow OK R120



General

A realistic analysis of the structure exposed to fire

Reliable approximation of the expected behaviour of the structure

Include calculation models for:

- Development and distribution of the temperature within structural members = **thermal response**
- Mechanical behaviour of the structure = **mechanical response**



Hypothesis for the modelling

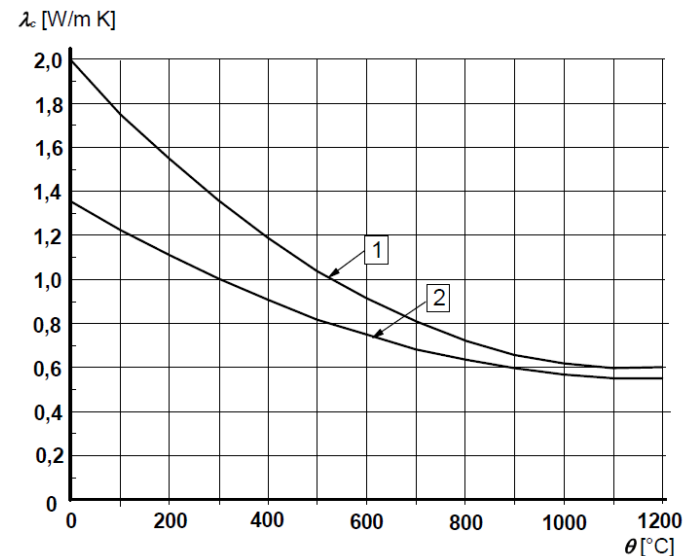
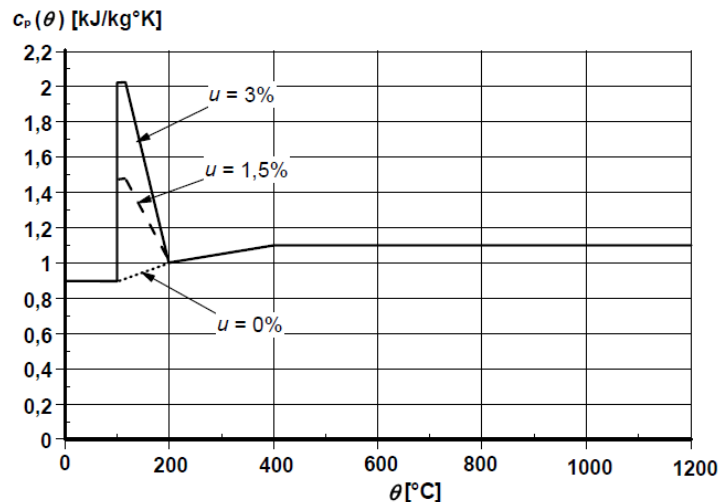
Thermal response (EC1-1-2)

- Based on principles and assumptions of the **theory heat transfer**

- Convection, radiation
- Thermal transmittance coefficient on the unexposed face ($\alpha_c = 4 \text{ W/m}^2\text{K}$)
- Thermal transmittance coefficient on the exposed face ($\alpha_c = 25 \text{ W/m}^2\text{K}$)
- Standard fire exposure

$$\theta_g = 20 + 345 \log_{10} (8t + 1) \quad [^{\circ}\text{C}]$$

- Include the relevant **thermal actions** (EN 1991-1-2), the **temperature dependent thermal properties of the materials**, the influence of

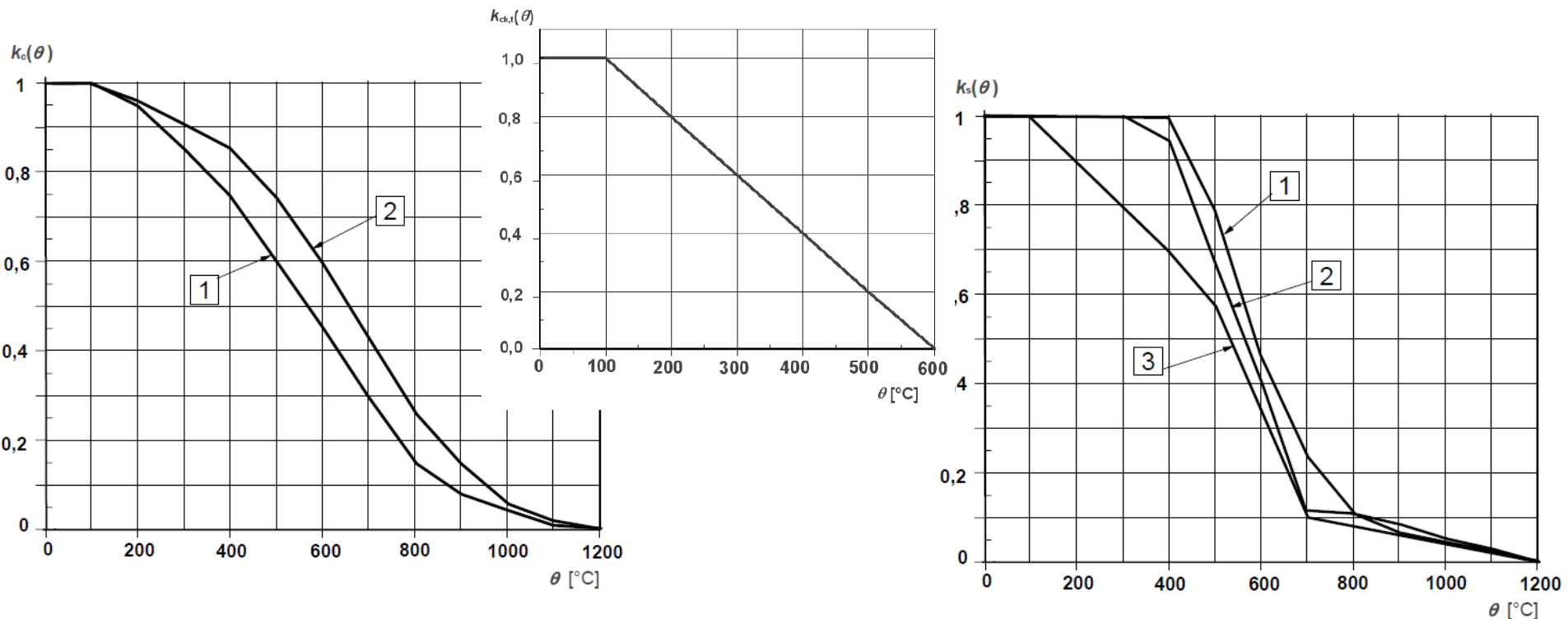




Hypothesis for the modelling

Mechanical response

- Based on the principles and assumptions of the theory of structural mechanics, taking into account the **changes of mechanical properties with temperature**
- Loads G, Q**

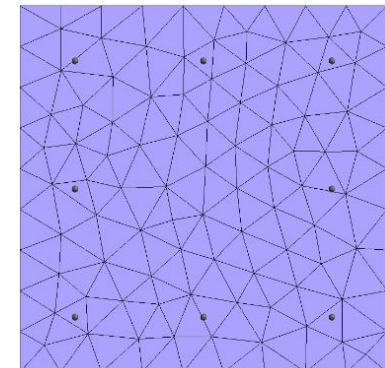
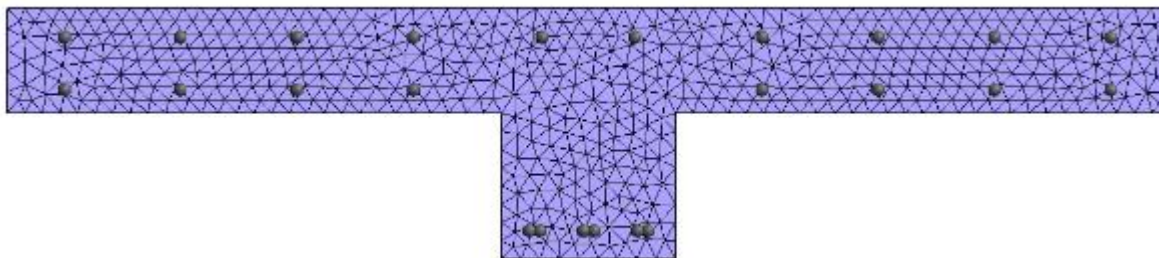
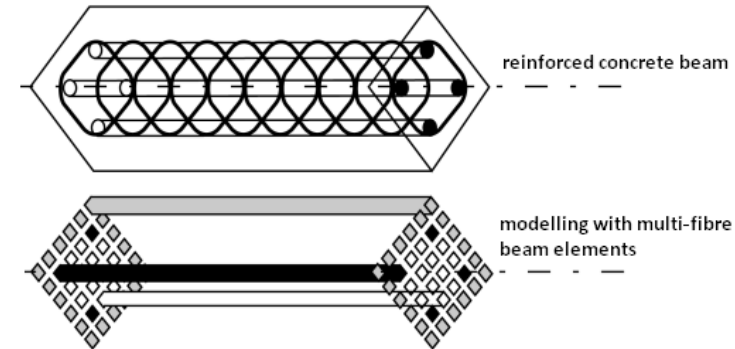
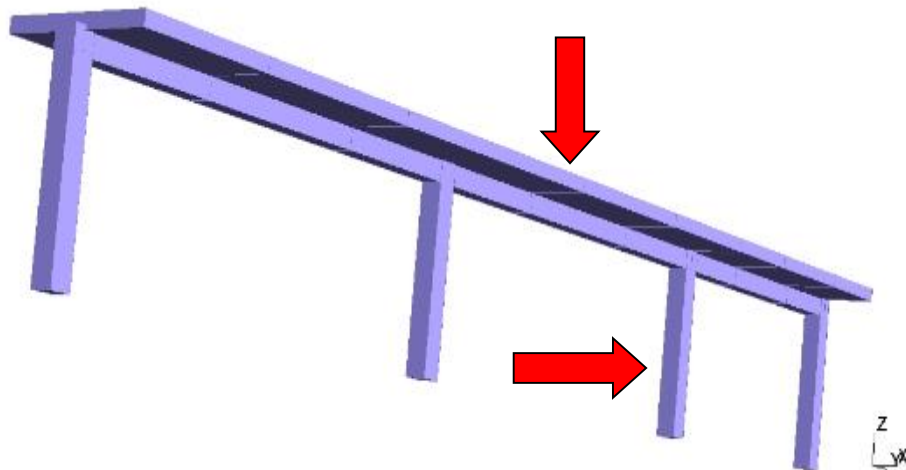




Modeling of the structure

Aster Code

Meshes using multi-fibre beam elements

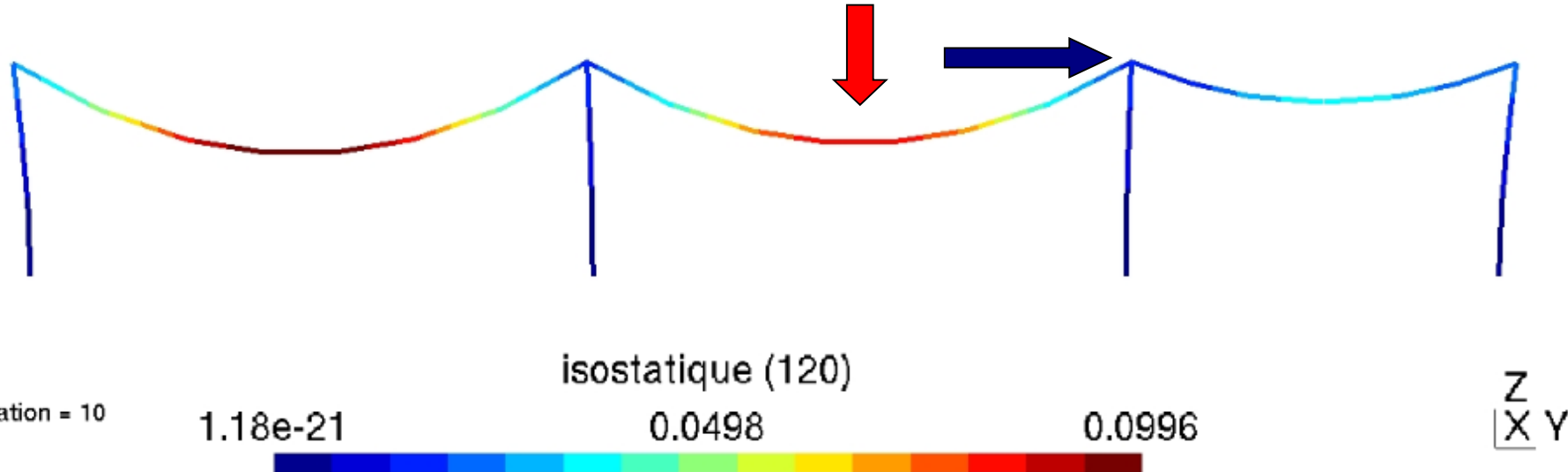




Results & analysis in terms of deflections

Vertical deflection of the middle of the beam (< 10 cm)

Horizontal displacement at the head of the column



Calculations → structure strength during 180 minutes (> 120 minutes)